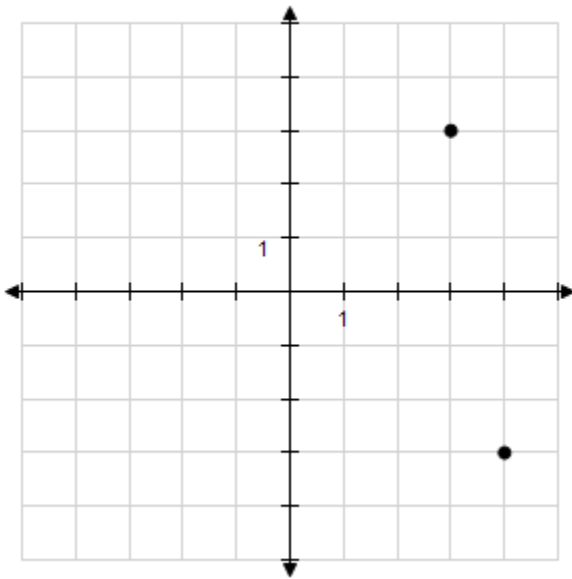


***Algebra and Trigonometry 5th edition Stewart Test
Bank***

SKU: 9780357753644-TEST-BANK

1.1 The Coordinate Plane

1. Find the coordinates of the points shown in the figure.



- a. $(4, -3), (3, 3)$
- b. $(-4, 3), (3, -3)$
- c. $(4, 3), (3, 3)$
- d. $(4, -3), (-3, 3)$
- e. $(4, -3), (3, -3)$

ANSWER: a

2. Find the distance between the points $(3, -4)$ and $(9, 4)$.

- a. 64
- b. 6
- c. 10
- d. 10
- e. 100

ANSWER: d

3. For the points $(5, 3)$ and $(2, 5)$:

- (a) Find the distance between them.
- (b) Find the midpoint of the line segment that joins them.

- a. (a) The distance is $\sqrt{13}$.
- (b) The midpoint is $\left(\frac{7}{2}, 4\right)$.
- b. (a) The distance is 13.

1.1 The Coordinate Plane

(b) The midpoint is $\left(\frac{7}{2}, 4\right)$.

c. (a) The distance is $\sqrt{13}$.

(b) The midpoint is $(7, 4)$.

d. (a) The distance is 13.

(b) The midpoint is $(7, 4)$.

e. (a) The distance is 13.

(b) The midpoint is $\left(4, -\frac{7}{2}\right)$.

ANSWER: a

4. Find the midpoint of the segment joining the points $(5, -6)$ and $(11, 2)$.

a. $(-2, -4)$

b. $(-2, 8)$

c. $(-4, -10)$

d. $(8, -2)$

e. $(-10, -2)$

ANSWER: d

5. Find the midpoint of the segment that joins the points $(6, 0)$ and $(0, 14)$.

a. $(3, 6)$

b. $(3, 7)$

c. $(3, 8)$

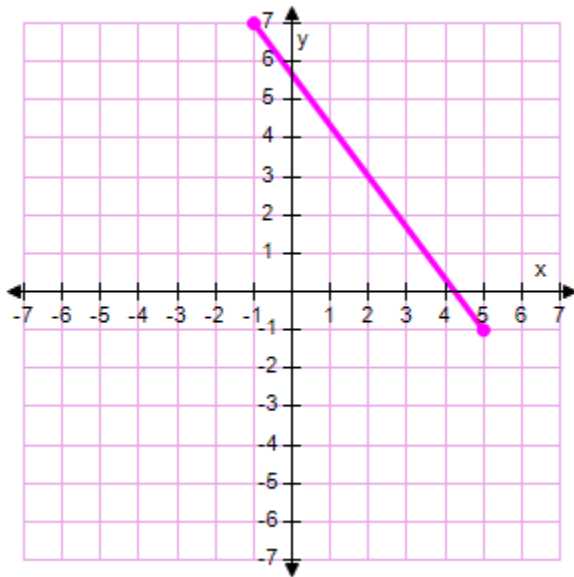
d. $(7, 3)$

e. $(6, 7)$

ANSWER: b

6. A pair of points is graphed.

1.1 The Coordinate Plane



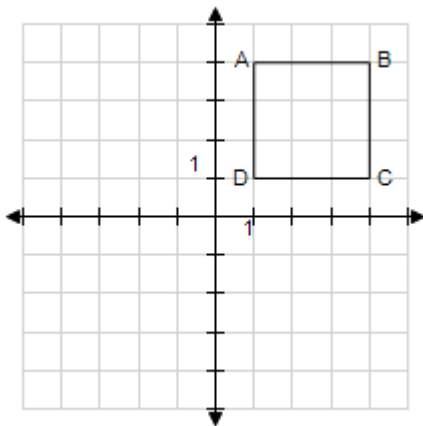
Find the midpoint of the segment that joins them.

- a. (3, 0)
- b. (1, 3)
- c. (2, 3)
- d. (1, 2)
- e. (2, 2)

ANSWER: c

7. Draw the square with vertices $A(1, 1)$, $B(4, 1)$, $C(4, 4)$, and $D(1, 4)$ on a coordinate plane. Find the area of the square.

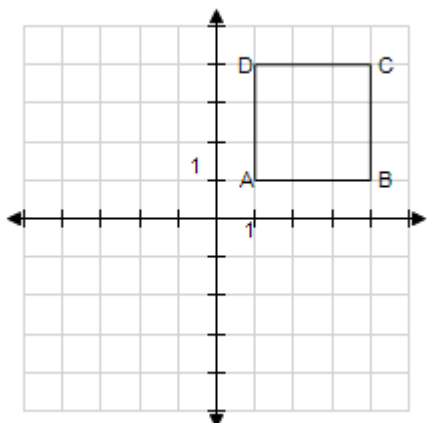
a.



The area is 9.

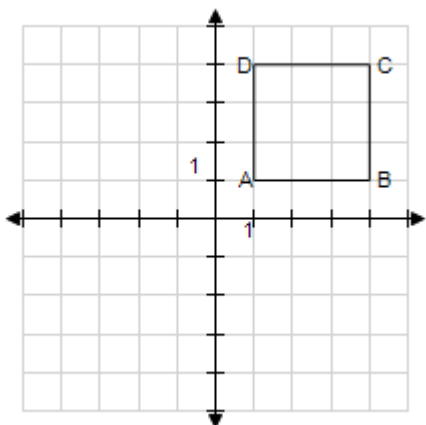
1.1 The Coordinate Plane

b.



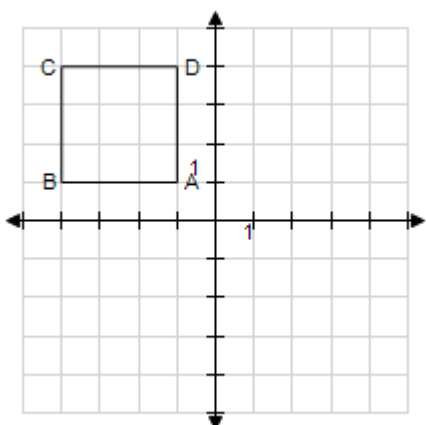
The area is 3.

c.



The area is 9.

