

***Digital Image Processing and Analysis Applications
with MATLAB and CVIPtools 3rd edition Umbaugh
Solutions Manual***

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Solutions for Chapter 2: Computer Imaging Systems

1. hardware and software.
2. Gigabyte Ethernet, Firewire, USB 3.0, Camera Link.
3. It samples an analog video signal to create a digital image. This sampling is done at a fixed rate when it measures the voltage of the signal and uses this value for the pixel brightness. It uses the horizontal synch pulse to control timing for one line of video (one row in the digital image), and the vertical synch pulse to tell the end of a field or frame
4. A sensor is a measuring device that responds to various parts of the EM spectrum, or other signal that we desire to measure. To create images the measurements are taken across a two-dimensional grid, thus creating a digital image.
5. A range image is an image where the pixel values correspond to the distance from the imaging sensor. They are typically created with radar, ultrasound or lasers.
6. The reflectance function describes the way an object reflects incident light. This relates to what we call color and texture it determines how the object looks.
7. Radiance is the light energy reflected from, or emitted by, an object; whereas irradiance is the incident light falling on a surface. So radiance is measured in $\text{Power}/(\text{Area})(\text{SolidAngle})$, and irradiance is measured in Power/Area .
8. A photon is a massless particle that is used to model EM radiation. A CCD is a charge-coupled device. Quantum efficiency is a measure of how effectively a sensing element converts photonic energy into electrical energy, and is given by the ratio of electrical output to photonic input.

9. See fig 2.2-5 and use the lens equation: $\frac{1}{a} + \frac{1}{b} = \frac{1}{f}$. If the object is at infinity:

$$\frac{1}{\infty} + \frac{1}{b} = \frac{1}{f} = 0 + \frac{1}{b} = \frac{1}{f}; \therefore f = b$$

10.

$$\begin{aligned} N &= \delta A \delta t \int b(\lambda) q(\lambda) d\lambda \\ &= 20(10 \times 10^{-3}) \int_{400}^{700} 600 \lambda (0.95) d\lambda \\ &= 114 \int_{400}^{700} \lambda d\lambda = 114 \left[\frac{\lambda^2}{2} \right]_{400}^{700} = 114 (165,000) = 1.881 \times 10^7 \end{aligned}$$

13. With interlaced scanning, a frame in 1/30 of a second is a field rate of 1/60 of a second. Here we 240 lines per field and 640 pixels per line which gives (240)(640) = 153,600 pixels in 1/60 of a second. So the sampling rate must be:

$$\frac{153,600 \text{ pixels}}{1/60 \text{ sec}} = 9.216 \times 10^6; \text{ or about 9 megahertz}$$

12. Gamma rays have the most energy, radio waves have the least. For human life, more energy is more dangerous.

13. UV is used in fluorescence microscopy, and IR images are used in remote sensing, law enforcement and fire detection.

14. Acoustic imaging works by sending out pulses of sonic energy (sound) at various frequencies, and then measuring the reflected waves. The time it takes for the reflected signal to appear contains distance information, and the amount of energy reflected contains information about the object's density and material. The measured information is then used to create a two or three dimensional image. It is used in geological applications, for example oil and mineral exploration, typically use low frequency sounds (around hundreds of hertz). Ultrasonic, or high

frequency sound, imaging is often used in manufacturing to detect defects and in medicine to “see” inside opaque objects such as a woman’s womb to image a developing baby.

15. Electron microscopes can magnify much more than light microscopes, 1,000 compared to 200,000 times. It uses a focused beam of electrons instead of light energy to image the objects.

16. 1) structured lighting created with a laser and rotating mirrors, 2) time-of-flight using a transmitter and receiver and various types of signals.

17. An *optical image* is a collection of spatially distributed light energy. Optical images can be represented as video information in the form of analog electrical signals, and these are sampled to generate the digital image $I(r,c)$.

18. A “real” image is measured by a sensor, a computer image is generated by software often using a mathematical model.

19. Binary images are 1-bit per pixel (bpp), gray-scale typically 8 bpp, color typically 24 bpp, and multispectral images can be many more bpp. With fewer bpp, we have less information, but smaller files. Binary images contain only shape information, gray-scale images contain brightness information, and color images have brightness information typically in three spectral bands. Multispectral images have more than 3 bands and typically include information outside of the human visual spectrum.

20. Often to decouple the brightness and the color information, which creates a more people-oriented way of describing colors. Hue/Saturation/Lightness (HSL) color transform allows us to describe colors in terms that we can more readily understand (see Figure 2.4-3). The *lightness* (also referred as *intensity* or *value*) is the brightness of the color, and the *hue* is what we normally think of as “color”; for example green, blue or orange. The *saturation* is a measure of

how much white is in the color; for example, pink is red with more white, so it is less saturated than a pure red.

21. It means that two different colors in one part of the color space will not exhibit the same degree of perceptual difference as two colors in another part of the color space, even though they are the same "distance" apart (see Figure 2.4-7). $L^*u^*v^*$ and $L^*a^*b^*$ are examples of perceptually uniform color spaces.

22. Inverse spherical coordinate transform (SCT):

$$R = L \sin(\text{Angle}A) \cos(\text{Angle}B)$$

$$G = L \sin(\text{Angle}A) \sin(\text{Angle}B)$$

$$B = L \cos(\text{Angle}A)$$

Inverse cylindrical coordinate transform (CCT):

$$R = d \cos \theta$$

$$G = d \cos(\pi/2 - \theta)$$

$$B = z$$

23. For color printing we use a subtractive color model, where we consider subtracting cyan, magenta or yellow (CMY) from white, such as printing on white paper illuminated by white light. The model for white light is that it consists of red, green and blue. The CMY conversion from RGB is defined as follows (these equations assume that the RGB values are normalized to the range of 0 to 1):

$$C = 1 - R$$

$$M = 1 - G$$

$$Y = 1 - B$$

Cyan absorbs red light, magenta absorbs green and yellow absorbs blue. Thus, to print a normalized RGB triple that appears green, (0,1,0), we would use CMY (1,0,1). For this example the cyan will absorb the red light and the yellow absorbs the blue light, leaving only the green

light to be reflected and seen. Also, to print black we print all three (CMY) inks, and all the components of white light, RGB, will be absorbed. In practice, this produces a poor looking black, so black ink is added to the printing process leading to a four-color printing system, called CMYK.

For example, if $(R,G,B) = (100,50,200)$

$$\text{Cyan} = 1 - R = 1 - 100/255 \approx 0.608$$

$$\text{Magenta} = 1 - G = 1 - 50/255 \approx 0.804$$

$$\text{Yellow} = 1 - B = 1 - 200/255 \approx 0.216$$

24. *Bitmap images* (also called raster images) can be represented by our image model, $I(r,c)$, where we have pixel data and the corresponding brightness values stored in some file format.

Vector images refers to methods of representing lines, curves and shapes by storing only the key points and then using this information to create a bitmap image by a process called rendering.

25. 1) the number of rows (height), 2) the number of columns (width), 3) the number of bands, 4) the number of bits per pixel (bpp), and 5) the file type.

26. VIP (Visualization in Image Processing) format. Standard image file types were not used because they may not handle floating point, complex data, any size, multiple bands and a special history data structure that allows the maintenance of a record of operations that have been performed on the image

27. Experiment with CVPITools.

Supplementary Exercises:

1. a) $f\text{-number} = \frac{f}{D_{\text{effective}}}$. The focal length, f , is fixed. We can change the f-number by

changing the effective diameter by varying the aperture. As the effective diameter goes up, the f-number goes down, and vice versa. b) The amount of light energy that is intercepted by the lens

is proportional to the area on which the light energy falls. In this case, the area of the circle of the lens with diameter D : $\text{Area} = \pi r^2 = \pi(D/2)^2 = (\pi/4)D^2$. So, we can see that the area is inversely

to the f-number squared $= \frac{1}{(f - \text{number})^2} = \left(\frac{D_{\text{effective}}}{f} \right)^2$. Since the area is proportional to the light

energy, or brightness, the image brightness is inversely proportional to the f-number squared.

b) **Alternate explanation:** Measuring the brightness by measuring the number of electrons liberated, and using K as a constant to represent that we have a fixed time interval and a constant incident photon flux, we can say:

$$N = \delta A \delta t \int b(\lambda) q(\lambda) d\lambda = \text{Brightness} = \pi \left(\frac{D_{\text{eff}}}{2} \right)^2 K = \frac{K\pi}{4} (D_{\text{eff}})^2$$

$$\therefore (D_{\text{eff}})^2 = \frac{4(\text{Brightness})}{K\pi}$$

Where we use the area of the circular lens with D_{eff} as the effective lens diameter. Now since the

f-number is given by: $f - \text{number} = \frac{f}{D_{\text{eff}}}$ and $(f - \text{number})^2 = \frac{f^2}{(D_{\text{eff}})^2}$, putting these two

equations together:

$$(f - \text{number})^2 = \frac{f^2 K\pi}{(\text{Brightness})4} \rightarrow \text{Brightness} = \frac{f^2 K\pi}{4(f - \text{number})^2}$$

2. See figure 2.2-6 and apply similar triangles:

$$\frac{c/2}{b'-b} = \frac{d/2}{b'}$$

$$c/2 = \frac{(b'-b)d/2}{b'}$$

$$c = \frac{d}{b'} |b - b'|$$

3.

$$\begin{aligned} N &= \delta A \delta t \int b(\lambda) q(\lambda) d\lambda \\ &= 1000 (10) \int_{400}^{700} 1/(5\lambda + 8)^2 (0.8) \lambda d\lambda \\ &= 8,000 \int_{400}^{700} \lambda / (5\lambda + 8)^2 d\lambda = 8,000 \left[\frac{8}{25(5\lambda + 8)} + \frac{1}{25} \ln |5\lambda + 8| \right]_{400}^{700} \approx 178 \end{aligned}$$

$$4. \text{ See Figure 2.2.6. Blur circle} = \frac{50}{10.05025126} |10.03344482 - 10.05025126| = 0.0834 \text{ mm}$$

Therefore, image is clear since blur circles less than the resolution of device

$$5. \ 1/a + 1/b = 1/50, \text{ and, } a + b = 200; \text{ therefore, } a = b = 100$$

$$6. \text{ See Figure 2.4.9. a) 0 b) 255 c) } (455 + 333) = 788. \ 788/(577 + 333) = 0.865934.$$

$$(0.865934) \times 255 \approx 221$$

$$7. \text{ See Figure 2.2.6. Blur circle} = \frac{100}{10.033445} |10.033445 - 10.025063| = 0.0835 \text{ mm}$$

Therefore, image is slightly blurry since blur circles greater than the resolution of device

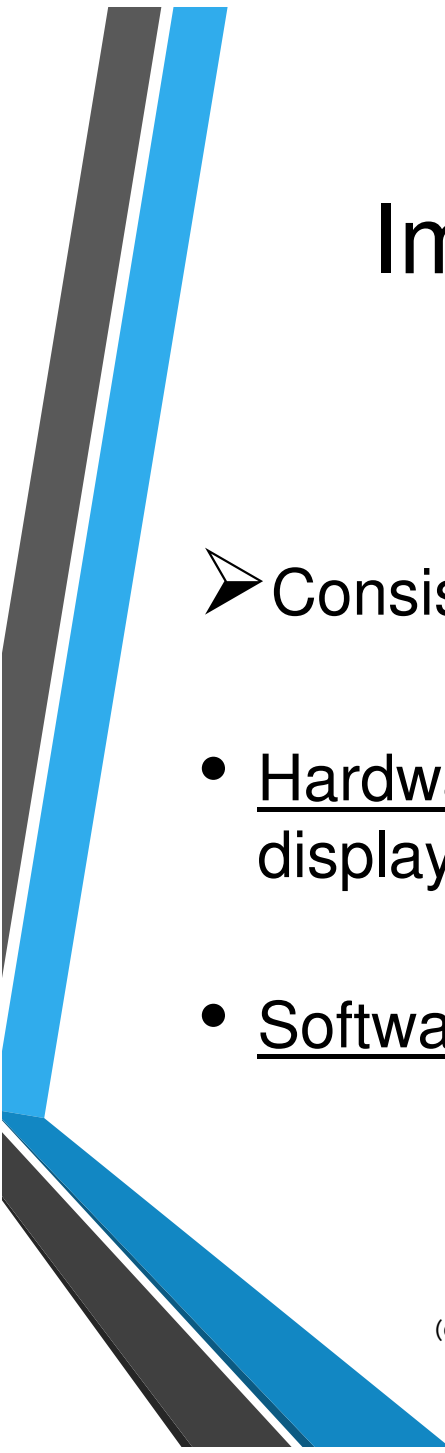


Chapter 2

Computer Imaging Systems

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Imaging Systems Overview

- Consists of two primary component types:
 - Hardware – Image acquisition system, computer, and display devices
 - Software – Image manipulation, analysis, and processing

Imaging System Hardware

Image Acquisition

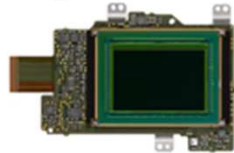
Phone



Camera



Image Sensor



Computer System



Image Display/Storage

Monitor



Printer



Phone



Flash Drive



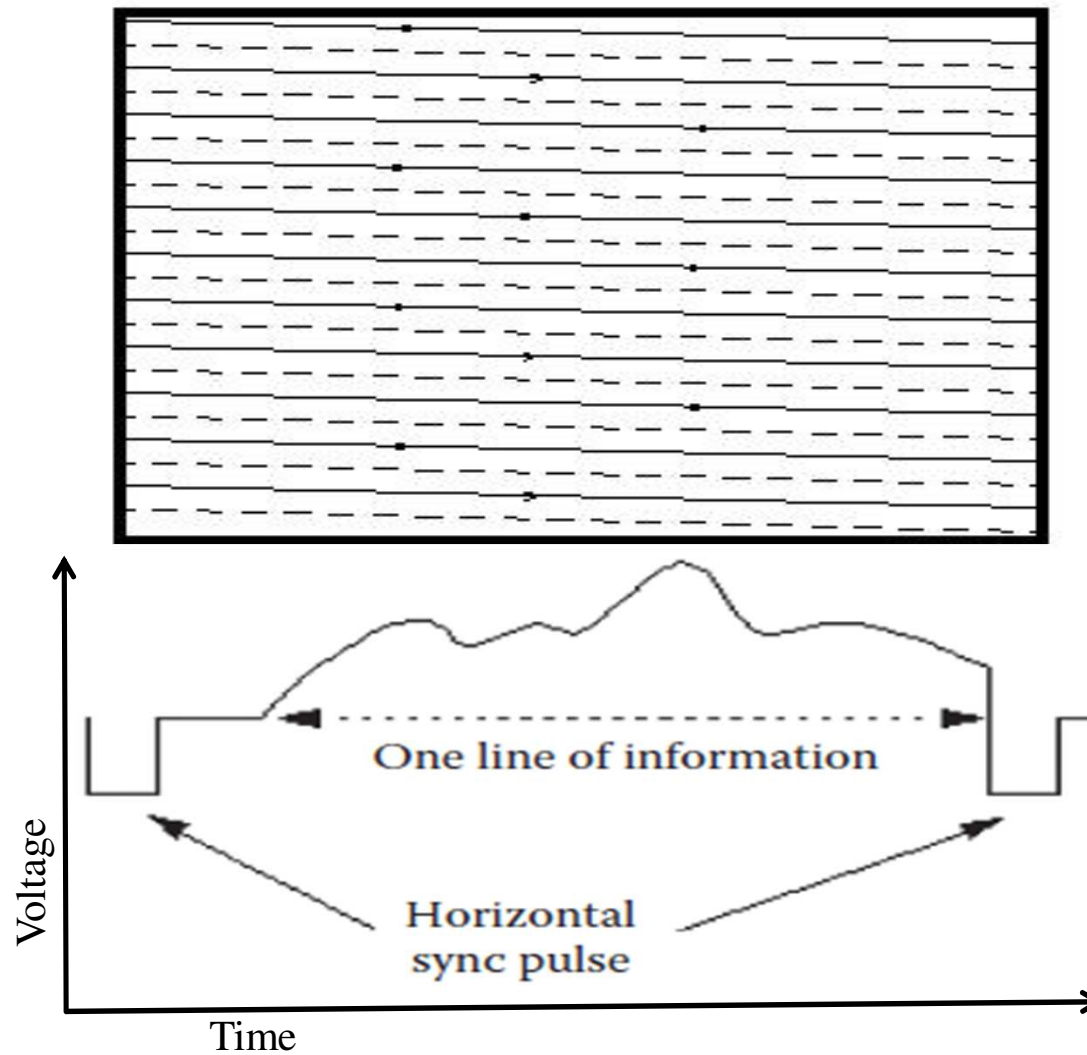
(c) Scott E Umbaugh, SIUE 2018

Digital Camera Interfaces

	10 Gigabit Ethernet (IEEE 802.3-2015)	Firewire S3200 (IEEE 1394)	USB 3.1	Camera Link
Type of standard	Public	Public	Public	Commercial
Connection Type	Point-to-point or Local Area Network (LAN)	Peer-to-peer, shared bus	Master-slave, shared bus	Point-to-point
Maximum Bandwidth for Images	~10.0 Gigabit/sec (Gbs)	~3.2 Gbs	~10 Gbs	~2.0 to 7.0 Gbs
Distance	~100 meters, no limit with switches or fiber	~4.5 meters, ~72 meters with switches, ~200 meters with fiber	~5 meters, ~30 meters with switches	~10 meters
PC Interface	Network	PCI card	PCI card	PCI frame grabber
Wireless support	Yes	No	No	No
Max # of Devices	Unlimited	63	127	1