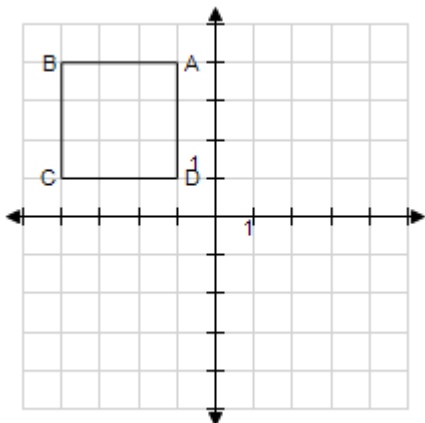
d.



The area is 3.

1.1 The Coordinate Plane

e.



The area is 12.

ANSWER: c

8. A rectangle has the vertices of $A(2, 5)$, $B(4, 5)$, $C(2, 0)$, and $D(4, 0)$ on a coordinate plane. Find the area of the rectangle.

- a. 9
- b. 14
- c. 10
- d. 11
- e. 6

ANSWER: c

9. The parallelogram has the vertices of $A(2, 1)$, $B(8, 1)$, $C(9, 4)$, and $D(3, 4)$ on a coordinate plane. Find the area of the parallelogram.

- a. 17
- b. 18
- c. 20
- d. 16
- e. 19

ANSWER: b

10. If the points $P(6, 2)$, $Q(0, 8)$, and $R(-6, 2)$ are drawn on a coordinate plane, where must the point S be located so that the figure $PQRS$ is a square?

- a. $(0, -4)$
- b. $(-6, 0)$
- c. $(0, -3)$
- d. $(-4, 0)$
- e. $(0, -5)$

ANSWER: a

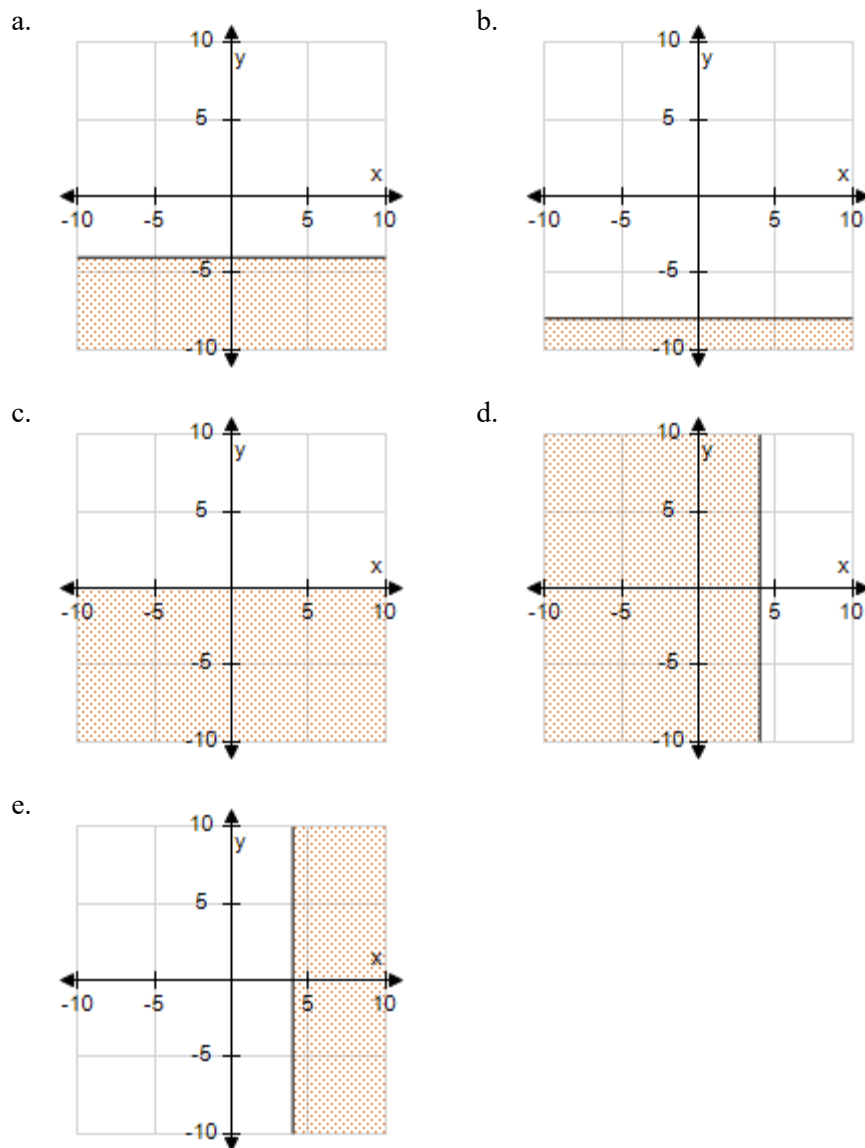
1.1 The Coordinate Plane

11. Determine which of the points $(-5, 0)$, $(5, 20)$, and $(-\sqrt{5}, 2\sqrt{5})$ are on the graph of the equation $x^2 + y^2 = 25$

- a. $(5, 20)$, $(-\sqrt{5}, 2\sqrt{5})$
- b. $(-5, 0)$, $(-\sqrt{5}, 2\sqrt{5})$
- c. $(-5, 0)$, $(5, 20)$, $(-\sqrt{5}, 2\sqrt{5})$
- d. $(-5, 0)$, $(5, 20)$
- e. None

ANSWER: b

12. Determine the sketch of the region given by the set $\{(x, y) \mid x \leq 4\}$.

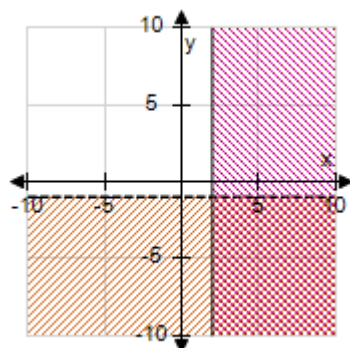


ANSWER: d

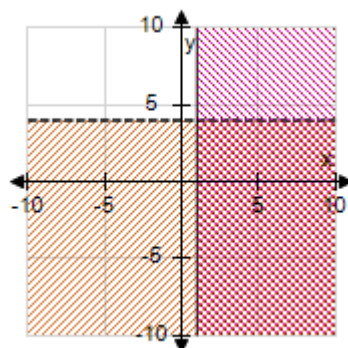
13. Determine the sketch of the region given by the set $\{(x, y) \mid x \geq 4 \text{ and } y < 1\}$.

1.1 The Coordinate Plane

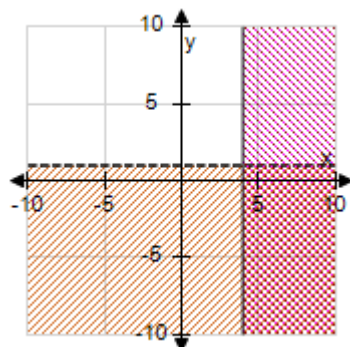
a.



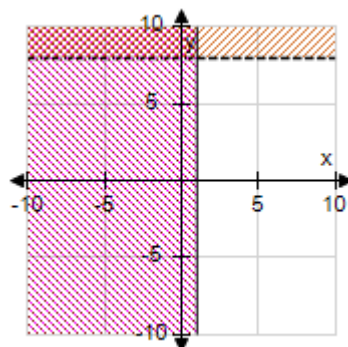
b.