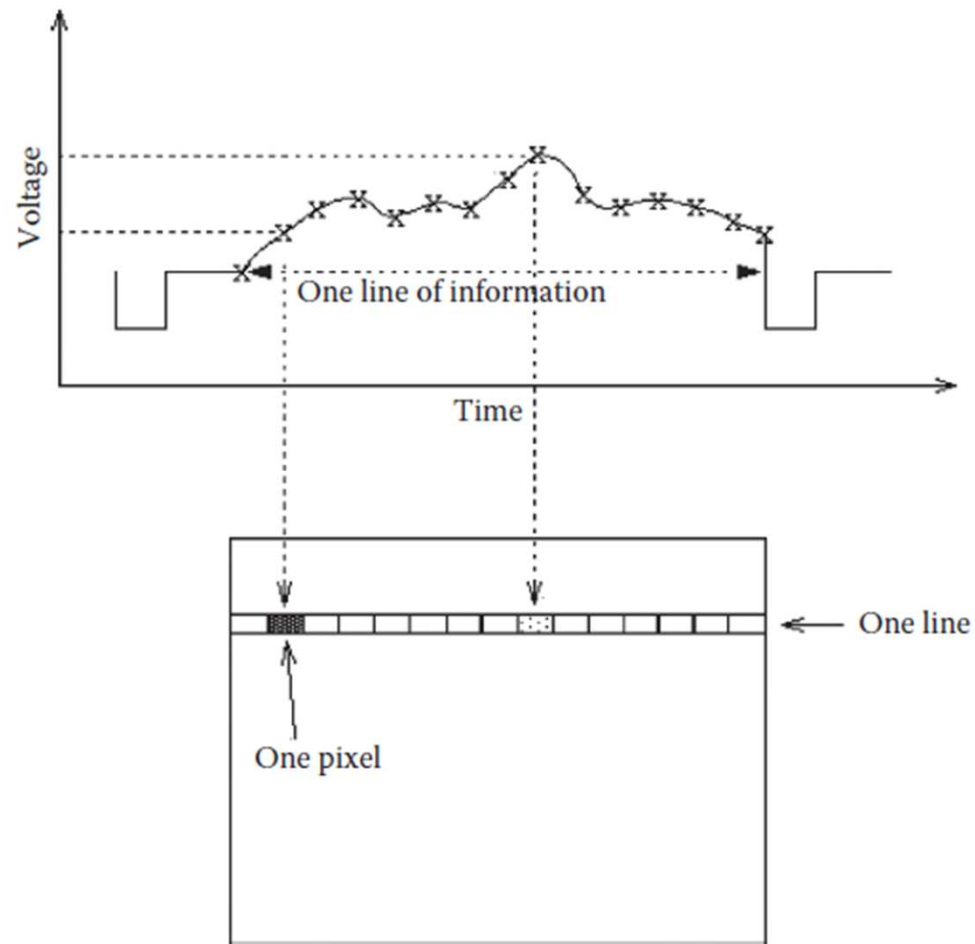
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Analog Video Signal



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Digitizing (sampling) an analog video signal



➤ Digitization: transformation of video signal into digital image



Digital Video

- Digital television (DTV) – standard definition TV (SDTV) and high definition (HDTV)
- SDTV similar to previous analog, NTSC, SECAM, PAL
- HDTV standards: 1280 columns by 720 rows (lines), in progressive scan mode, referred to as *720p*, or 1920x1080 in interlaced mode, called *1080i*
- SDTV uses a 4:3 aspect ratio, the newer HDTV standards specifies a 16:9 aspect ratio

Figure 2.1-4 Aspect Ratio. The *aspect ratio* is the ratio of the image or display width (columns) to the image or display height (rows or lines). a) The aspect ratio is 4:3 for standard definition television (SDTV), and is, b) 16:9 for high definition television (HDTV).

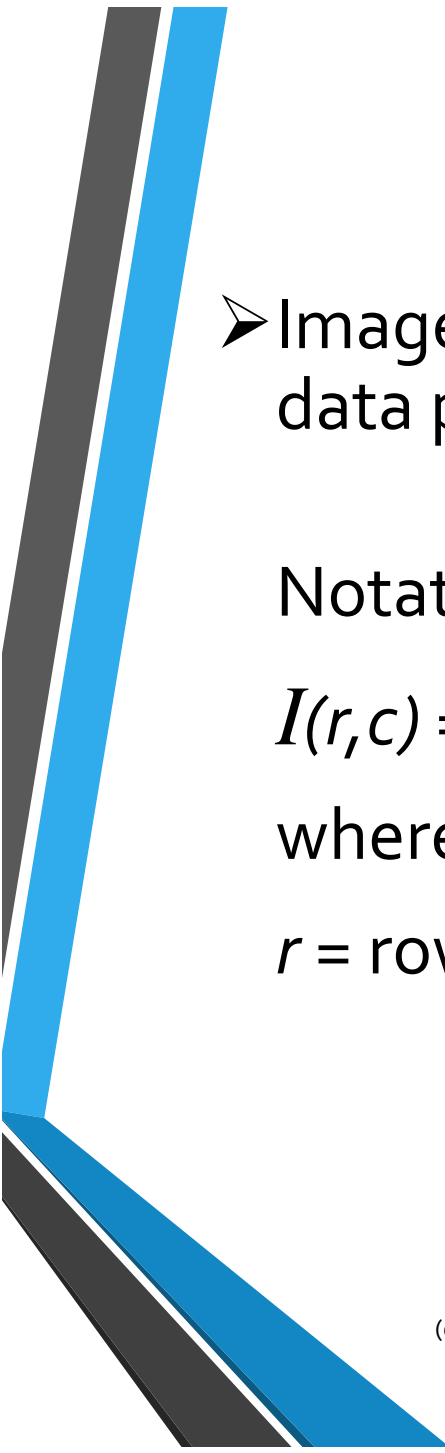


a)



b)

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- 
- Image is accessed as a 2-D array of data, where each data point is referred to as a *pixel*

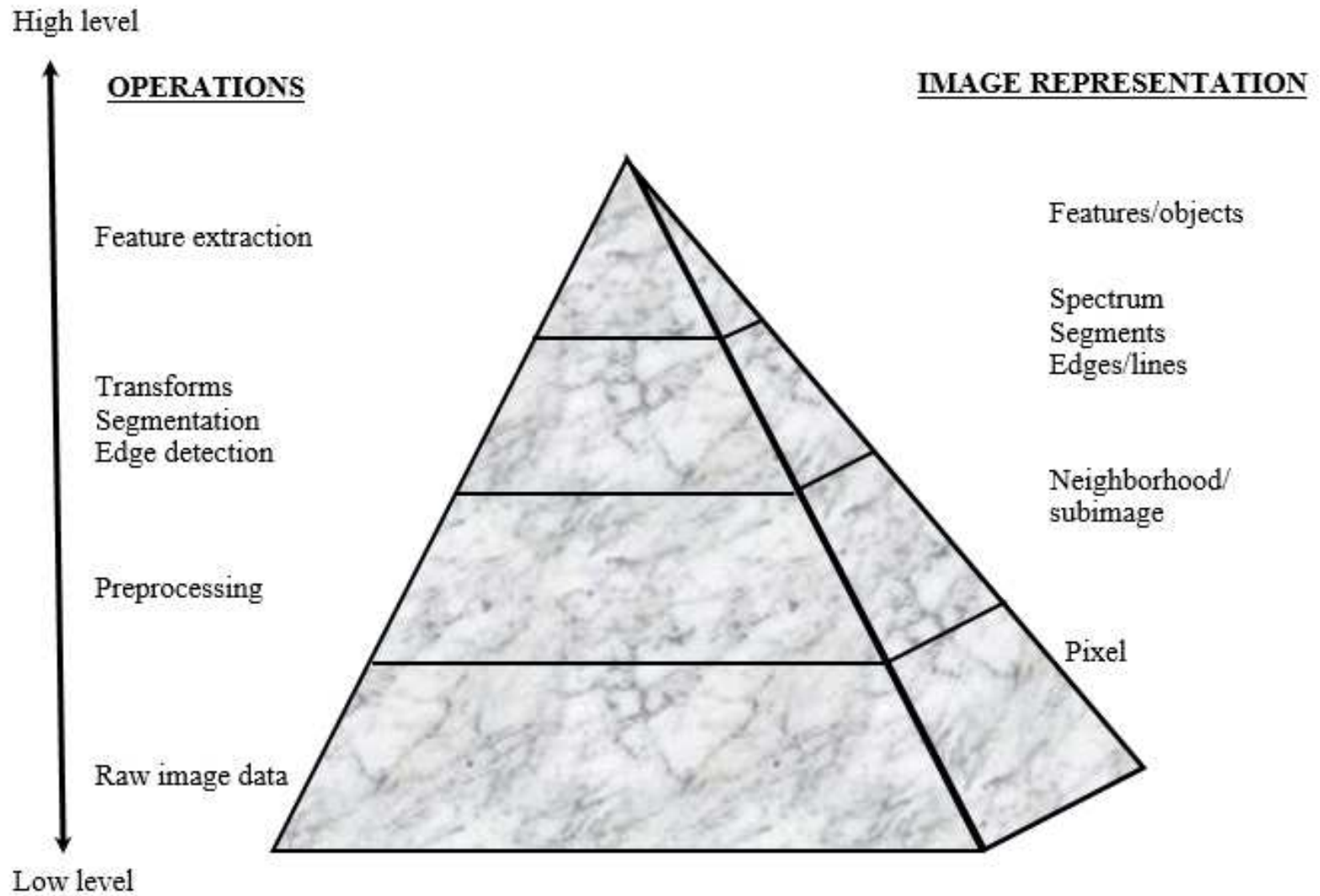
Notation:

$I(r,c)$ = Brightness of image at the pt (r,c)

where

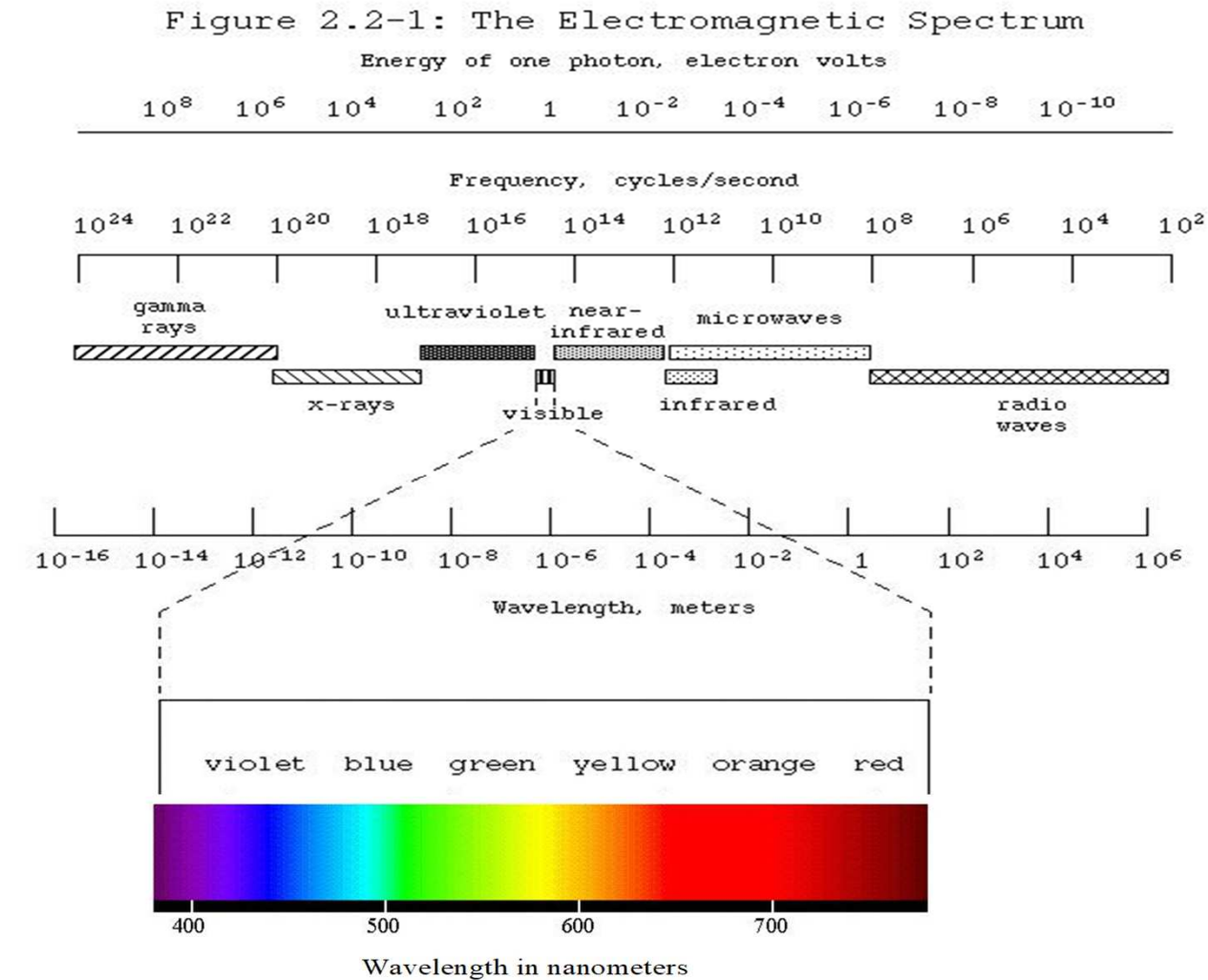
r = row, and c = column

The Hierarchical Image Pyramid



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Image Formation and Sensing



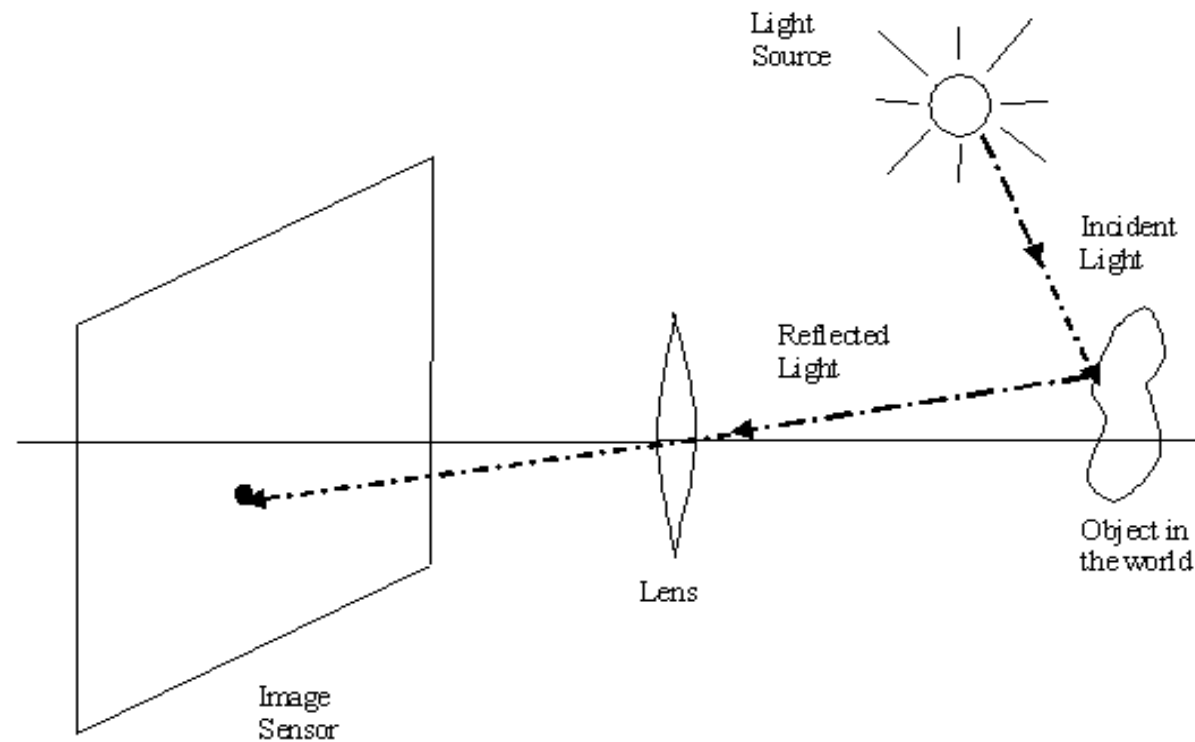
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Key components of image formation

- Where will the image point appear?
 - Determined by lenses and the physics of light, the science of *optics*
- Value, or brightness, of that point?
 - Sensor and electronic technology

Visible Light Imaging



- Reflectance function determines manner in which objects reflect light

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The Reflectance Function

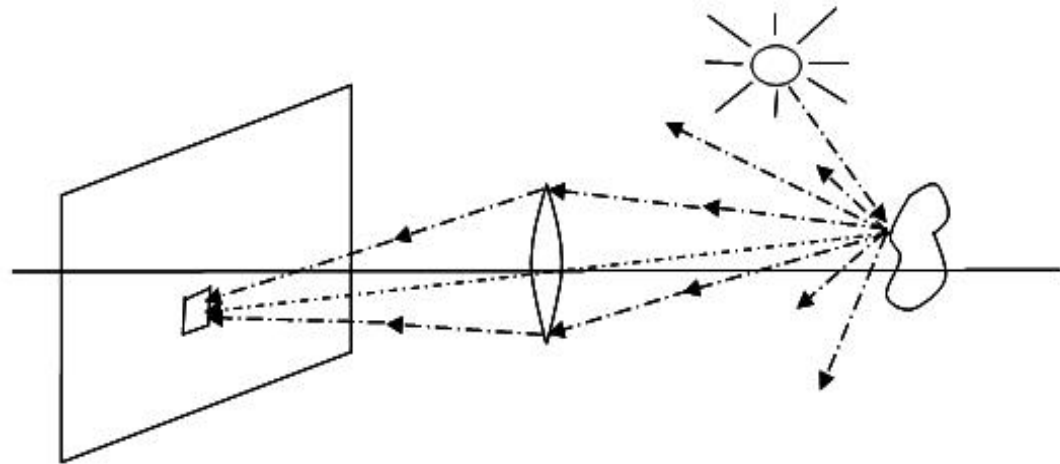


- Reflectance function determines an object's appearance
- Texture by light scattering and color by wavelengths reflected and absorbed