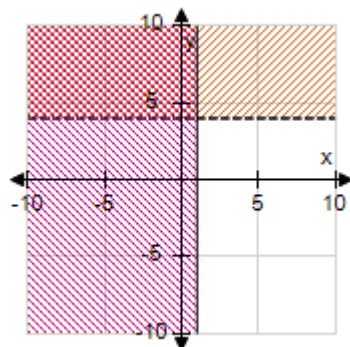
c.



d.



e.

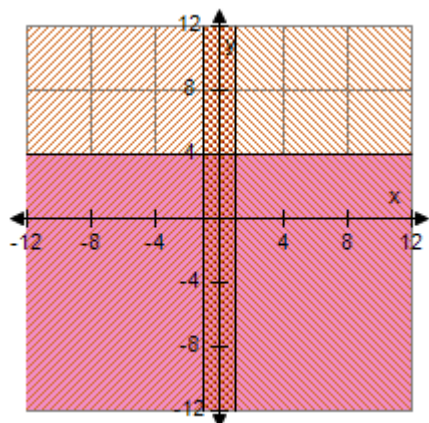


ANSWER: c

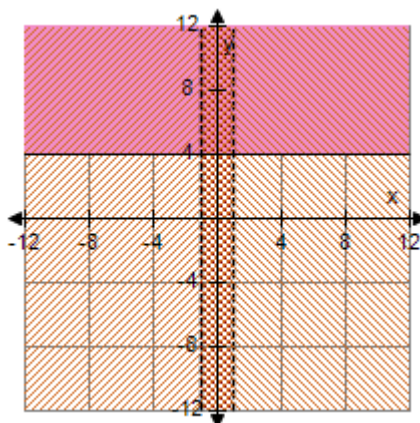
14. Determine the sketch of the region given by the set $\{(x, y) \mid -1 < x < 1 \text{ and } y \geq 4\}$.

1.1 The Coordinate Plane

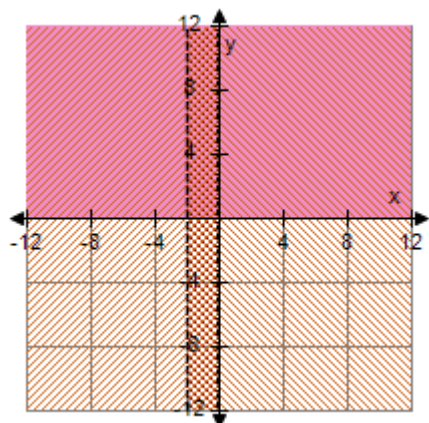
a.



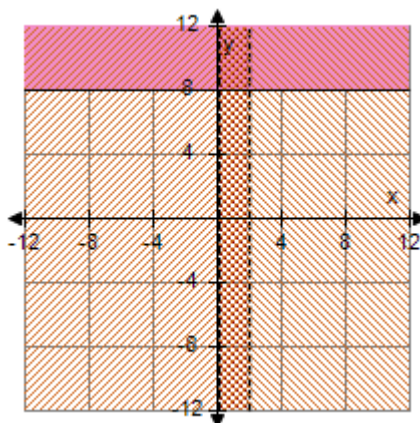
b.



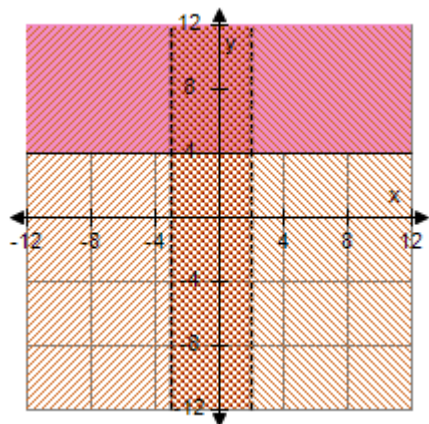
c.



d.



e.



ANSWER: b

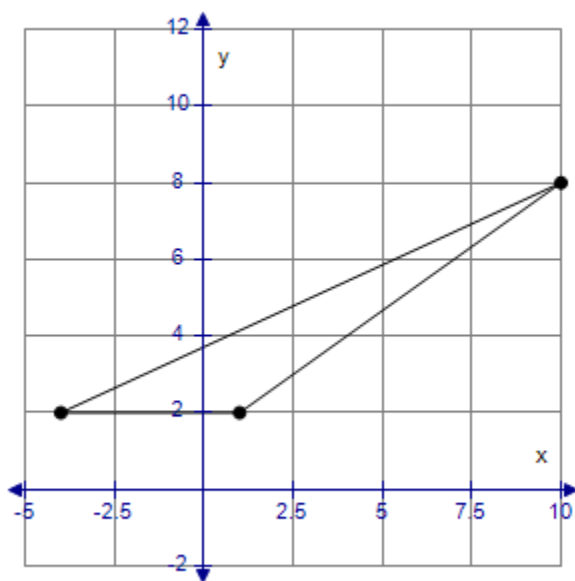
15. Determine which point $A(7, 8)$ or $B(6, 9)$ is closer to the origin?

- a. Point $A(7, 8)$ is closer to the origin.
- b. Point $B(6, 9)$ is closer to the origin.

ANSWER: a

1.1 The Coordinate Plane

16. Find the area of the triangle shown in the figure. Round to the closest positive whole number.



- a. 12
- b. 15
- c. 17
- d. 18
- e. 13

ANSWER: b

17. Find a point on the y -axis that is equidistant from the points $(2, -9)$ and $(7, 0)$.

- a. $(0, 0)$
- b. $(0, 5)$
- c. $(-2, 0)$
- d. $(0, -4)$
- e. $(0, -2)$

ANSWER: e

18. Find the point that is one-fourth of the distance from the point $P(-1, 5)$ to the point $Q(3, 17)$ along the segment PQ .

- a. $(0, -8)$
- b. $(2, 11)$
- c. $(0, 8)$
- d. $(8, 0)$
- e. $(0, 0)$

ANSWER: c

1.1 The Coordinate Plane

19. If the points $P(-7, -7)$, $Q(-6, -3)$, and $R(2, 8)$ are plotted on a coordinate plane, where should the point S be located so that the figure $PQRS$ is a parallelogram?

- a. $(2, 4)$
- b. $(1, 2)$
- c. $(1, 4)$
- d. $(4, 0)$
- e. $(0, 5)$

ANSWER: c

20. If $M(9, 7)$ is the midpoint of the line segment AB , and if A has coordinates $(5, 5)$, find the coordinates of B .

- a. $(-13, 9)$
- b. $(13, 9)$
- c. $(-5, -1)$
- d. $(-11, -8)$
- e. $(13, -9)$

ANSWER: b

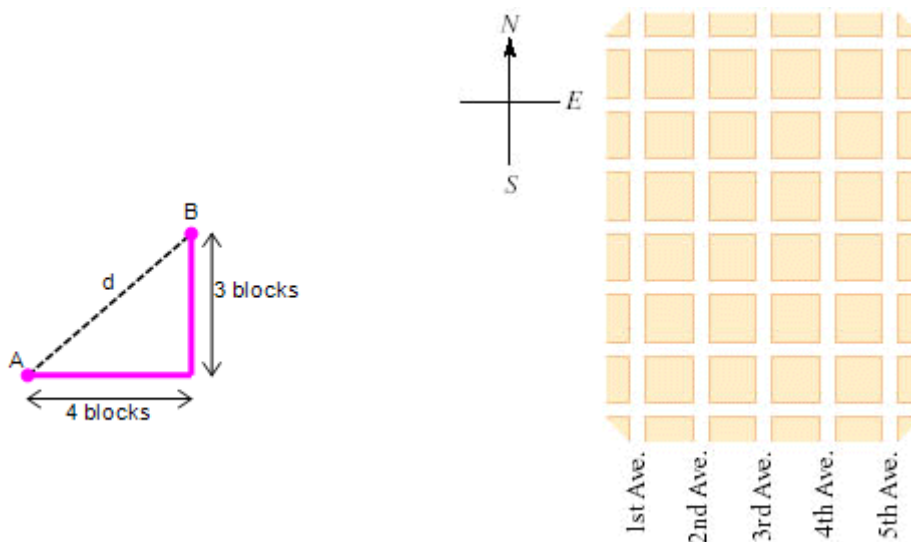
21. The parallelogram has vertices of $A(-5, -1)$, $B(1, 1)$, $C(4, 9)$, and $D(-2, 7)$. Find the midpoints of the diagonals of this parallelogram.