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- Brightness:



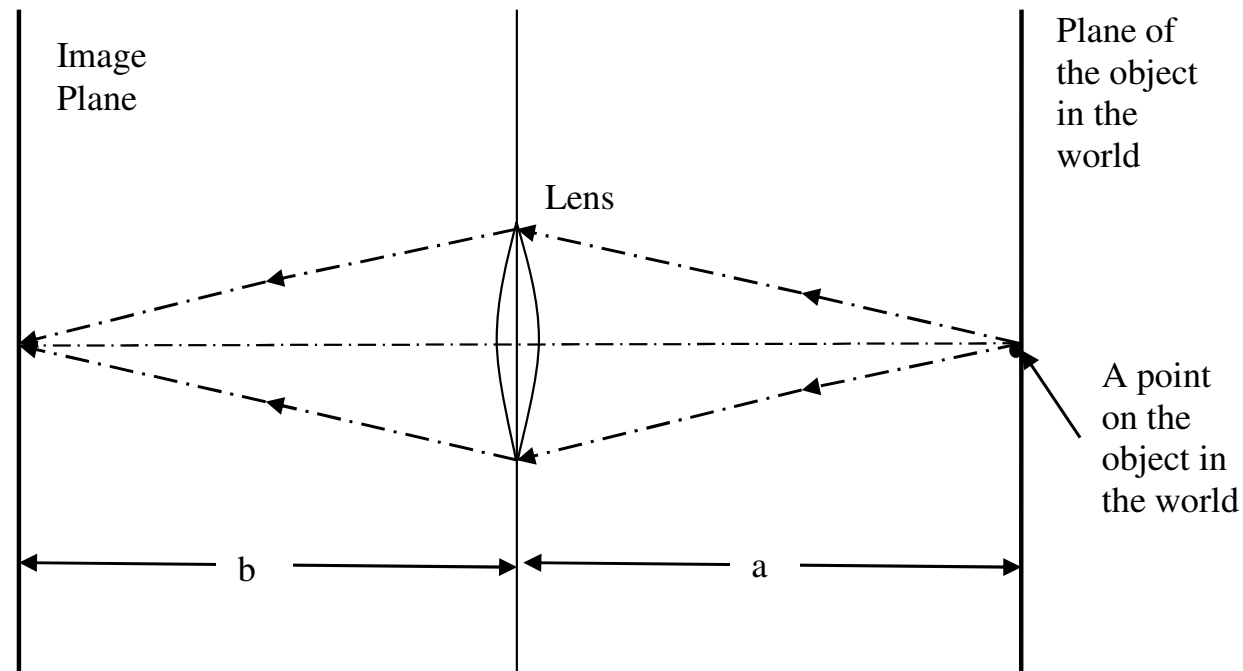
- Irradiance (Image brightness): Amount of light falling on surface, measured by a sensor

$$\text{Irradiance} = \text{Power} / \text{Area}$$

- Radiance (Scene brightness): Amount of light emitted from a surface into a unit solid angle

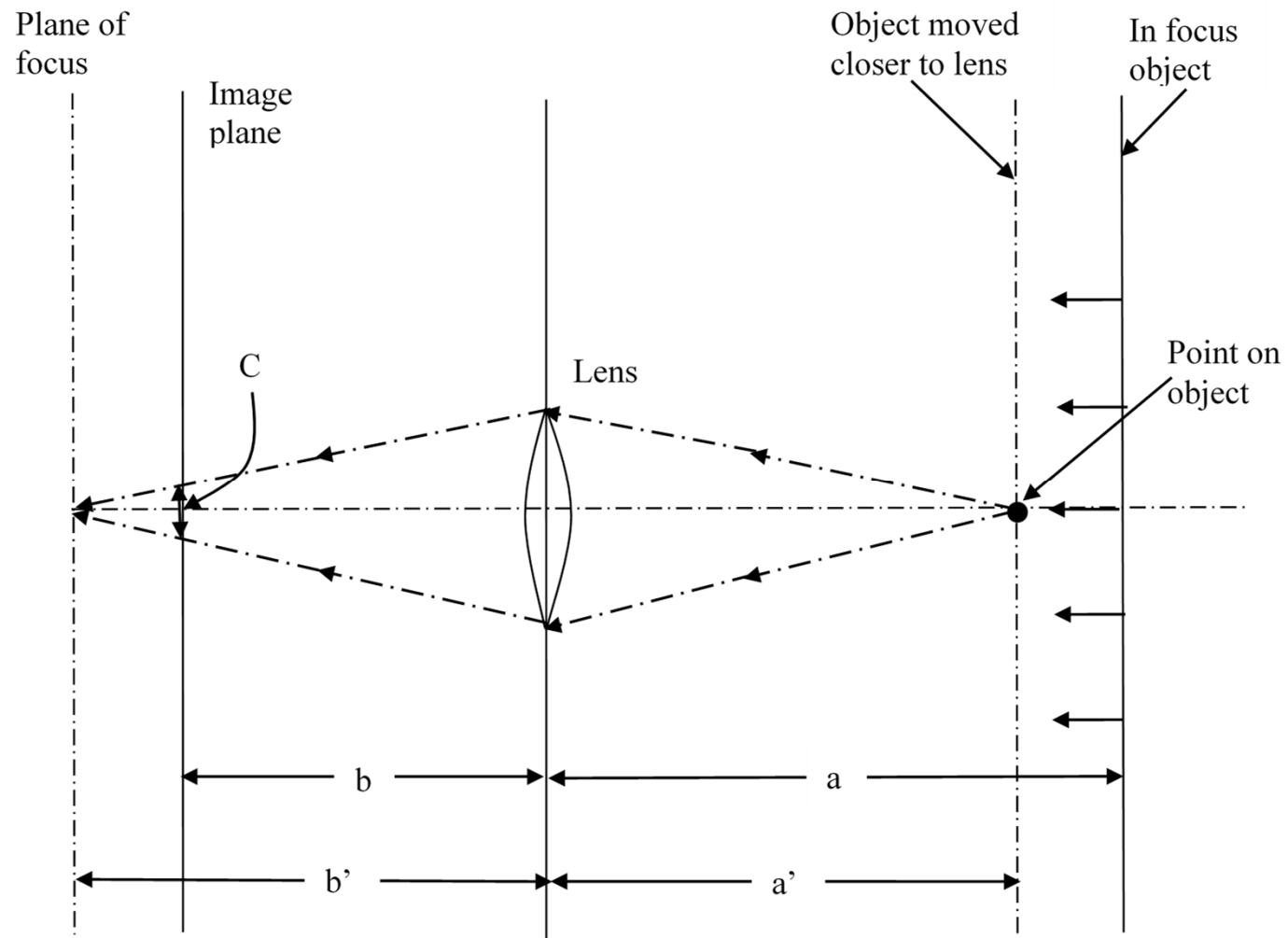
$$\text{Radiance} = \text{Power} / (\text{Area} * \text{Solid Angle})$$

- Lens equation: $1/a + 1/b = 1/f$

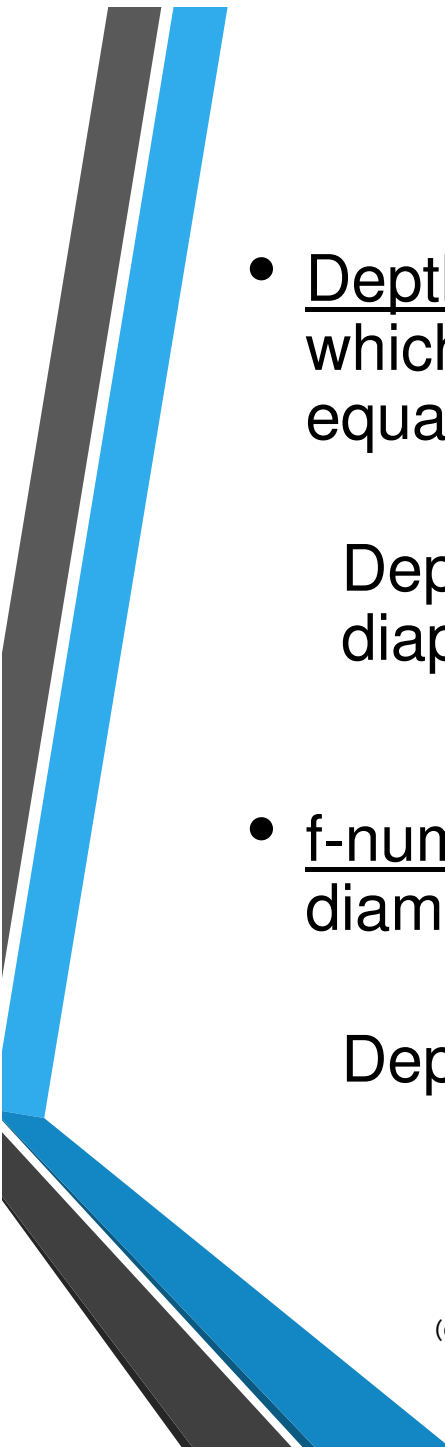


➤ f is the focal length and is an intrinsic property of the lens

- Blur equation: $c = (d/b')/b' - b/$



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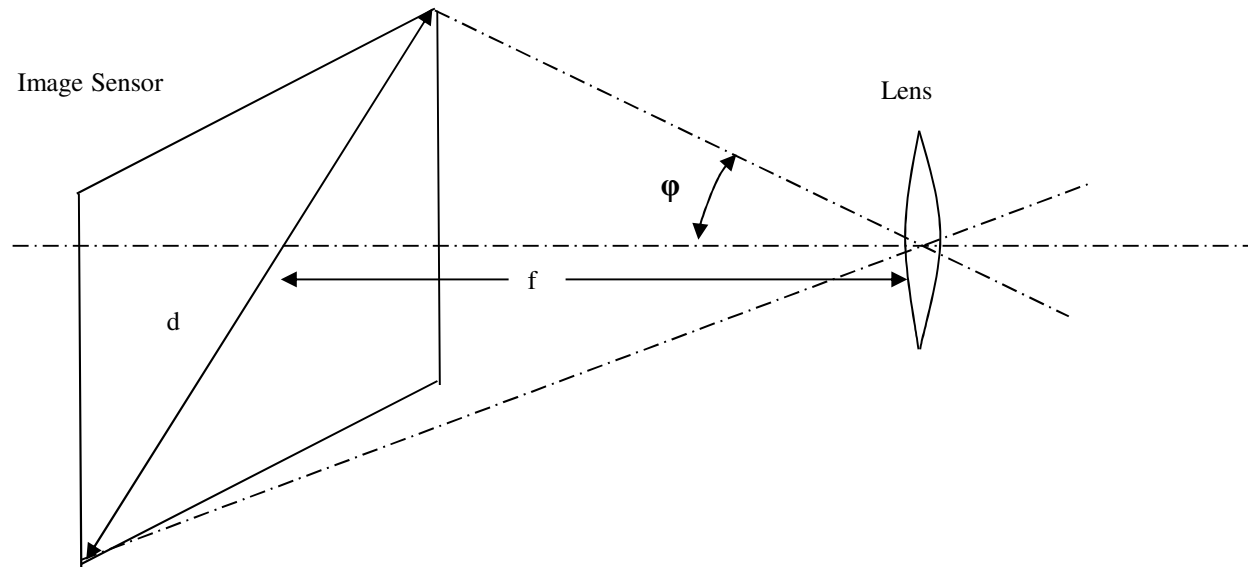
- 
- Depth of field (Depth of focus): Range of distances over which objects are focused sufficiently well (blur circle equal or smaller than device resolution)

Depth of field can be controlled by adjusting the diaphragm

- f-number (f-stop): Ratio of the focal length to the lens diameter

Depth of field is directly proportional to f-number

- Field of view (FOV) : Angle of cone of directions from which the device will create the image



$$\text{FOV} = 2\phi, \text{ where } \phi = \tan^{-1}((d/2)/f)$$

Depends upon focal length of the lens and size of image sensor

- Types of Lenses:

- Wide Angle lens: Short focal length, FOV greater than 45°

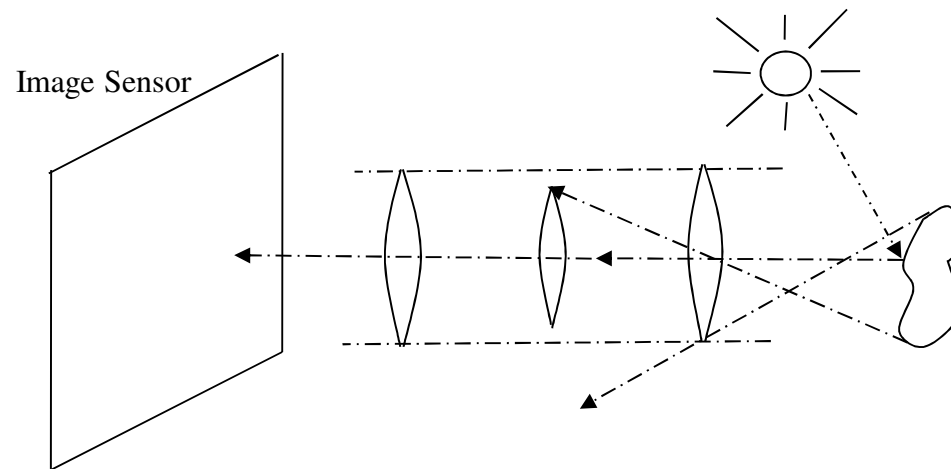
- Normal lens: Medium focal length, FOV from 25° to 45°

- Telephoto lens: Long focal length, FOV less than 25°

- Real lens consists of multiple lenses, as single lens may contain aberrations

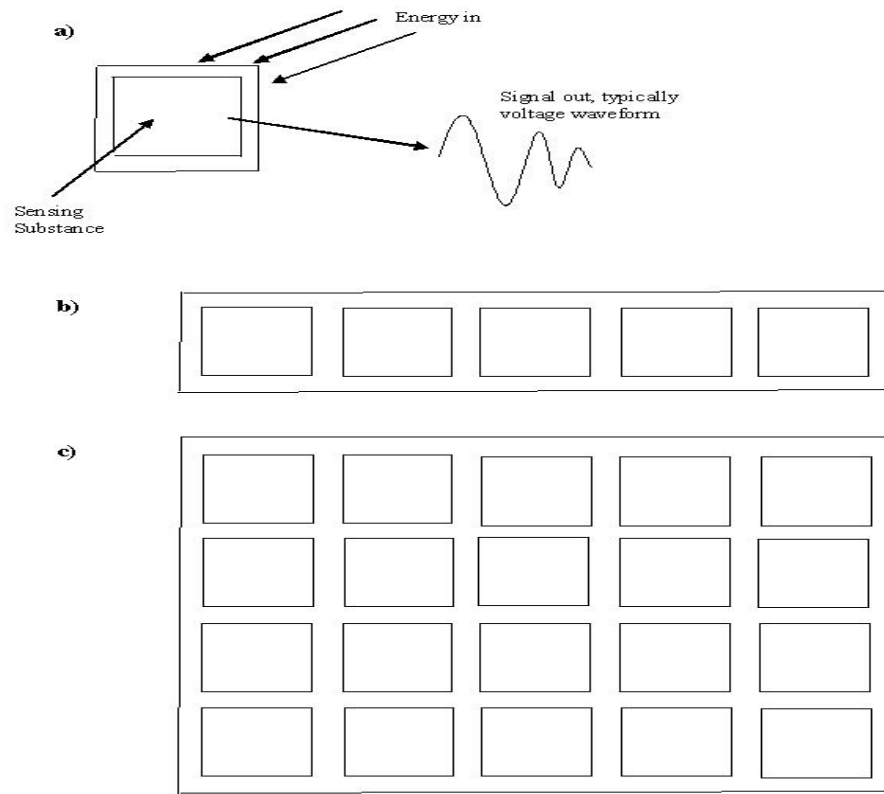
- Vignetting effect:

- Negative effects of compound lens
- Decreases the amount of energy to the image plane passing through the lens, as we move farther away from the center of the lens
- Can be avoided by using center portion of the lens



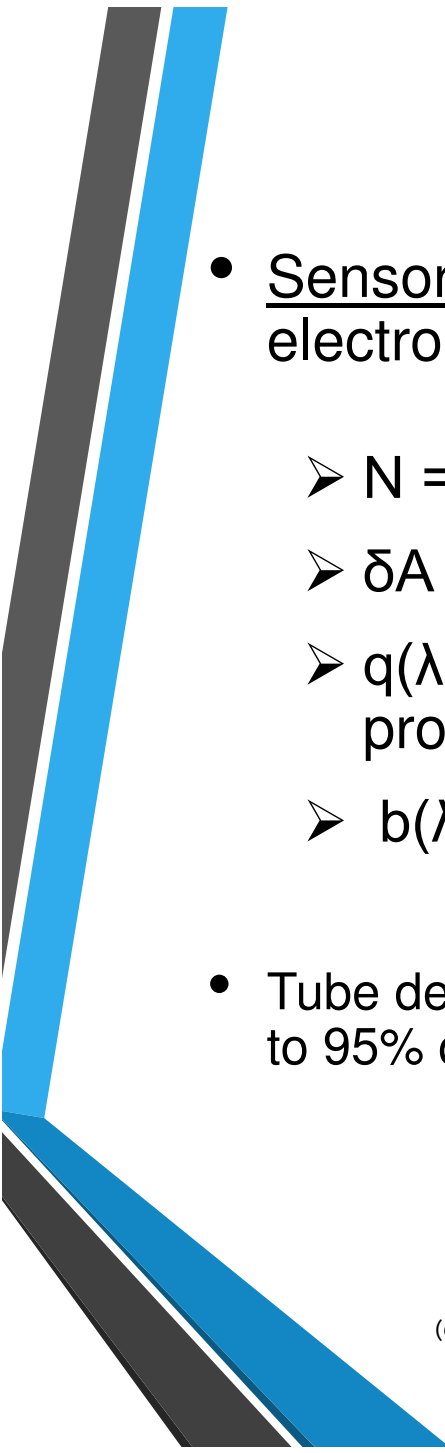
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- Sensors : Converts light energy into electrical energy



a) Single imaging sensor ; b) Linear (line) sensor ; c) 2-D or array sensor

➤ CCD: 9kx9k CMOS: less power, cheaper, image quality not as good as CCD

- 
- Sensor equation: Calculates the approximate number of electrons (N) liberated in a sensor
 - $N = \delta A \delta t \int b(\lambda) q(\lambda) d\lambda$
 - δA is the area; δt is the time interval
 - $q(\lambda)$ is the *quantum efficiency* – the ratio of electron flux produced to the incident photon flux
 - $b(\lambda)$ is incident photon flux (irradiation)
 - Tube devices are 5% quantum efficient and solid state devices are 60% to 95% quantum efficient

SMALL CAMERAS

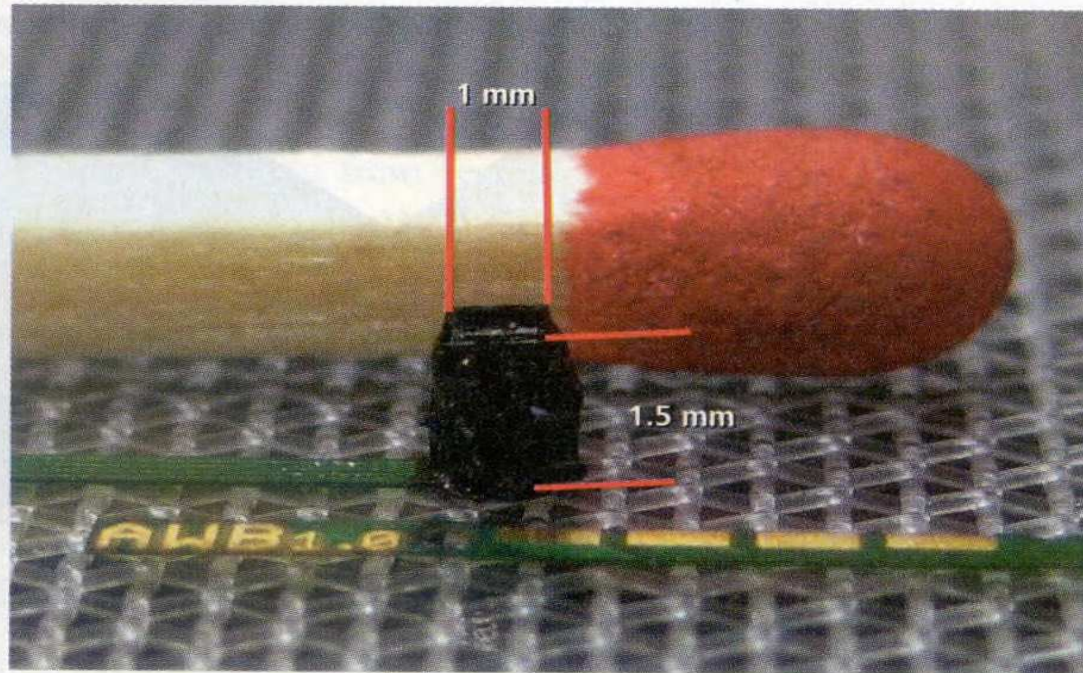


FIGURE 1. In the development of Awaiba's NanEye miniature camera, individual lenses, sensors, and readout electronics are fabricated at the wafer level and then bonded to form a single camera.

➤ Source: VISION SYSTEMS DESIGN, November 2010, "Color Camera Cubes", p. 17

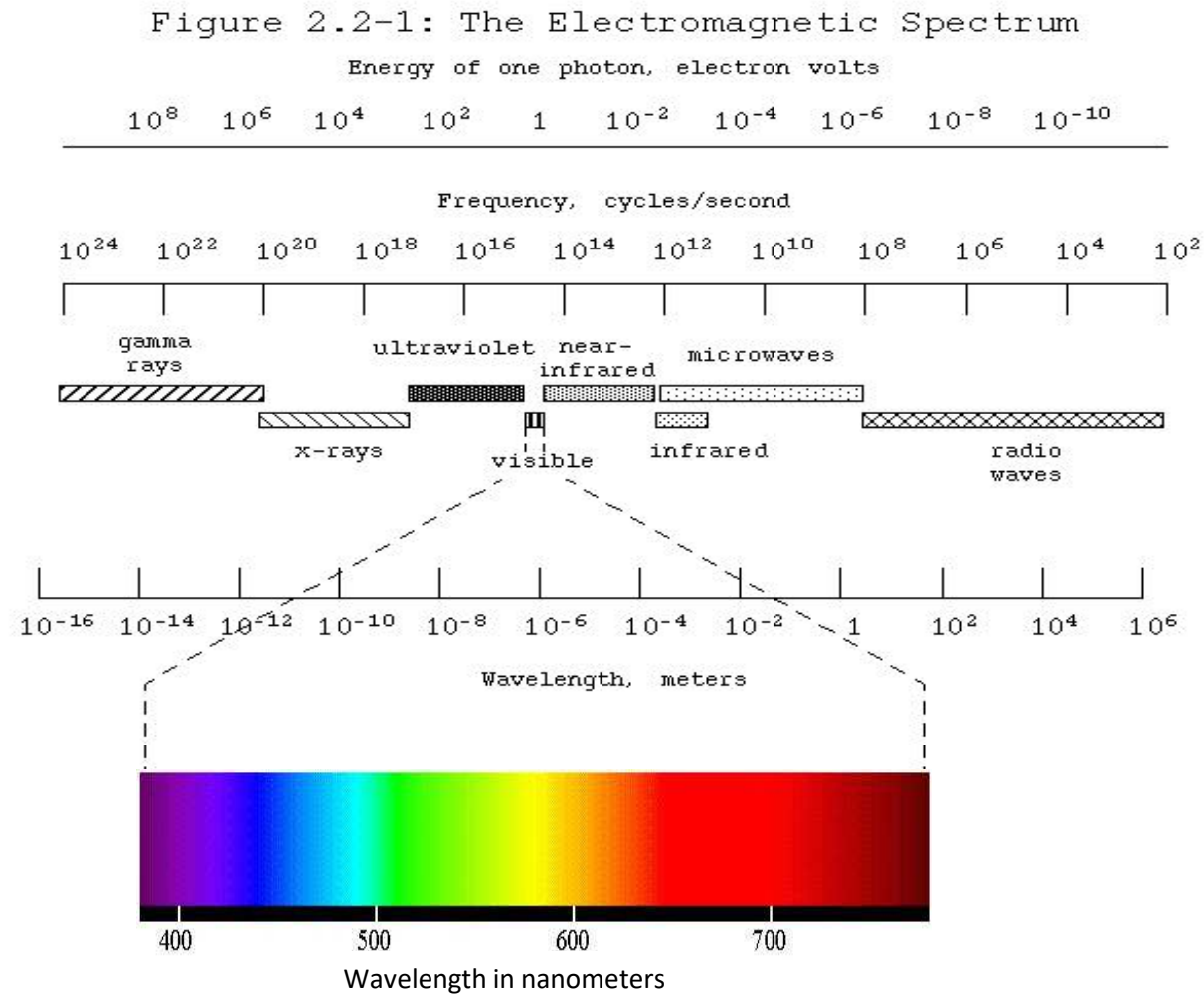
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Multispectral Sensor Chip



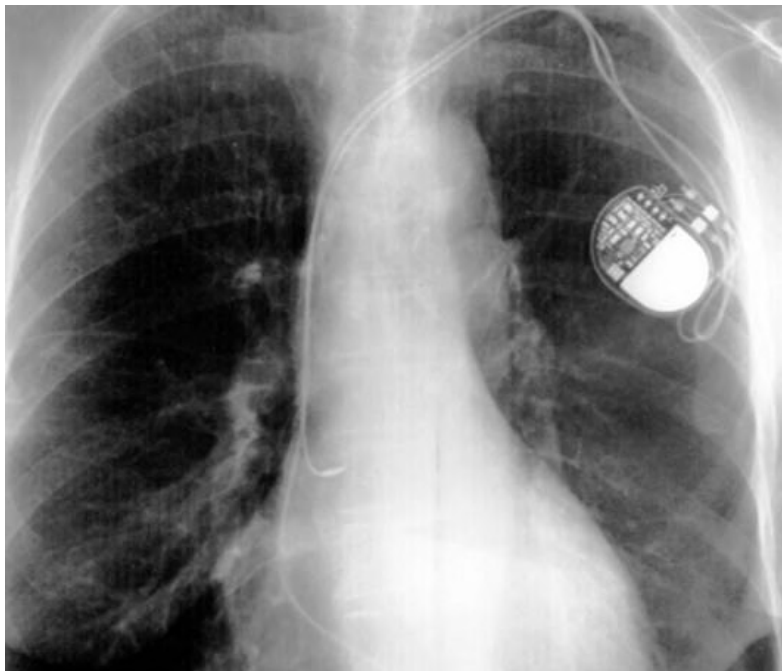
- 2.7×2.7×1.1 mm in size
- Two versions: 1) 385-900 nm, 2) 775-1065 nm
- Manufactured by Viavi Solutions
- Development kit available
- Photonics Spectra, June 2017, p. 36

Imaging Outside the Visible Range of the EM Spectrum



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- X-Rays: Used in medical diagnostics and computerized tomography (CT)



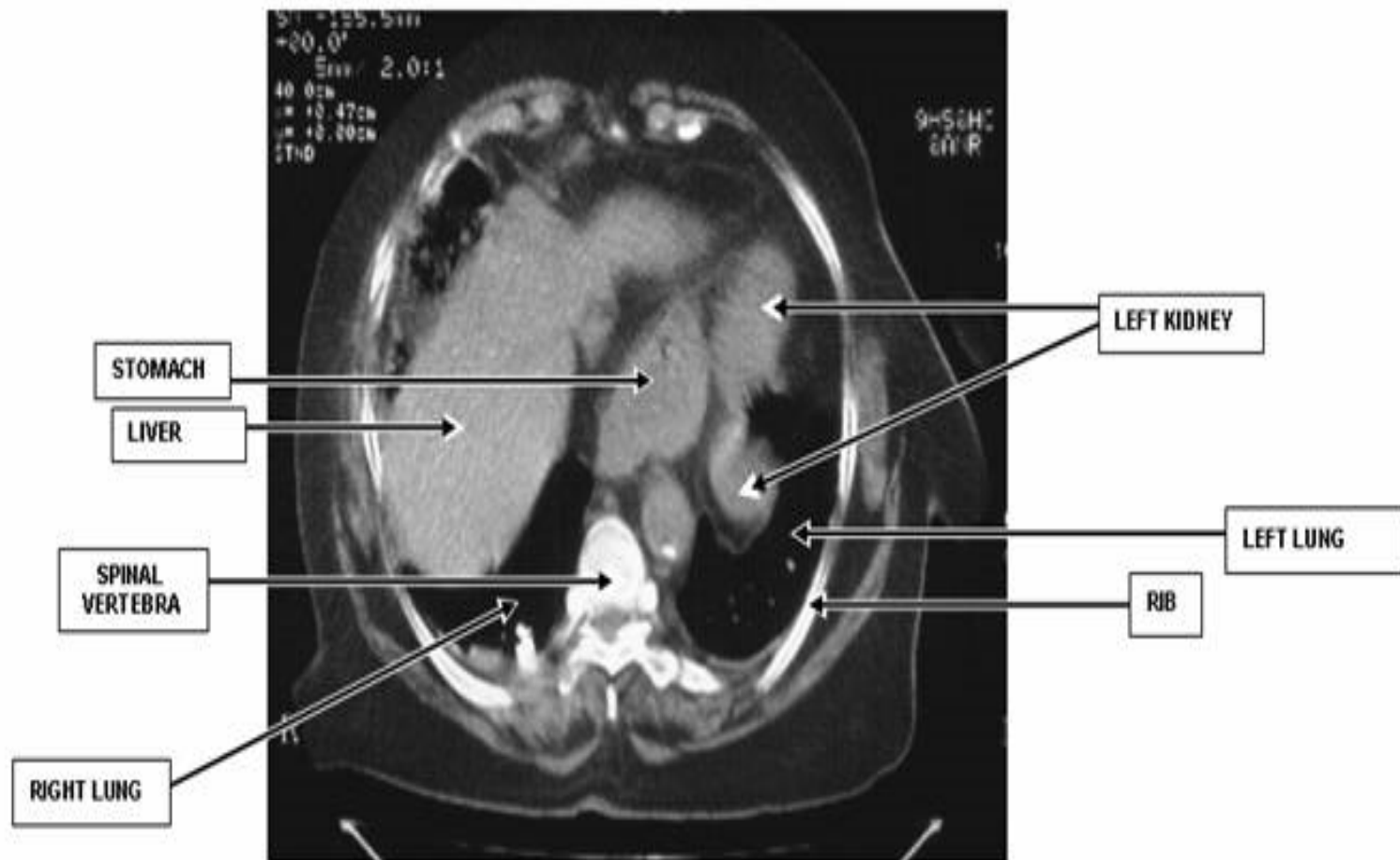
Chest X-ray



Dental X-ray

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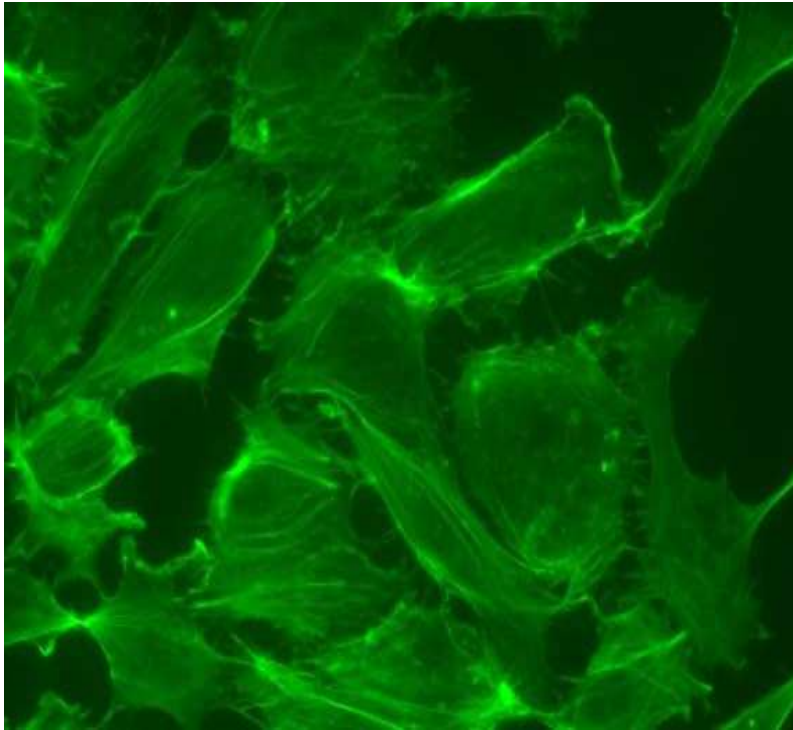
➤ Computerized Tomography



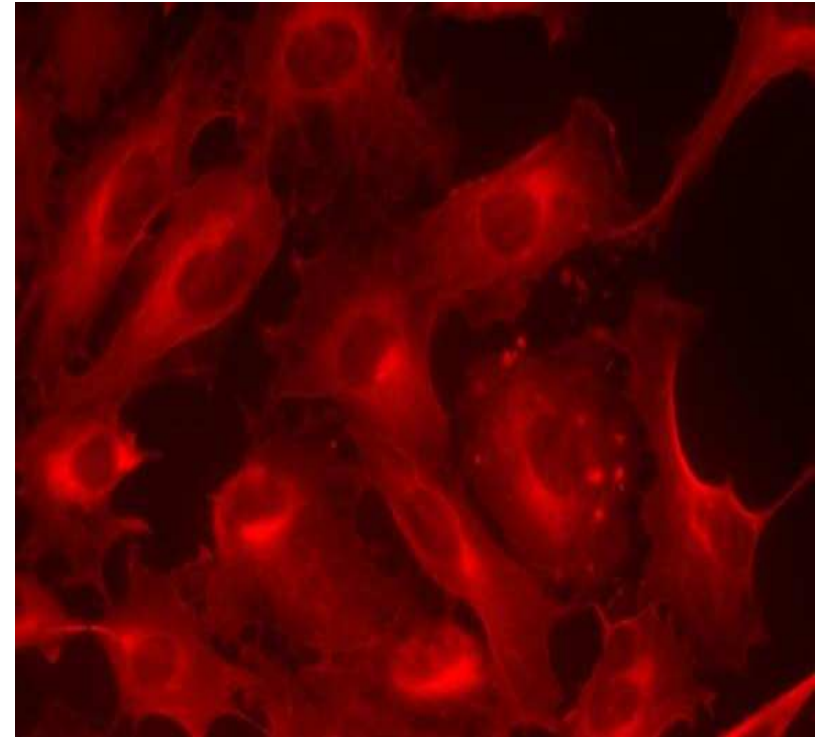
One slice of CT of patient's abdomen

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- Ultraviolet imaging (300nm): Used in industrial applications, law enforcement, microscopy and astronomy