- a. $(0, 3.5)$, $(-0.5, 4)$
- b. $(0, 3.5)$, $(0, 3.5)$
- c. $(0, -0.5)$, $(0, -0.5)$
- d. $(1, 0)$, $(-1, 0)$
- e. $(-0.5, 4)$, $(-0.5, 4)$

ANSWER: e

22. A city has streets that run north and south, and avenues that run east and west, all equally spaced. Streets and avenues are numbered sequentially, as shown in the figure. The walking distance between points A and B is 7 blocks; that is, 4 blocks east and 3 blocks north. To find the straight-line distance d , we must use the Distance Formula.

1.1 The Coordinate Plane



Find the walking distance and the straight-line distance between the corner of 4th St. and 2nd Ave. and the corner of 19th St. and 38th Ave.

- The walking distance is 51 blocks and the straight-line distance is 40 blocks.
- The walking distance is 50 blocks and the straight-line distance is 39 blocks.
- The walking distance is 53 blocks and the straight-line distance is 41 blocks.
- The walking distance is 50 blocks and the straight-line distance is 40 blocks.
- The walking distance is 51 blocks and the straight-line distance is 39 blocks.

ANSWER: e

23. Find the distance between $(-2, 7)$ and $(1, 11)$.

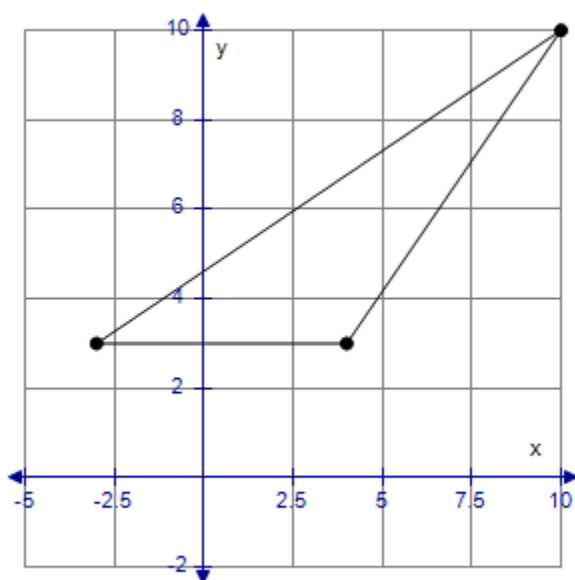
ANSWER: 5

24. A rectangle has vertices of $A(5, 5)$, $B(11, 5)$, $C(5, 2)$, and $D(11, 2)$ on a coordinate plane. Find the area of the rectangle.

ANSWER: 18

25. Find the area of the triangle shown in the figure.

1.1 The Coordinate Plane



ANSWER: 24.5

26. Find the midpoint of the segment joining the points $(5, -9)$ and $(7, -5)$.

ANSWER: $(6, -7)$

27. Find the midpoint of the segment that joins the points $(2, 0)$ and $(0, 6)$.

ANSWER: $(1, 3)$

28. The parallelogram has the vertices of $A(4, 4)$, $B(8, 4)$, $C(10, 6)$, and $D(6, 6)$ on a coordinate plane. Find the area of the parallelogram.

ANSWER: 8

29. Find a point on the y -axis that is equidistant from the points $(4, -8)$ and $(7, 3)$.

ANSWER: $(0, -1)$

30. Find the point that is one-fourth of the distance from the point $P(-2, 5)$ to the point $Q(6, 13)$ along the segment PQ .

ANSWER: $(0, 7)$

31. The points $P(-8, -9)$, $Q(4, -3)$, and $R(11, 4)$ are on a coordinate plane. Where should the point S be located so that the figure $PQRS$ is a parallelogram?

ANSWER: $(-1, -2)$

32. If $M(7, 7)$ is the midpoint of the line segment AB , and if A has coordinates $(5, 3)$, find the coordinates of B .

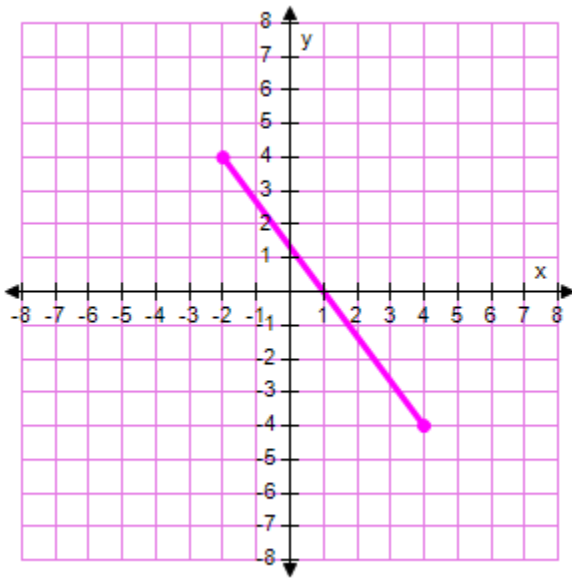
ANSWER: $(9, 11)$

33. The parallelogram has vertices of $A(-1, -1)$, $B(4, 1)$, $C(9, 8)$, and $D(4, 6)$. Find the midpoints of the diagonals of this parallelogram.

ANSWER: $(4, 3.5); (4, 3.5)$

1.1 The Coordinate Plane

34. A pair of points is graphed.



Find the distance between them. _____

Find the midpoint of the segment that joins them. _____

ANSWER: 10; (1, 0)

35. Which of the points $A(6, 7)$ or $B(5, 8)$ is closer to the origin, Point A or B ?

ANSWER: A

1.2 Graphs of Equations in Two Variables

1. Determine which point is on the graph of the equation $y = 5x + 9$.

- a. (4, 28)
- b. (5, 9)
- c. (1, 27)
- d. (4, 29)
- e. (3, 29)

ANSWER: d

2. Calculate the y -coordinates in the table below for the function $y = 7x + 4$.

x	y
-4	?
-3	?
2	?
3	?
7	?

x	y
-4	?
-3	?
2	?
3	?
7	?
x	y
-4	?
-3	?
2	?
3	?
7	?

a.

x	y
-4	-24
-3	-17
2	18
3	25
7	53

b.

x	y
-4	-23
-3	-16
2	20
3	28
7	57

c.

x	y
-4	-26
-3	-19
2	17

d.