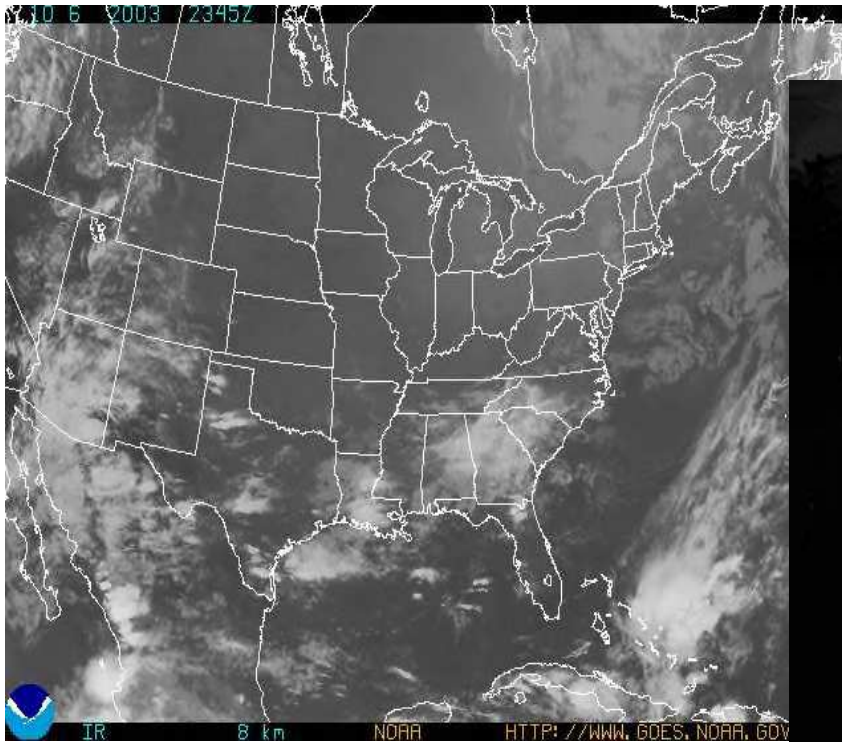
Fluorescence microscopy of cells



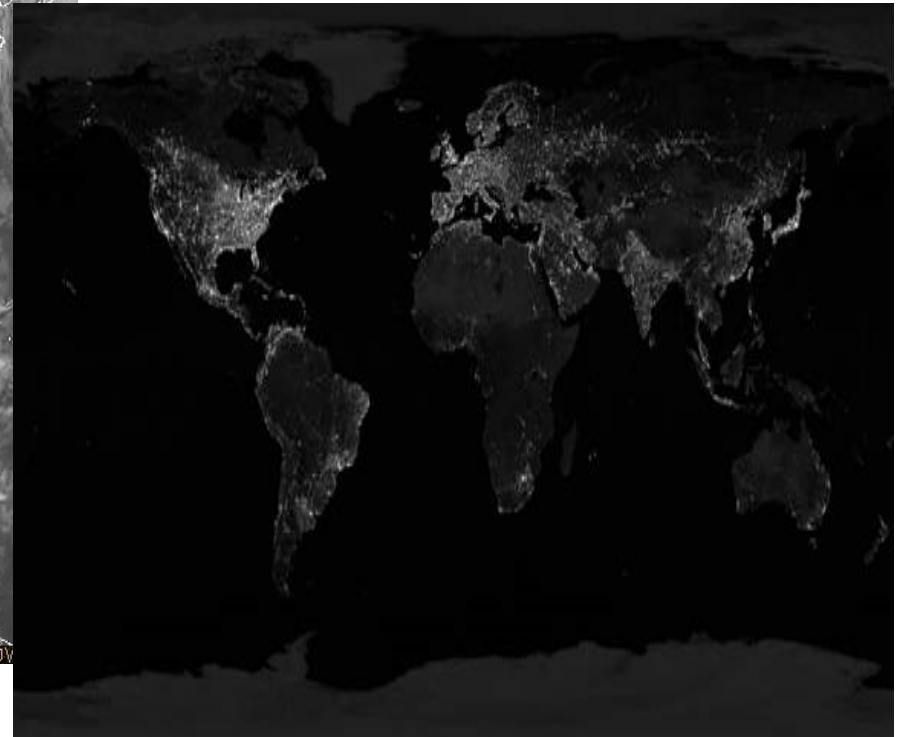
Fluorescence microscopy of cells

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- Infrared imaging (800nm+): Used in satellite imaging, law enforcement, medical diagnosis and fire detection

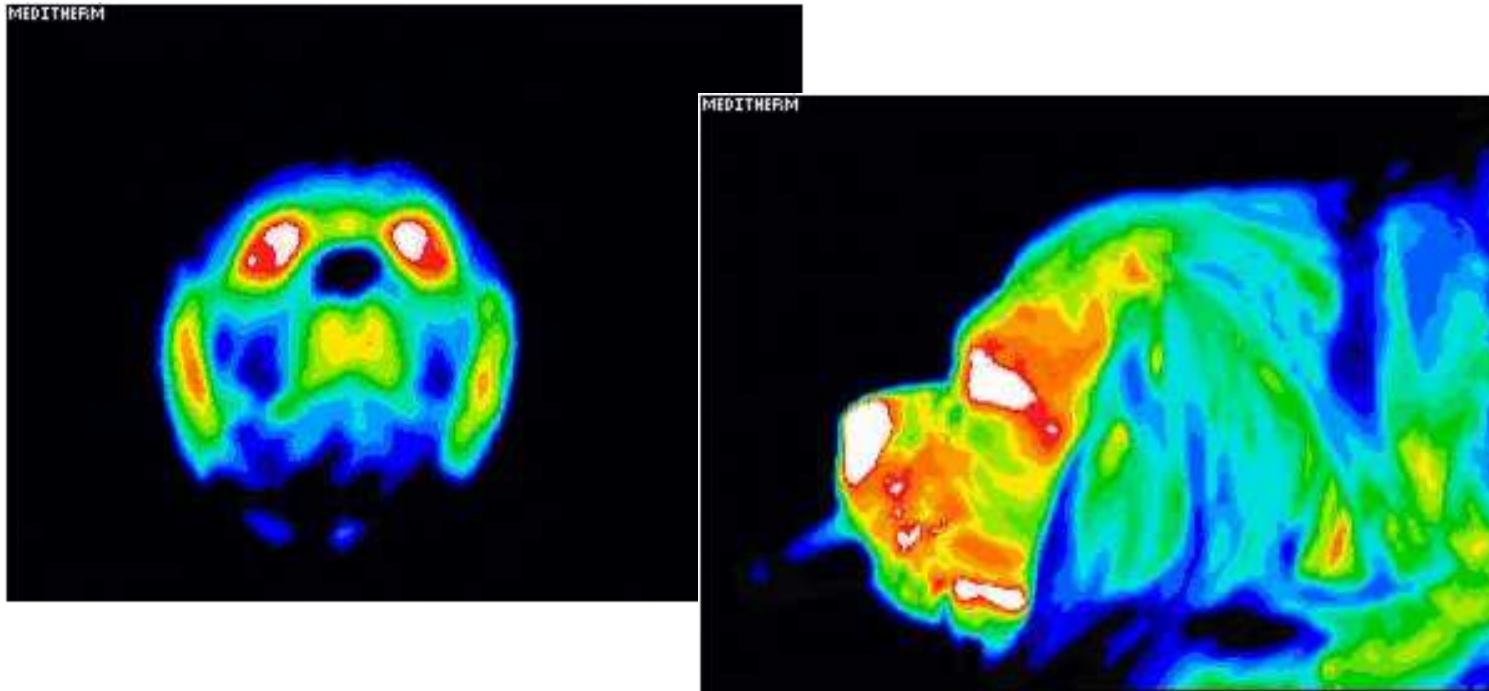


Satellite image showing
water vapor



Infrared satellite imagery in the
near infrared band

- Infrared imaging (800nm+): Used in satellite imaging, law enforcement, medical diagnosis and fire detection

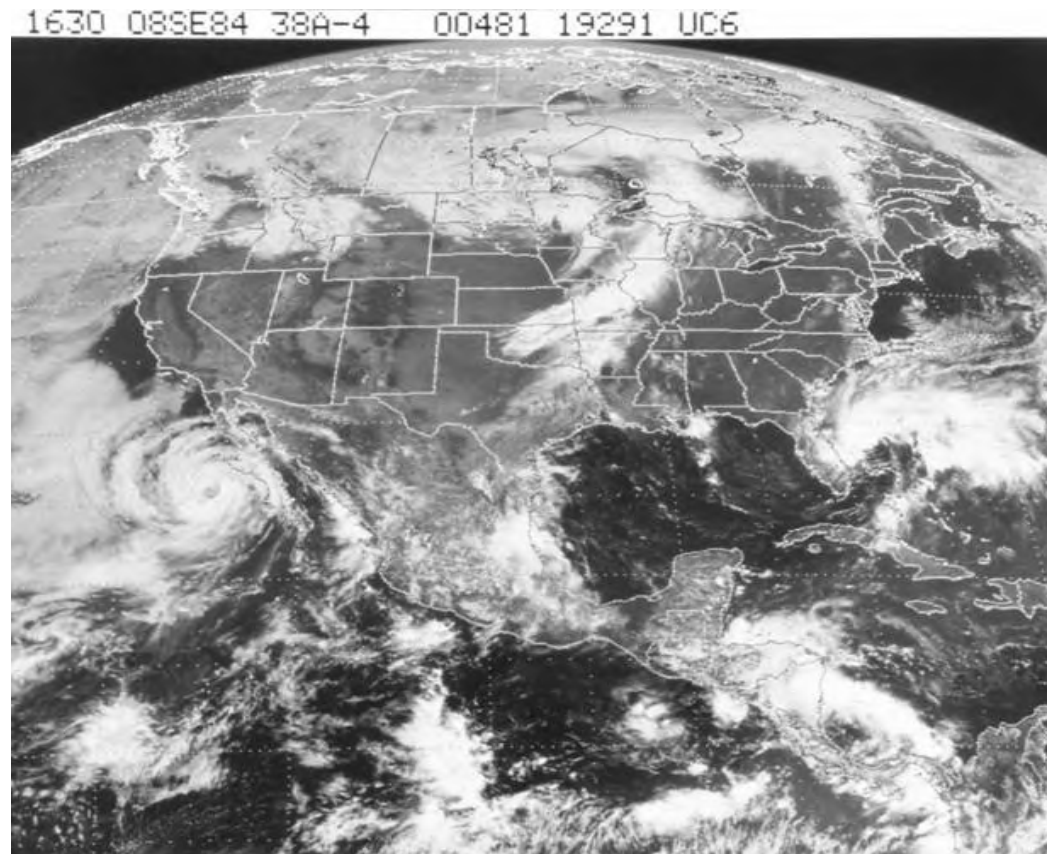


Thermographic images used in research for the diagnosis of Chiari malformation, a brain disease, in dogs

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➤ Multispectral imaging: Used in weather analysis



GOES image of North America
(Multispectral Geostationary Operational Environment Satellite)

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- Microwave images: Used in radar applications, to acquire info through obstacles in any light conditions
- Radio waves: Used in astronomy and medicine (MRI)

MRI of patient's shoulder



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Acoustic Imaging

- Works by sending out sound waves at various frequencies and then measuring the reflected waves
- Used in biological and man-made systems, geological systems, and medicine



Conventional ultrasound



3-D Ultrasound

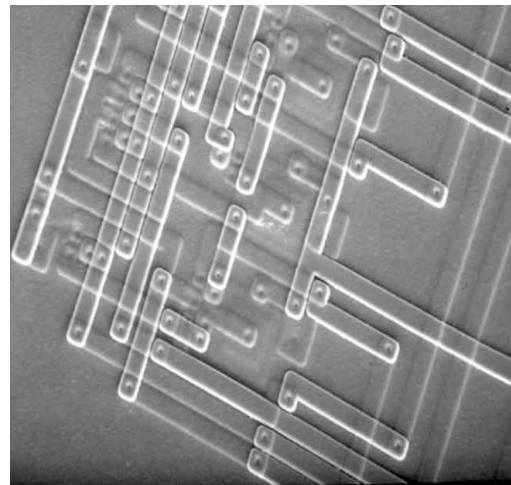
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Electron Imaging

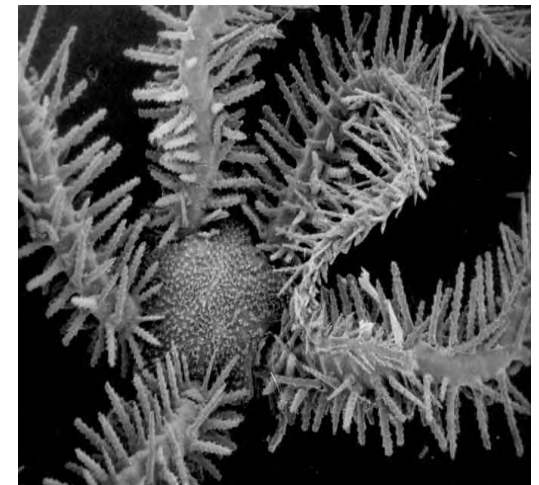
- Uses a focused beam of electrons
- Provides high magnification (200 thousand times)
- Two types: SEM (scan) and TEM (xmit)



SEM image of mosquito

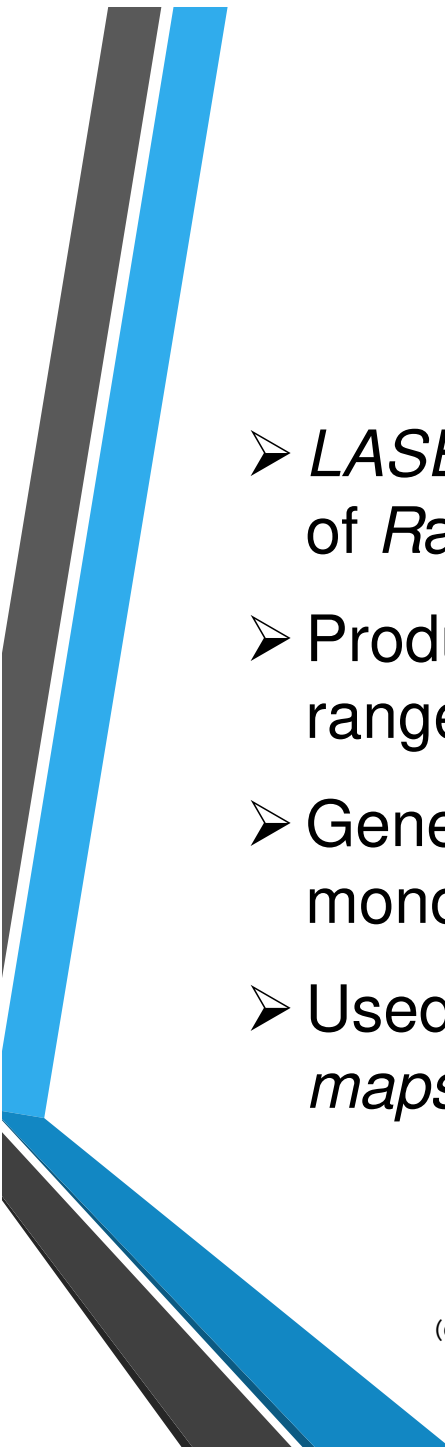


Logic gate in microchip



Brittlestar

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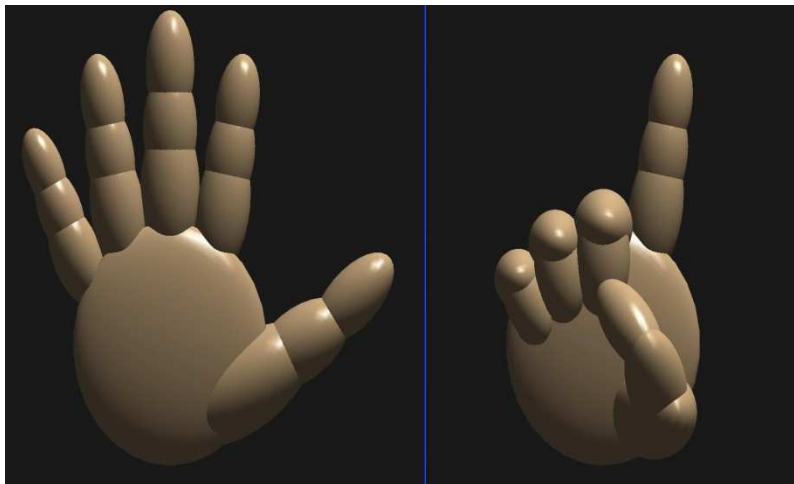