x	y
-4	53
-3	25
2	18

1.2 Graphs of Equations in Two Variables

3	24
7	52

3	-17
7	-24

e.

x	y
-4	24
-3	17
2	-18
3	-25
7	-46

ANSWER: a

3. Calculate the y-coordinates in the table below for the function $y = 5x^2 + 2$.

x	y
-3	?
-2	?
1	?
2	?
6	?

x	y
-3	182
-2	22
1	7
2	22
6	47

a.

x	y
-3	182
-2	22
1	7
2	22
6	47

b.

x	y
-3	47
-2	22
1	7
2	22
6	180

c.

x	y
-3	-47
-2	-22
1	-7
2	-22
6	-182

d.

x	y
-3	47
-2	21
1	7
2	22
6	182

1.2 Graphs of Equations in Two Variables

e.

x	y
-3	47
-2	22
1	7
2	22
6	182

ANSWER: e

4. Fill the table of values for the function $xy = 14$.

x	y
-14	?
-7	?
1	?
7	?
14	?

a.

x	y
-14	1
-7	2
1	14
7	-2
14	-1

b.

x	y
-14	1
-7	2
1	-14
7	-2
14	-1

c.

x	y
-14	-1
-7	-2
1	14
7	2
14	1

d.

x	y
-14	-1
-7	-2
1	14
7	-3
14	-9

e.

x	y
-14	-1
-7	-2
1	14
7	-8
14	-4

ANSWER: c

1.2 Graphs of Equations in Two Variables

5. Fill in the table of values for the function $y = |x - 2|$.

x	y
-6	?
-2	?
1	?
3	?
7	?

a.

x	y
-6	-8
-2	-4
1	1
3	1
7	5

b.

x	y
-6	8
-2	4
1	-1
3	-1
7	-5

c.

x	y
-6	-8
-2	-4
1	-1
3	-1
7	-1

d.

x	y
-6	5
-2	1
1	1
3	4
7	8

e.

x	y
-6	8
-2	4
1	1
3	1
7	5

ANSWER: e

6. Fill in the table of values for the function $y = 20 - 4x^3$.

x	y
-3	?
-2	?
1	?
2	?
3	?

1.2 Graphs of Equations in Two Variables

a.

x	y
-3	127
-2	52
1	16
2	-12
3	-88

b.

x	y
-3	-128
-2	-52
1	-16
2	12
3	88

c.

x	y
-3	-88
-2	-12
1	16
2	52
3	128

d.

x	y
-3	128
-2	52
1	16
2	-14
3	-88

e.

x	y
-3	128
-2	52
1	16
2	-12
3	-88

ANSWER: e

7. Fill in the table of values for the function $y = 9 - 5x^4$.

x	y
-2	?
-1	?
1	?
2	?
3	?

a.

x	y
-2	-71
-1	4
1	4
2	-71
3	-396

b.

x	y
-2	-396
-1	-71
1	4
2	5
3	-71

c.

x	y
-----	-----

d.

x	y
-----	-----

1.2 Graphs of Equations in Two Variables

-2	71
-1	-4
1	-4
2	71
3	396

-2	-71
-1	4
1	3
2	-71
3	-396

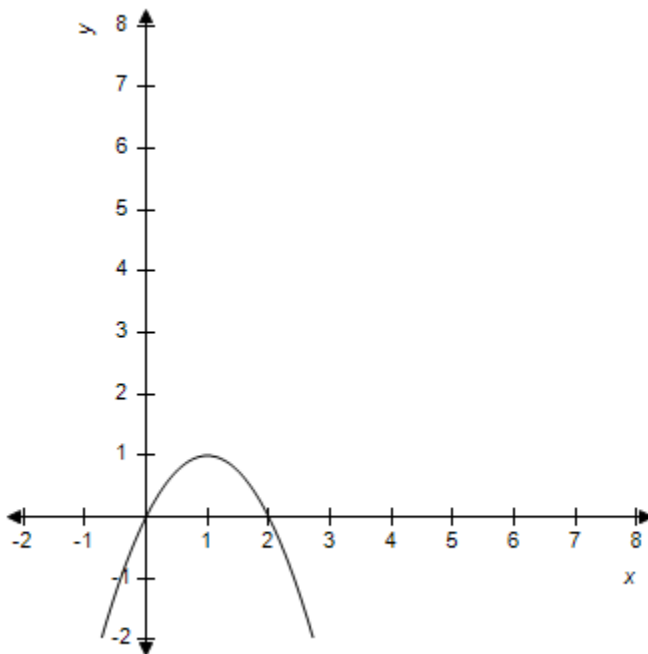
e.

x	y
-2	-70
-1	4
1	4
2	-71
3	-396

ANSWER: a

8. An equation and its graph are given. Find the x -intercepts.

$$y = 2x - x^2$$



- a. 0
- b. 0, 5
- c. 5
- d. 0, 2
- e. 2

ANSWER: d

1.2 Graphs of Equations in Two Variables

9. Find the x - and y -intercepts of the graph of the equation $y = 2x + 3$.

- a. x - intercept $\frac{3}{2}$, y - intercept 3.
- b. x - intercept $-\frac{3}{2}$, y - intercept -4 .
- c. x - intercept $\frac{3}{2}$, y - intercept 3.
- d. x - intercept $-\frac{3}{2}$, y - intercept 3.
- e. x - intercept $-\frac{3}{2}$, y - intercept 2.

ANSWER: d

10. Find the x - and y -intercepts of the graph of the equation $y = \sqrt{2x + 5}$.

- a. x - intercept $\frac{5}{2}$, y - intercept $-\sqrt{5}$
- b. x - intercept $-\frac{5}{2}$, y - intercept $-\sqrt{5}$
- c. x - intercept $\frac{2}{5}$, y - intercept $\sqrt{5}$
- d. x - intercept $-\frac{2}{5}$, y - intercept $-\sqrt{5}$
- e. x - intercept $-\frac{5}{2}$, y - intercept $\sqrt{5}$

ANSWER: e

11. Find the x and y - intercepts of the graph of $x^2 + 2xy + 9y^2 = 9$.

- a. x - intercepts ± 3 , y - intercepts ± 3
- b. x - intercepts ± 3 , y - intercepts ± 1
- c. x - intercept 3 , y - intercepts ± 1
- d. x - intercept 3 , y - intercept 1
- e. x - intercepts ± 1 , y - intercepts $\pm \frac{1}{3}$

ANSWER: b

12. Determine which of the points $(-4, 0)$, $(2, 14)$, and $(-\sqrt{2}, \sqrt{14})$ are on the graph of the equation $x^2 + y^2 = 16$

1.2 Graphs of Equations in Two Variables

- a. $(2, 14), (-\sqrt{2}, \sqrt{14})$
- b. $(-4, 0), (-\sqrt{2}, \sqrt{14})$
- c. $(-4, 0), (2, 14), (-\sqrt{2}, \sqrt{14})$
- d. $(-4, 0), (2, 14)$
- e. None

ANSWER: b

13. Test the equation $y = 3x^3 + 5x$ for symmetry.

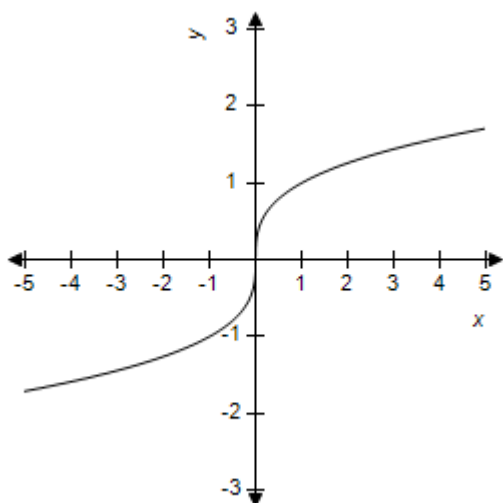
- a. The symmetry is around the x -axis.
- b. The symmetry is around the y -axis.
- c. The symmetry is around the point $(5, 5)$.
- d. The symmetry is around the origin.
- e. There is no symmetry.