Laser Imaging

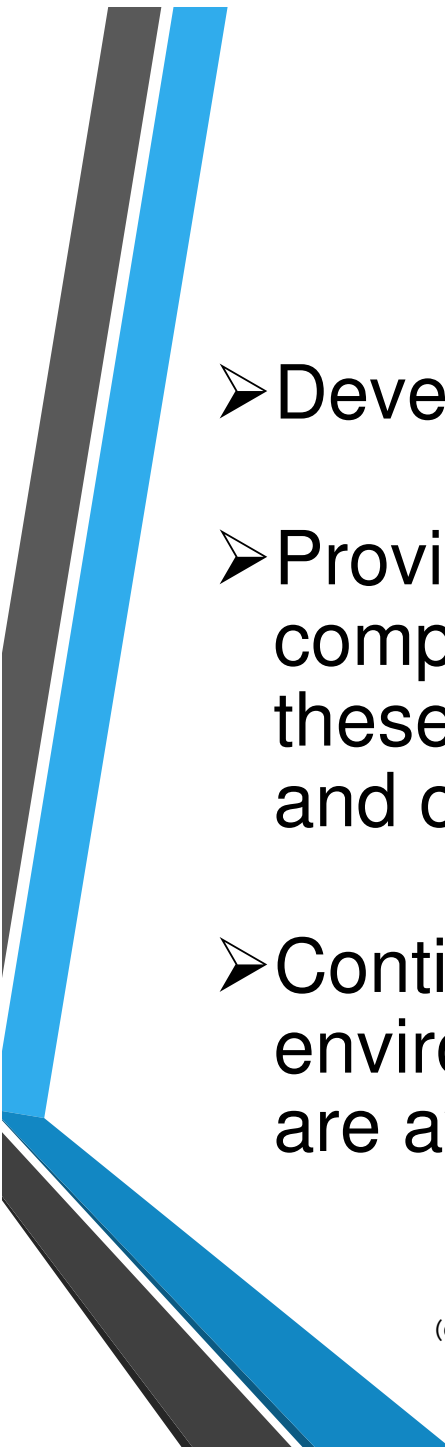
- *LASER* = Light Amplification by Stimulated Emission of Radiation
- Produces narrow beam of light in visible, IR, or UV range of EM spectrum
- Generates coherent light, highly intense and monochromatic
- Used to create *range images*, referred to as *depth maps*

Computer Generated Images

- Computers are used to generate images, they are not *sensed* from the real world
- Used in engineering (CAD), medicine, education, arts, games, aviation



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The CVIPtools Software

- Developed at SIUE
- Provides the user access to a wide variety of computer imaging operations and to explore these operations by varying all the parameters and observing the results in real time
- Continually under development in the university environment, so that newly developed algorithms are available for exploration and research



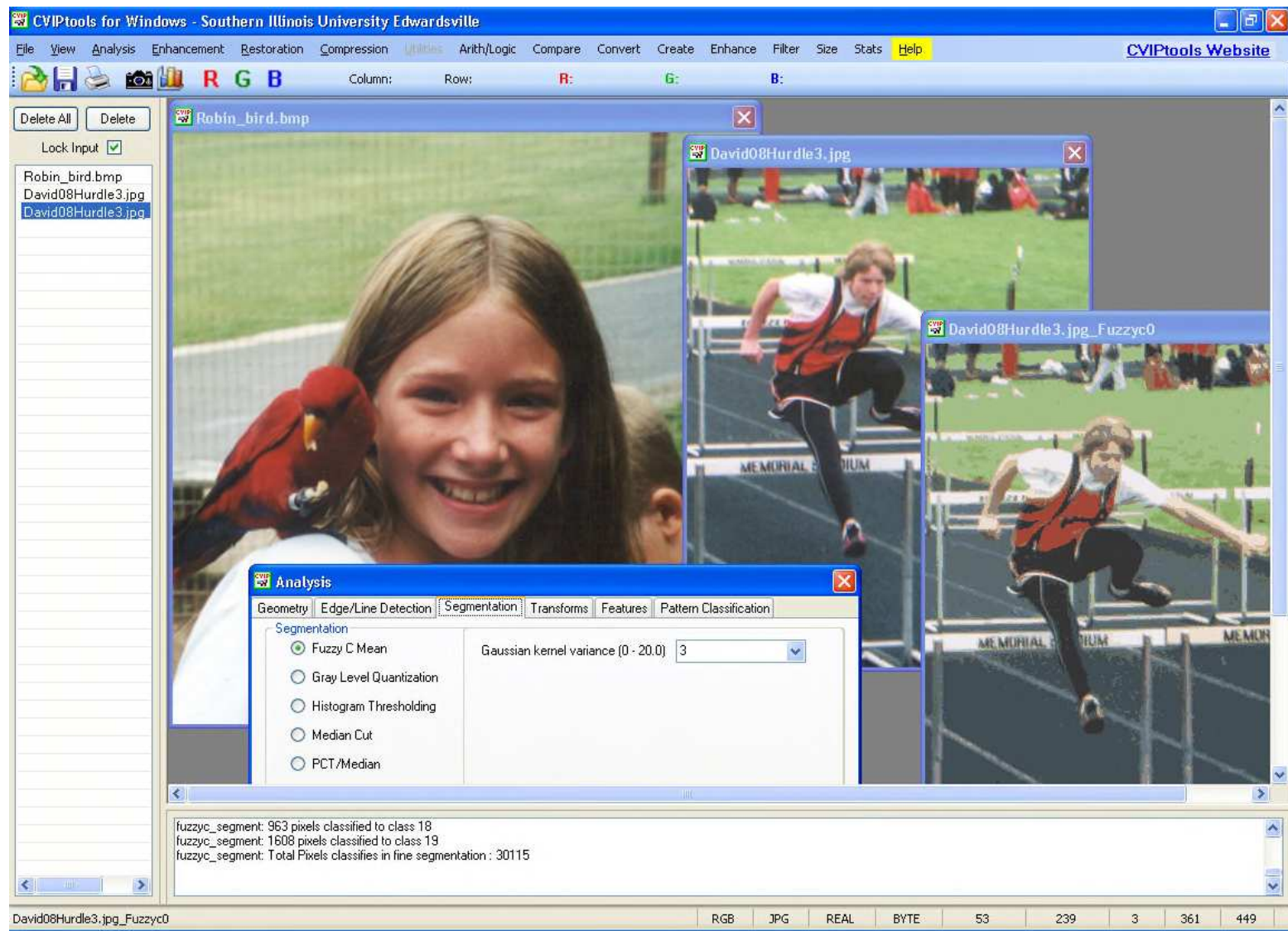
Image Viewer

- Loading an image requires clicking on the standard file open icon in the upper left of the main window
- The image is read into the memory and its name appears in the image queue and is displayed in the main window
- Image information shown in the status bar at the bottom of the main window



Image Viewer

- The loaded image is the active image, which can be changed at anytime either by clicking on the image name in the queue or the image itself
- The image viewer allows the user to perform standard image geometry as well as image enhancement operations via histogram equalization
- These operations affect only the image that is displayed, and not the images in the CVIPtools image queue



Main Window with images in queue

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Viewer Commands

DRAW, MARK, SELECT	Shift key-drag left mouse button	Select rectangular area of image, used in crop, etc
	Control key-drag left mouse button	Select irregular shaped area of image, used in <i>Utilities->Create->Border Mask and Border Image and crop, etc</i>
	Control key-click left mouse button	Select <i>Original Image for Analysis->Features</i>
	Control-A	Select entire image for copy/paste
	Control-C	If image has area currently selected, copy area to clipboard – this is used for copying images into documents Else, if image has current mesh (from <i>Restoration->Geometric Transforms</i>), copy mesh to clipboard
	Control-V	If mesh (from <i>Restoration->Geometric Transforms</i>) is available on clipboard, paste mesh to image
	Alt key-click left mouse button	Mark mesh points for <i>Restoration->Geometric Transforms</i> for <i>Enter a new mesh file</i> ; select <i>Segmented Image for Analysis->Features</i> ; select <i>Second Image for the Utility->Arith/Logic</i> operations; select Green band image for <i>Utility->Create->Assemble Bands</i>
	Shift key-click left mouse button	Select Blue band image for <i>Utility->Create->Assemble Bands</i>
	Alt key-click left mouse button drag	After a mesh is entered in <i>Restoration->Geometric Transforms</i> , this will allow the user to move mesh points
	Right mouse button on image	Mesh display select box (followed by left button to select) Copy/Paste current mesh
	Middle mouse button on image	Removes drawn boxes and borders

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Viewer Commands (cont')

ROTATE	t	turn 90 degrees clockwise
	T	Turn 90 degrees counter-clockwise
FLIP	h H	horizontal flip
	v V	vertical flip
OTHERS	N	Change back to original image, including size
	n	Change back to original image, without changing size
	q Q	Quit – removes image from display but leaves in queue (clicking on the X in the upper right corner will remove the image from queue)
	e E	Histogram equalization
	Right mouse button in image viewing area (workspace)	Brings up <i>Utilities</i> menu

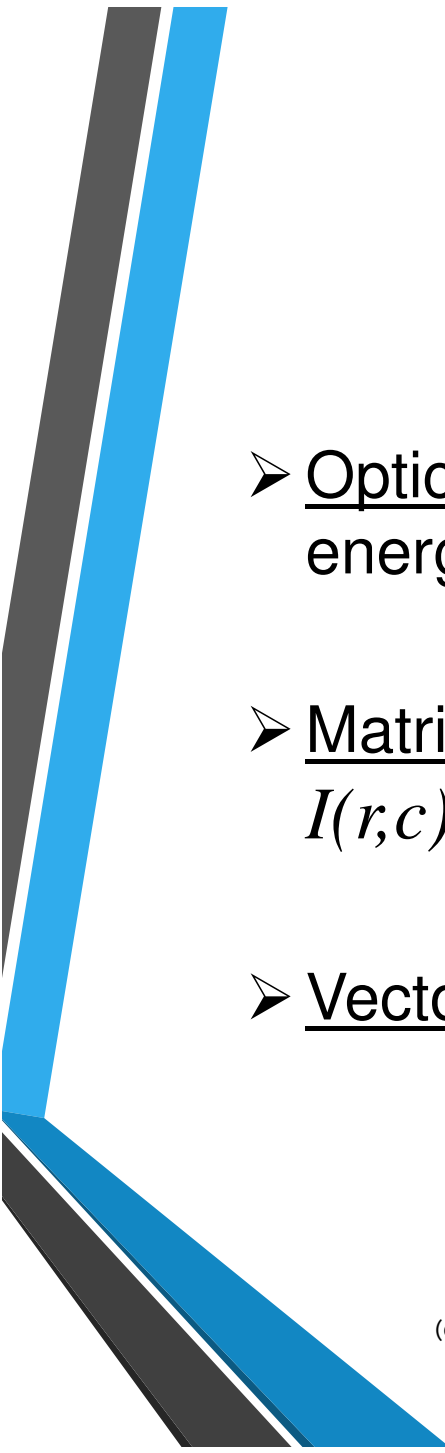


Image Representation

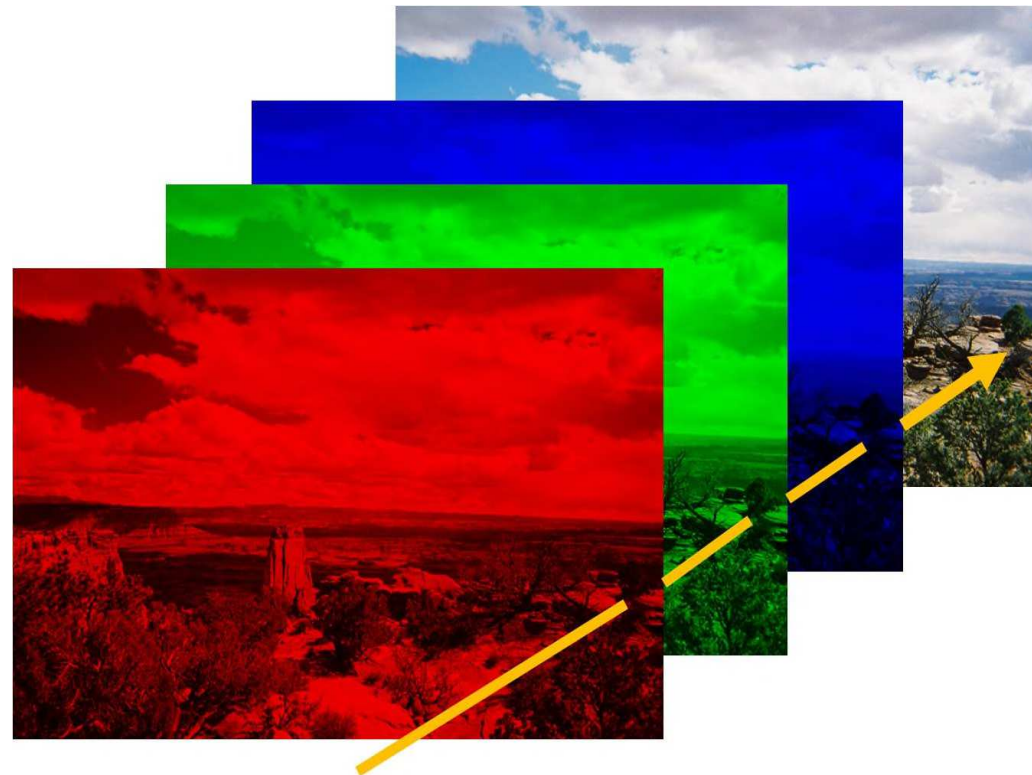
- Optical image: Collection of spatially distributed light energy measured by an image sensor to generate $I(r,c)$
- Matrix: 2-D array corresponding to the image model, $I(r,c)$
- Vector: One row or column in a matrix



Image Types

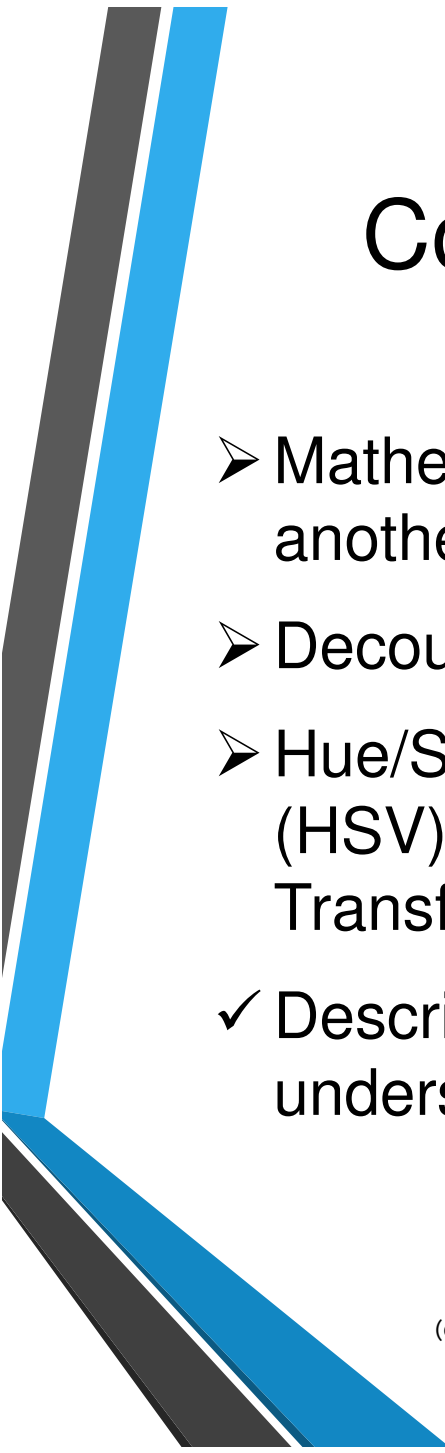
- Binary images: Simplest type of images, which can take two values, typically black or white, or “0” or “1”
- Gray scale images: One-color or monochrome images that contain only brightness information and no color information
- Color images: 3 band monochrome images, where each band corresponds to a different color, typically red, green and blue or RGB

Color pixel vector: Single pixel's values for a color image, (R,G,B)



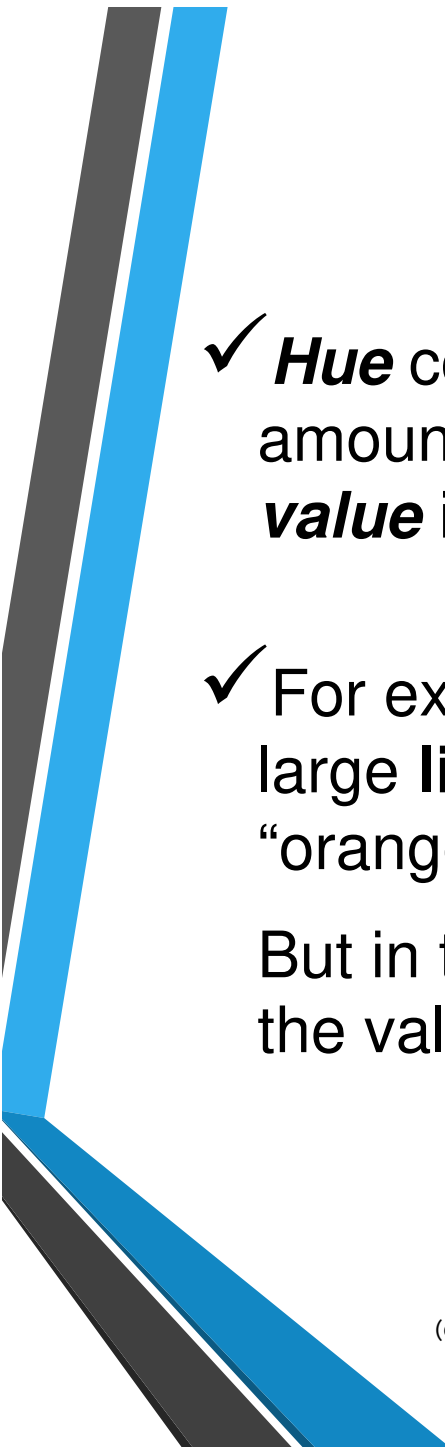
- Multispectral Images: Images of many bands, which may contain information outside of the visible spectrum

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Color Transform/Color Model

- Mathematical model or algorithm to map RGB data into another color space
- Decouples brightness and color information
- Hue/Saturation/Lightness (HSL), Hue/Saturation/Value (HSV) and Hue/Saturation/Intensity (HSI) Color Transforms:
- ✓ Describes colors in terms that we can more readily understand

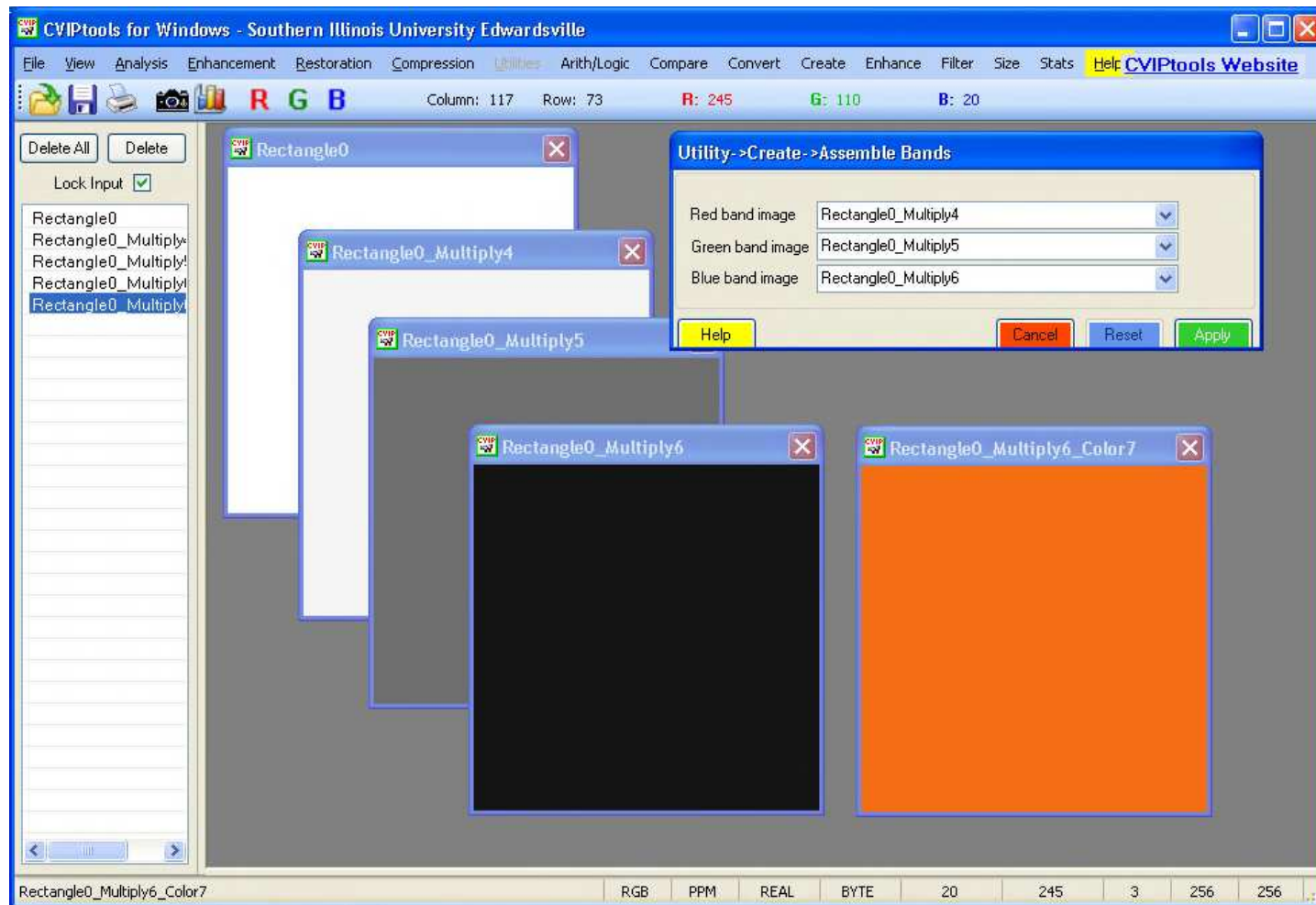


✓ **Hue** corresponds to color, **saturation** corresponds to the amount of white in color, and **lightness, intensity** or **value** is the brightness

✓ For example: a **deep, bright orange** color would have a large **lightness/intensity/value** (bright), a **hue** of “orange”, and a high value of **saturation** (“deep”)

But in terms of RGB components, this color would have the values as R=245, G=110, and B=20

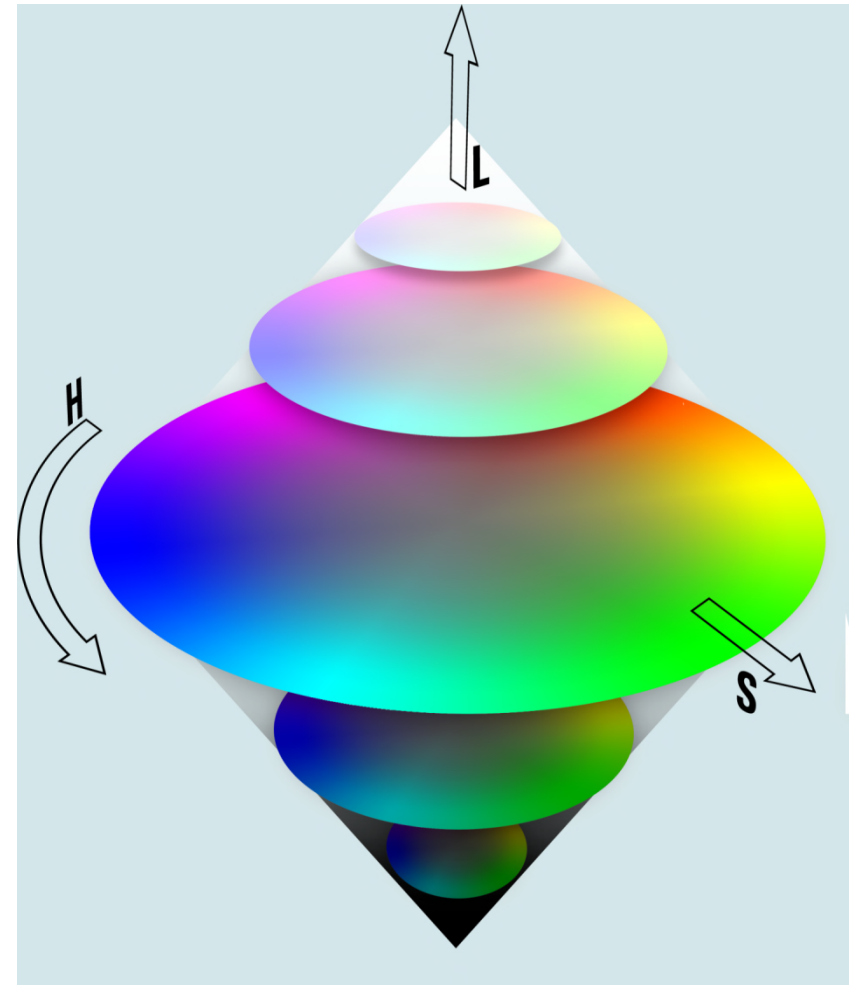
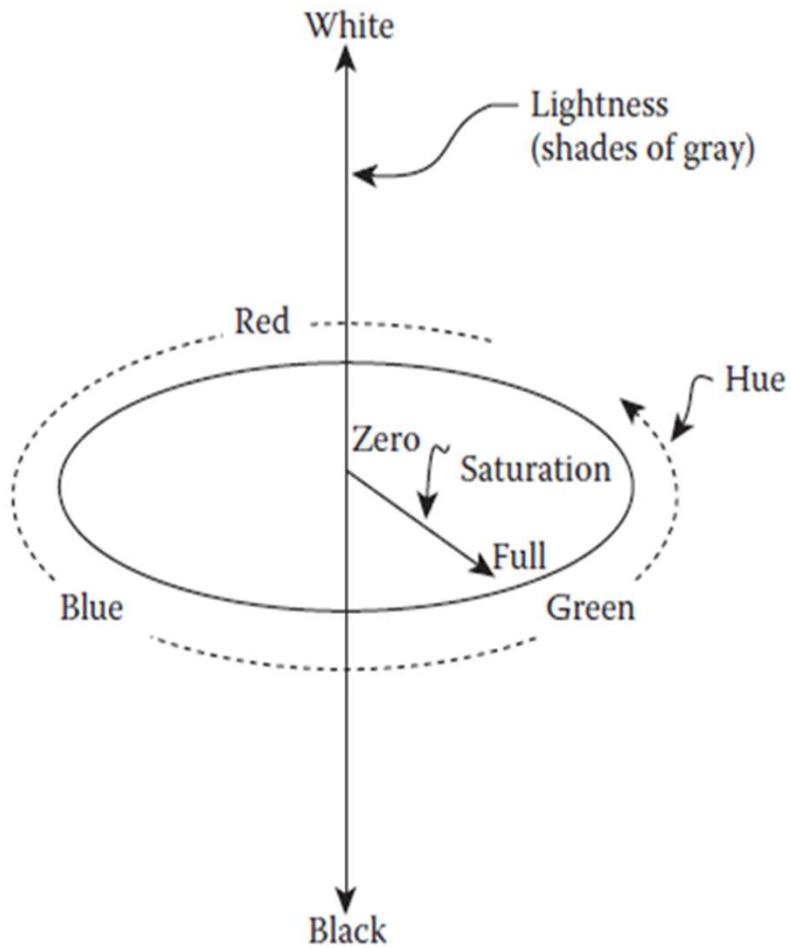
Creation of Orange Image in CVIPtools



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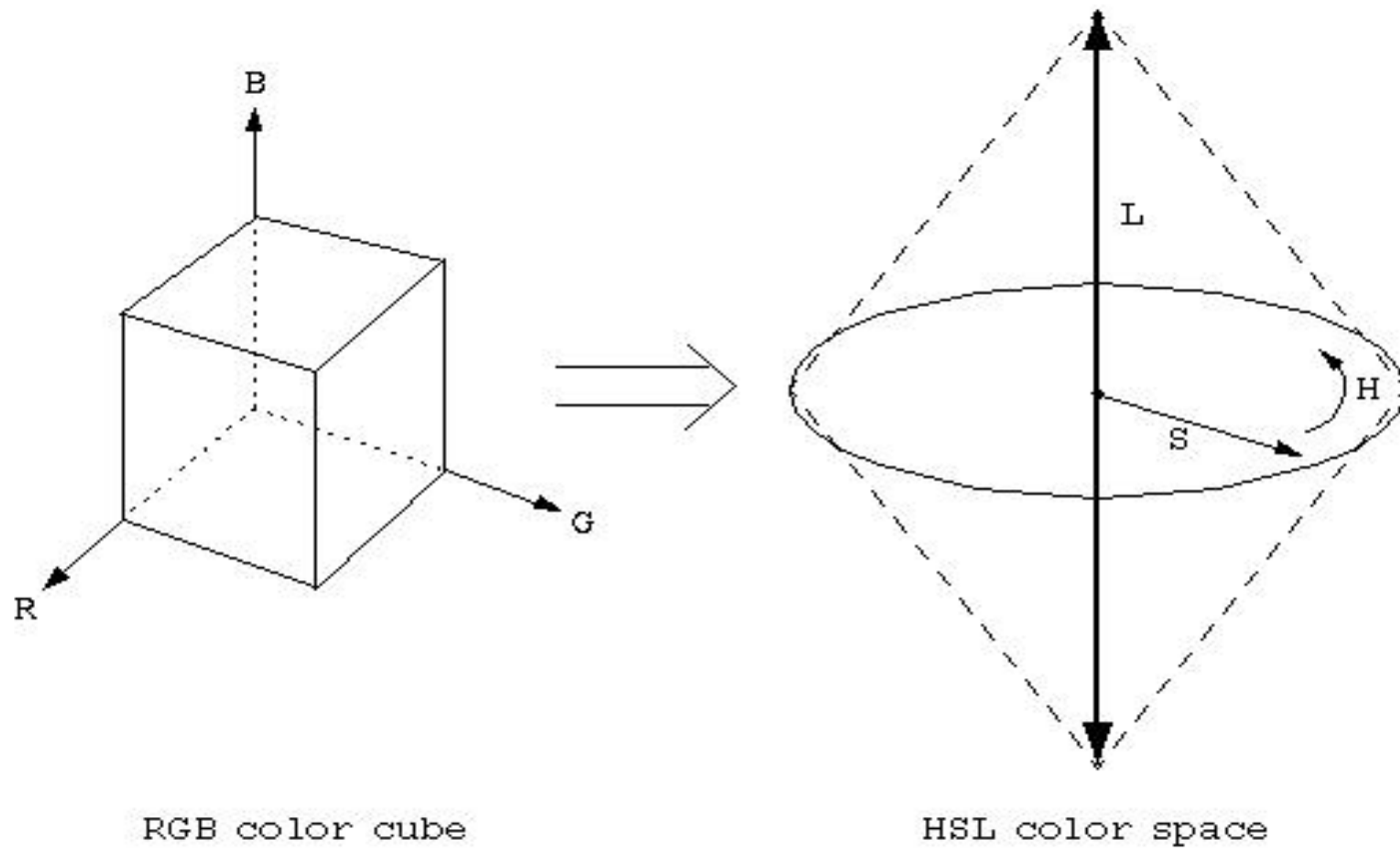
49

HSL Color Space



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RGB to HSL Mapping



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✓ Equations for mapping RGB to HSI are:

$$H = \begin{cases} \theta & \text{if } B \leq G \\ 360 - \theta & \text{if } B > G \end{cases}$$

where

$$\theta = \cos^{-1} \left\{ \frac{\frac{1}{2}[(R - G) + (R - B)]}{[(R - G)^2 + (R - B)(G - B)]^{1/2}} \right\}$$

$$S = 1 - \frac{3}{(R + G + B)} [\min(R, G, B)]$$

$$I = \frac{(R + G + B)}{3}$$

Note: See text for HSL, HSV and inverse of the equations

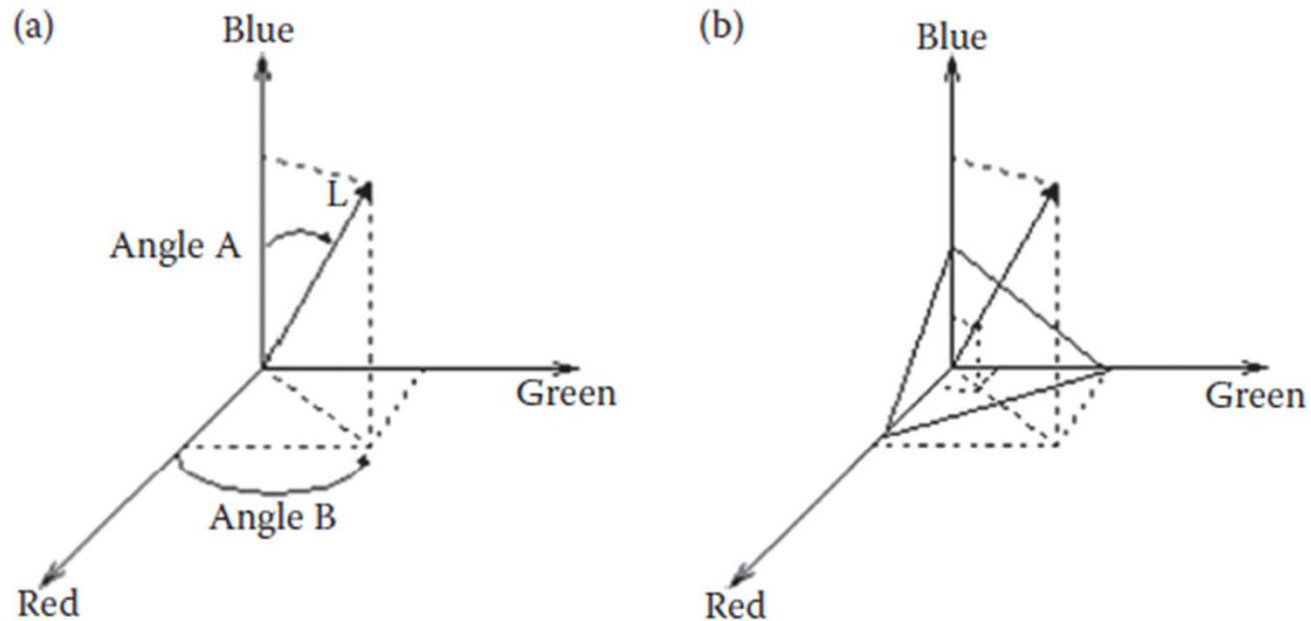
- 
- Spherical Coordinate Transform (SCT):
 - ✓ Maps color information into two angles (A and B), and the brightness into color vector length (L)
 - ✓ Equations relating SCT to RGB components are:

$$L = \sqrt{R^2 + G^2 + B^2}$$

$$\angle A = \cos^{-1} \left[\frac{B}{L} \right]$$

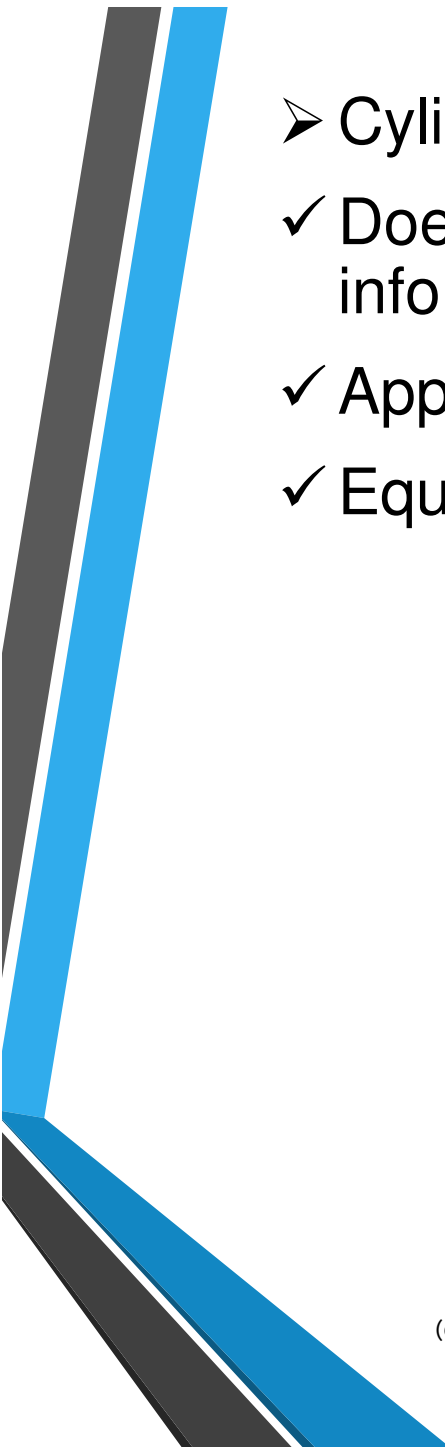
$$\angle B = \cos^{-1} \left[\frac{R}{L \sin(\angle A)} \right]$$