ANSWER: d

14. Test the equation for symmetry to determine the correct graph.

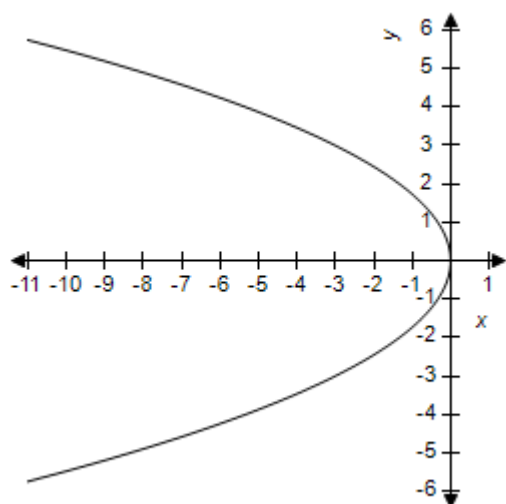
$$y^2 - 3x = 0$$

- a. *origin- symmetry*

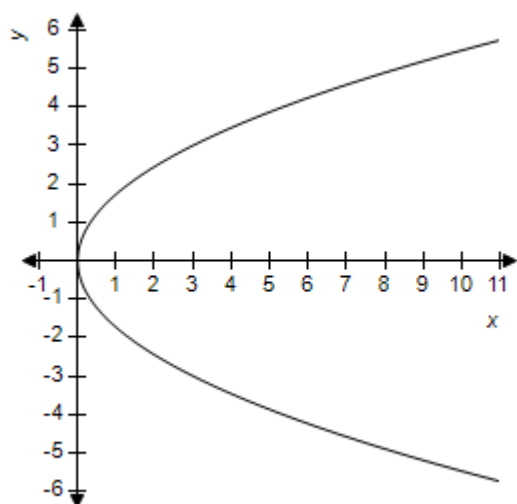


- b. *x-axis symmetry*

1.2 Graphs of Equations in Two Variables

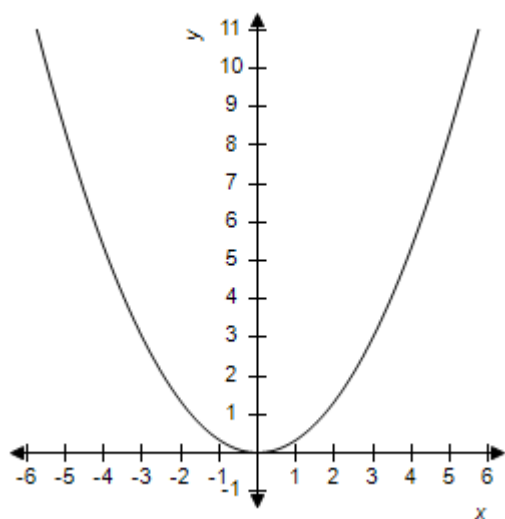


c. *x-axis symmetry*



d. *y-axis symmetry*

1.2 Graphs of Equations in Two Variables

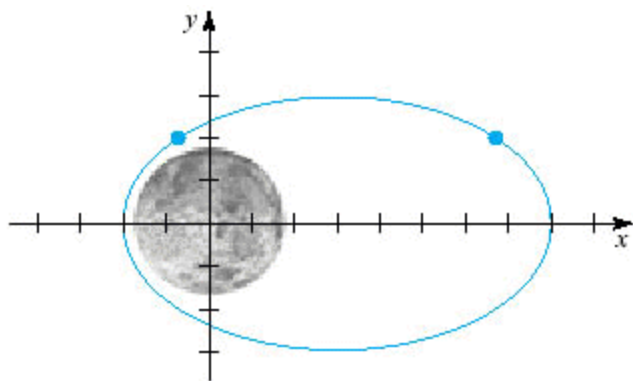


e. none

ANSWER: c

15. A satellite is in orbit around a planet. A coordinate plane containing the orbit is set up with the center of the planet at the origin, as shown in the graph, with distances measured in megameters (Mm). The equation of the satellite's orbit is

$$\frac{(x-3)^2}{25} + \frac{y^2}{16} = 1$$



There are two points in the orbit with y -coordinates equal to 2. Find the x -coordinates of these points. Please round the answers to two decimal places.

- a. 7.31, -1.35
- b. 7.29, -1.29
- c. 7.33, -1.33
- d. 7.33, -1.35
- e. 7.31, -1.33

ANSWER: c

16. Find the x - and y -intercepts of the graph of the equation $y = 3x + 7$.

1.2 Graphs of Equations in Two Variables

x-intercept = _____

y-intercept = _____

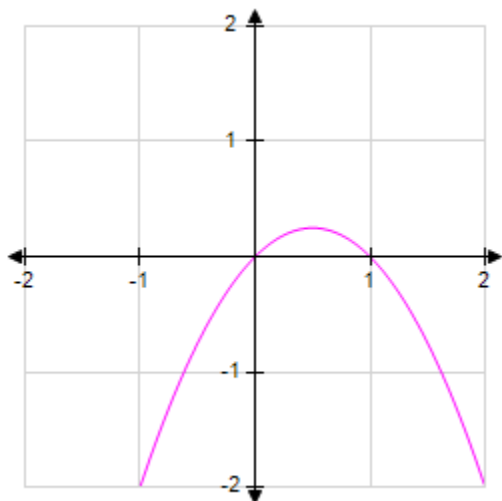
ANSWER: $-\frac{7}{3}; 7$

17. Find the x- and y-intercepts of the graph of the equation $y = \sqrt{3x + 5}$

ANSWER: $-\frac{5}{3}, \sqrt{5}$

18. An equation and its graph are given.

$$y = x - x^2$$



Find the x-intercepts.

x = _____

Find the y-intercepts.

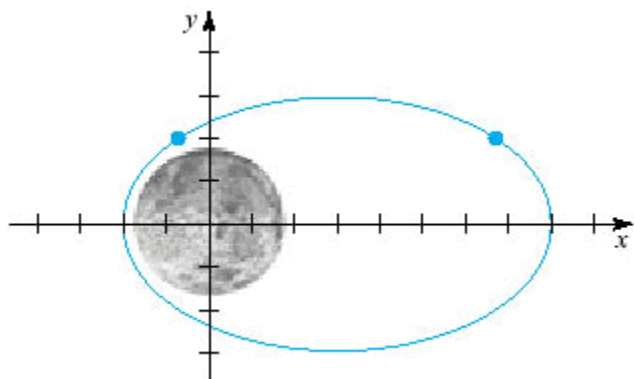
y = _____

ANSWER: 0, 1; 0

19. A satellite is in orbit around a planet. A coordinate plane containing the orbit is set up with the center of the planet at the origin, as shown in the graph, with distances measured in megameters (Mm). The equation of the satellite's orbit is

$$\frac{(x - 6)^2}{100} + \frac{y^2}{64} = 1$$

1.2 Graphs of Equations in Two Variables



Round your answers to two decimal places when necessary.