Spherical Coordinate Transform



Then SCT represents a color pixel vector by two angles and the vector length

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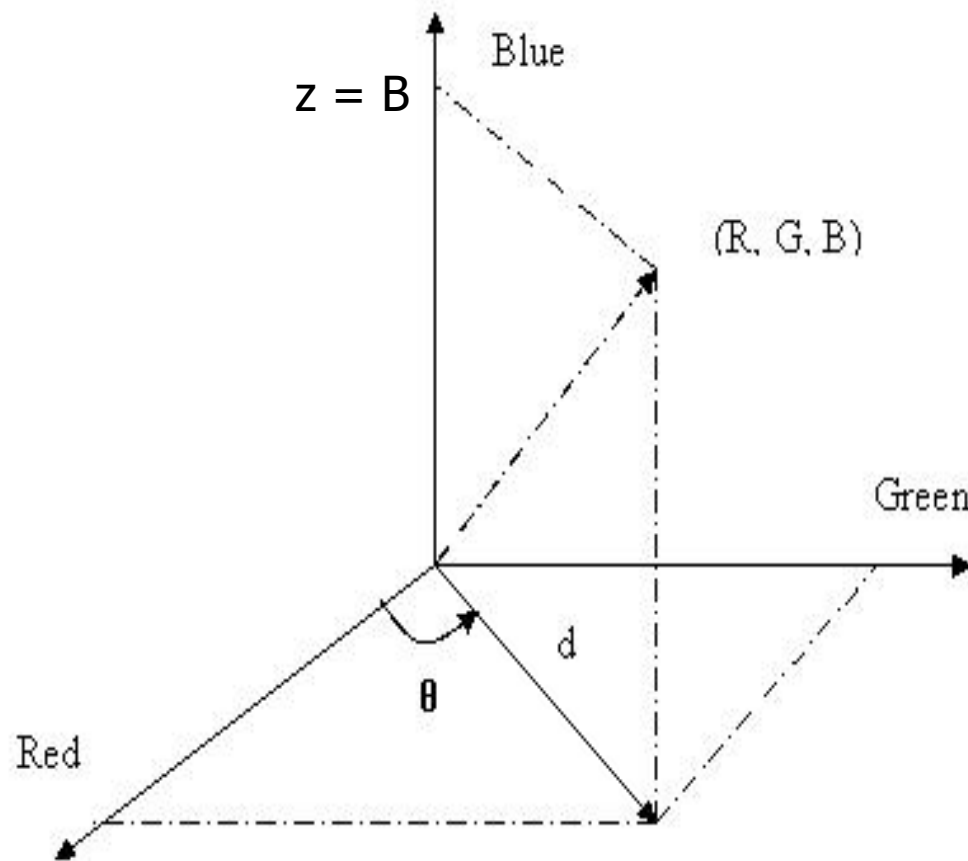
- 
- Cylindrical coordinate transform (CCT):
 - ✓ Does not completely separate brightness and color information
 - ✓ Application specific
 - ✓ Equations for finding CCT are:

$$z = B$$

$$d = \sqrt{R^2 + G^2}$$

$$\theta = \tan^{-1}\left(\frac{G}{R}\right)$$

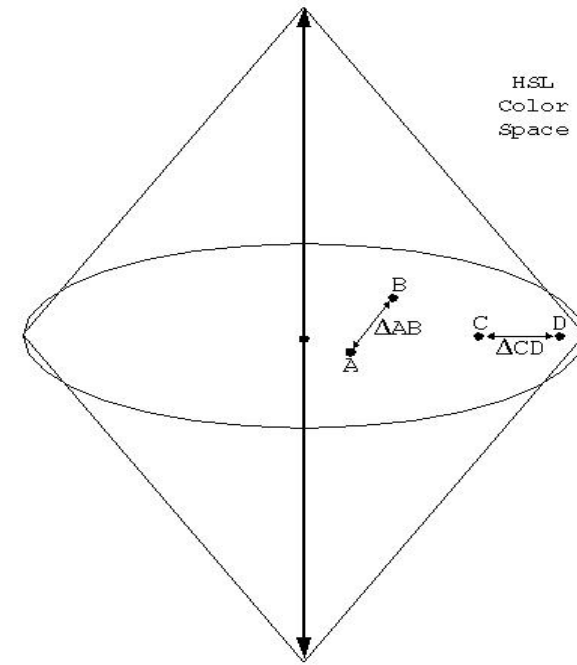
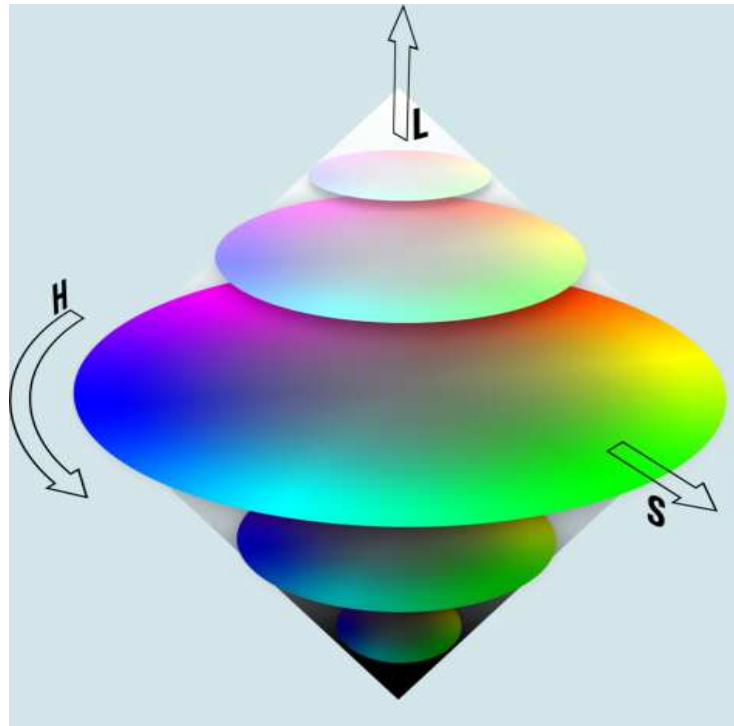
Cylindrical coordinates transform



Then CCT represents a color pixel vector by one angle and two distance measures

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- Comparing colors in the previously defined color spaces are not well correlated to human visual perception



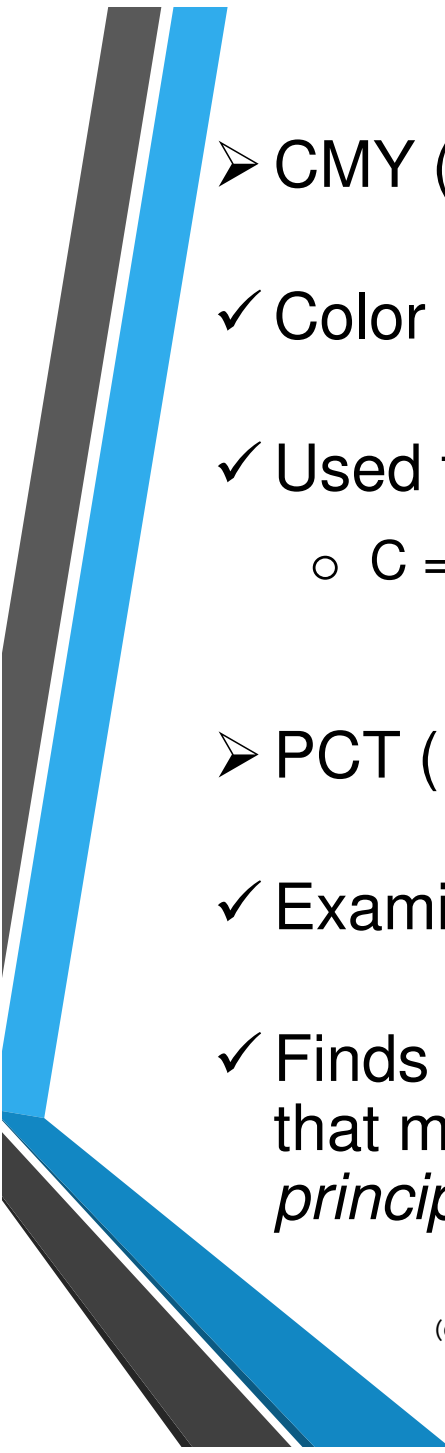
Color perception. Color A may be green and color B may be orange. Colors C and D may be slightly different shades green, but $\Delta CD = \Delta AB$.

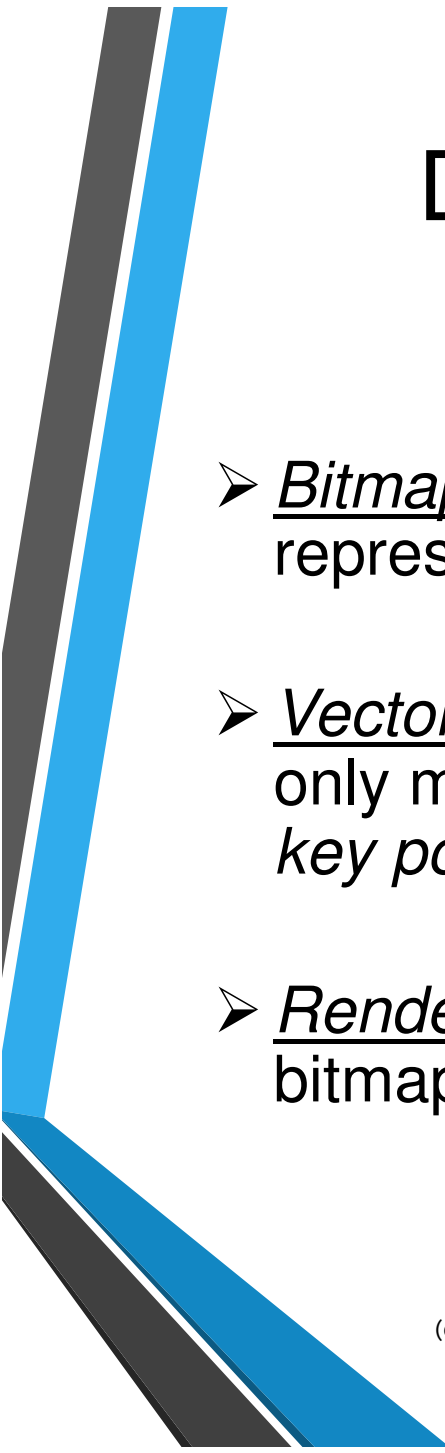
- 
- Chromaticity coordinates:
 - ✓ Normalizes RGB values to the sum of all three
 - ✓ Chromaticity coordinates are:

$$r = \frac{R}{R + G + B}$$

$$g = \frac{G}{R + G + B}$$

$$b = \frac{B}{R + G + B}$$

- 
- CMY (Cyan, Magenta, Yellow)/CMYK:
 - ✓ Color transform based on subtractive model
 - ✓ Used for color printing:
 - $C = 1 - R$; $M = 1 - G$; $Y = 1 - B$; $K = \text{Black}$
 - PCT (Principal components transform):
 - ✓ Examines all RGB vectors within an image
 - ✓ Finds linear transform, that aligns the coordinate axes so that most of the information is along one axis, the *principal axis*



Digital Image File Formats

- Bitmap images (*raster images*): Images that can be represented by our image model, $I(r,c)$
- Vector images: Artificially generated images by storing only mathematical description of geometric shapes using *key points*
- Rendering: Process of turning a vector image into a bitmap image



➤ Image file header: A set of parameters found at the start of the file image and contains information regarding:

- ✓ Number of rows (height)
- ✓ Number of columns (width)
- ✓ Number of bands
- ✓ Number of bits per pixel (bpp)
- ✓ File type

- Look-up table (LUT): Used for storing RGB values for 8-bit color images

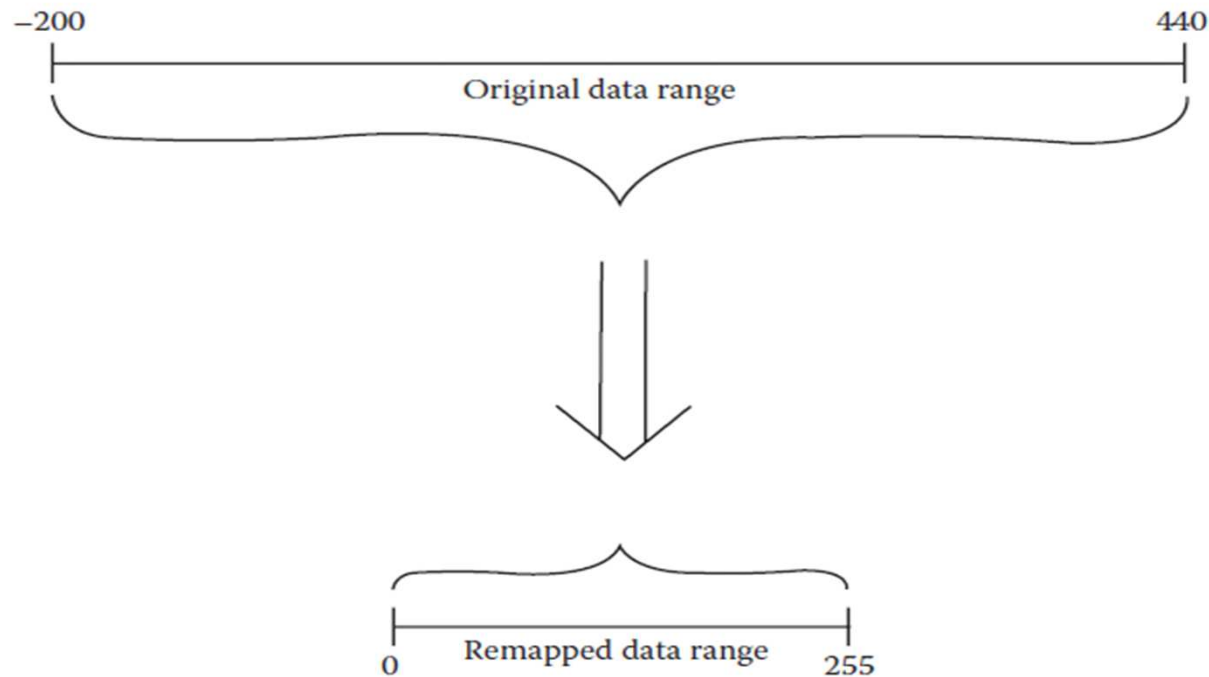
<u>8-bit Index</u>	RED	GREEN	BLUE
0	R_0	G_0	B_0
1	R_1	G_1	B_1
2	R_2	G_2	B_2
⋮	⋮	⋮	⋮
254	R_{254}	G_{254}	B_{254}
255	R_{255}	G_{255}	B_{255}

One byte is stored for each pixel in $I(r, c)$. When displayed, this 8-bit value is used as an index into the LUT, and the corresponding RGB values are displayed for that pixel.

➤ Common image file formats are:

- ✓ BIN, RAW
- ✓ PPM,PBM,PGM
- ✓ BMP
- ✓ JPEG, JPEG2000
- ✓ TIFF
- ✓ GIF
- ✓ RAS (Sun – old format)
- ✓ SGI (Silicon Graphics – old format)
- ✓ PNG
- ✓ PICT (old Apple format)
- ✓ EPS
- ✓ VIP, VIPM

- **Remapping for display.** If data range exceeds the bounds of a standard 8-bit (per band) image, it must be remapped for display. Typically with a linear remapping process. Note that data precision will be lost.



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