From the graph, determine the closest that the satellite gets to the center of the planet.

_____ Mm

From the graph, determine the furthest that the satellite gets from the center of the planet.

_____ Mm

There are two points in the orbit with y -coordinates equal to 4. Find the x -coordinates of these points.

Determine their distances to the center of the planet.

ANSWER: 4; 16; 14.66; -2.66; 15.16; 4.80

Determine which points are on the graphs of the given equations.

Match each point below with the letter of the corresponding equation.

a. $y = 4x + 9$

b. $y = \sqrt{x - 2}$

c. $x^2 + y^2 - 13 = 0$

20. $(3, 1)$

ANSWER: b

21. $(2, 3)$

ANSWER: c

22. $(-4, -7)$

ANSWER: a

Test each of the equations for symmetry.

Match each description below with the letter of the corresponding equation.

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1.2 Graphs of Equations in Two Variables

a. $y = 2x^4 + 7x^2 + 8$

b. $x = 7y^4 - 2y^2$

c. $y = 2x^3 - 7x$

23. symmetry about x -axis

ANSWER: b

24. symmetry about y -axis

ANSWER: a

25. symmetry about the origin

ANSWER: c

1.3 Circles

1. Find the center and radius of the circle with the equation of $x^2 + y^2 + 4x = 0$

- a. center (2, 0), radius 4
- b. center (-2, 0), radius 4
- c. center (-2, 0), radius 2
- d. center (0, -2), radius 4
- e. center (-2, 0), radius 5

ANSWER: c

2. Find the center and radius of the circle for the equation of $x^2 + y^2 - 2x - 2y = 2$.

- a. center (-1, -1), radius 4
- b. center (-1, 1), radius 2
- c. center (-1, 0), radius 2
- d. center (1, -1), radius 4
- e. center (1, 1), radius 2

ANSWER: e

3. Find the center and radius of the circle with the equation $x^2 + y^2 - \frac{1}{3}x + \frac{1}{3}y = -\frac{1}{36}$.

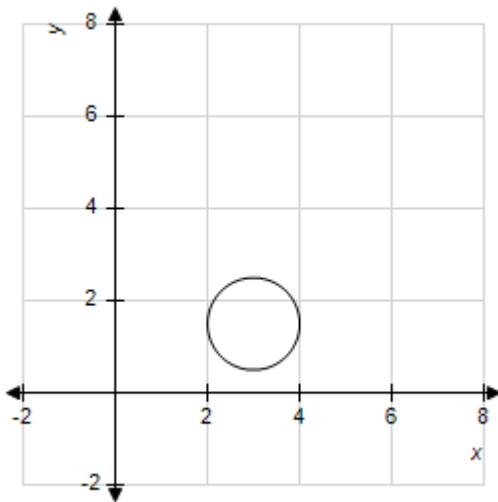
- a. center $\left(\frac{1}{6}, \frac{1}{6}\right)$, radius $\frac{1}{36}$
- b. center $\left(\frac{1}{6}, \frac{1}{6}\right)$, radius $\frac{1}{9}$
- c. center $\left(\frac{1}{6}, \frac{1}{6}\right)$, radius $\frac{1}{3}$
- d. center $\left(\frac{1}{3}, \frac{1}{3}\right)$, radius $\frac{1}{36}$
- e. center $\left(\frac{1}{6}, -\frac{1}{6}\right)$, radius $\frac{1}{6}$

ANSWER: e

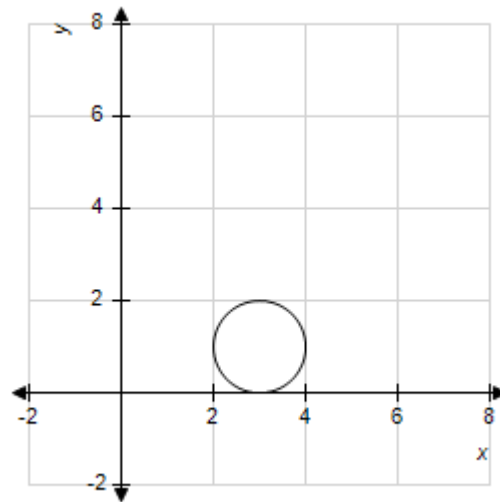
4. Determine the graph of the equation $x^2 + y^2 - 6x - 2y = -9$.

1.3 Circles

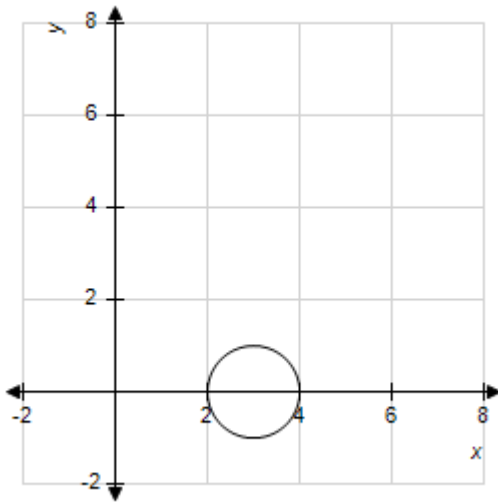
a.



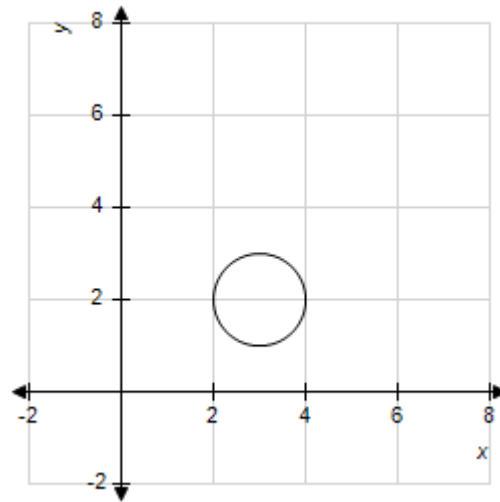
b.



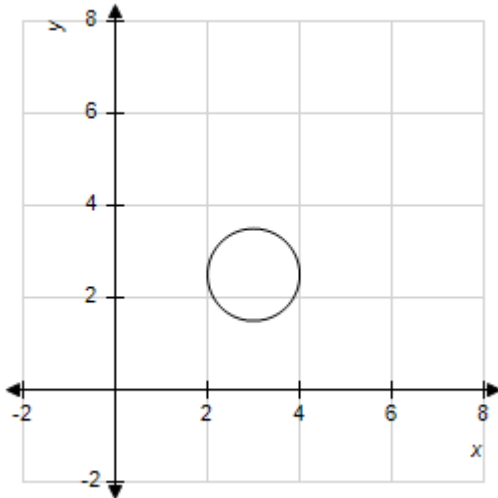
c.



d.



e.



1.3 Circles**ANSWER:** b5. The endpoints of a diameter of a circle are $P(1, 4)$ and $Q(4, 7)$. Find the equation of the circle.

- a. $(x - 2)^2 + (y - 5)^2 = 4.5$
- b. $(x - 5)^2 + y^2 = 26$
- c. $(x + 2.5)^2 + (y + 5.5)^2 = 4.5$
- d. $(x - 5)^2 + (y - 5.5)^2 = 2.25$
- e. $(x - 2.5)^2 + (y - 5.5)^2 = 4.5$

ANSWER: e6. Find an equation of the circle with the center at $(-3, 4)$ and a radius of 1.

- a. $(x + 3)^2 + (y - 4)^4 = 1$
- b. $(x - 5)^2 + y^2 = 25$
- c. $(x + 3)^2 + (y - 4)^2 = 1$
- d. $(x + 3)^2 + (y + 4)^2 = 1$
- e. $(x - 5)^2 + (y + 1)^2 = 9$

ANSWER: c7. Find the equation of the circle with center $(-3, 8)$ and radius $\sqrt{3}$.

- a. $x^2 - 6x - y^2 - 16y - 70 = 0$
- b. $x^2 - 16x + 70 + y^2 - 6y = 0$
- c. $x^2 + 6x + y^2 - 16y + 70 = 0$
- d. $x^2 + 16x + 70 + y^2 - 6y = 0$
- e. $x^2 + 6x + y^2 - 32y + 73 = 0$

ANSWER: c8. Find the equation of the circle with center $(0, -3)$ and tangent to the x -axis.

- a. $(x + 3)^2 + (y - 3)^2 = 5$
- b. $(x)^2 + (y - 3)^2 = 9$
- c. $(x)^2 + (y + 3)^2 = 9$
- d. $(x)^2 + (y + 3)^2 = 5$

1.3 Circles

e. $(x-3)^2 + (y)^2 = 9$

ANSWER: c

9. Find the area of the region that lies outside of the circle $x^2 + y^2 = 9$ but inside of the circle $x^2 + y^2 - 6y = 55$ to two decimal places.

- a. 172.79
- b. 183.79
- c. 182.79
- d. 173.79
- e. 175.79

ANSWER: a

10. Determine whether the equation represents a circle, a point, or has no graph. If the equation is that of a circle, find its center and radius.

$$x^2 + y^2 - 10x + 6y + 32 = 0$$

- a. center $(5, -3)$, radius $\sqrt{2}$
- b. center $(-5, 3)$, radius 4
- c. center $\left(-\frac{1}{3}, 5\right)$, radius $\sqrt{2}$
- d. point
- e. no graph

ANSWER: a

11. Determine what form the given equation represents.

$$x^2 + y^2 - 4x - 4y + 8 = 0$$

- a. The equation represents a single point.
- b. The equation represents an ellipse.
- c. The equation represents an empty set.
- d. The equation represents a circle.
- e. The equation represents a semi-circle with a curve approaching the positive x-axis.

ANSWER: a

12. Find the area of the region that lies outside of the circle $x^2 + y^2 = 1$ but inside of the circle $x^2 + y^2 - 2y = 8$.

Round your answer to two decimal places.

ANSWER: 25.13

Find the equations of the circles that satisfy the given conditions.

1.3 Circles

Match each equation below with the letter of the corresponding condition set.

- a. center $(-2, 2)$, radius 1
- b. center $(1, -2)$, radius 2
- c. center $(1, 0)$, radius 3

13. $(x + 2)^2 + (y - 2)^2 = 1$

ANSWER: a

14. $(x - 1)^2 + y^2 = 9$

ANSWER: c

15. $(x - 1)^2 + (y + 2)^2 = 4$

ANSWER: b

Find the equations of the circles that satisfy the given conditions.

Match each equation below with the letter of the corresponding condition set.

- a. Endpoints of a diameter are $P(3, 0)$, and $Q(5, 4)$
- b. Endpoints of a diameter are $P(2, 0)$, and $Q(6, 7)$
- c. Endpoints of a diameter are $P(4, 5)$, and $Q(9, -5)$

16. $(x - 6.5)^2 + y^2 = 31.25$

ANSWER: c

17. $(x - 4)^2 + (y - 2)^2 = 5$

ANSWER: a

18. $(x - 4)^2 + (y - 3.5)^2 = 16.25$

ANSWER: b

Determine whether each of the following equations represents a circle, a single point, or the empty set.

Match each item below with the letter of the corresponding equation.

- a. $x^2 + y^2 - 8x - 4y - 2 = 0$
- b. $x^2 + y^2 - 8x - 4y + 22 = 0$
- c. $x^2 + y^2 - 8x - 4y + 20 = 0$

Name: _____ Class: _____ Date: _____

1.3 Circles

19. empty set

ANSWER: b

20. single point

ANSWER: c

21. circle

ANSWER: a

1.4 Lines

1. Find the slope of the line through $P(-4, -3)$ and $Q(3, 4)$.

- a. $m = -4$
- b. $m = 1$
- c. $m = 2$
- d. $m = 4$
- e. $m = 7$

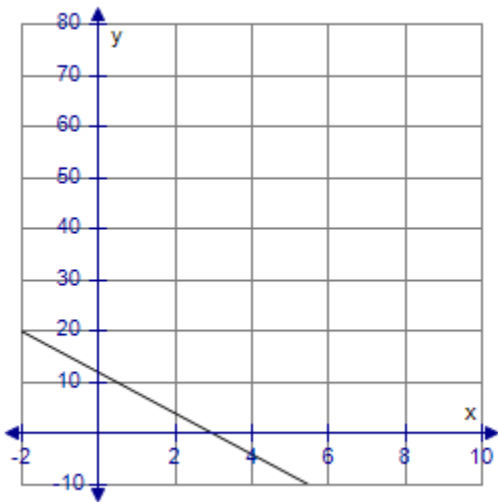
ANSWER: b

2. Find the slope of the line through $P(-8, 6)$ and $Q(-7, 11)$.

- a. $m = 4$
- b. $m = 7$
- c. $m = 6$
- d. $m = 3$
- e. $m = 5$

ANSWER: e

3. Determine the slope of the line which is sketched below.



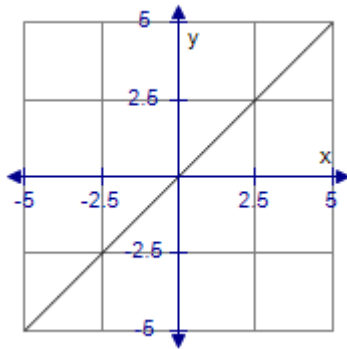
- a. $m = -9$
- b. $m = -3$
- c. $m = 2$
- d. $m = -1$
- e. $m = -4$

ANSWER: e

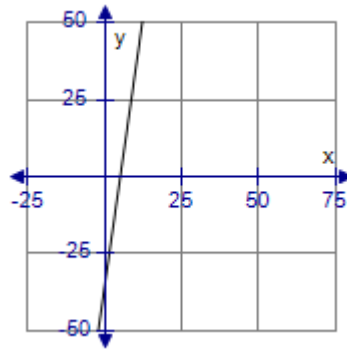
4. Determine the correct sketch of the line through $(3, -14)$ with a slope of 7.

1.4 Lines

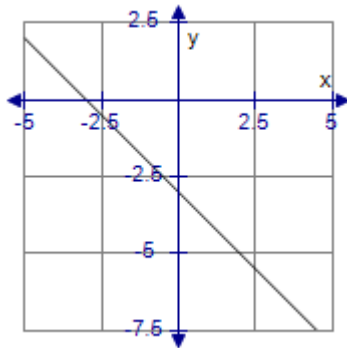
a.



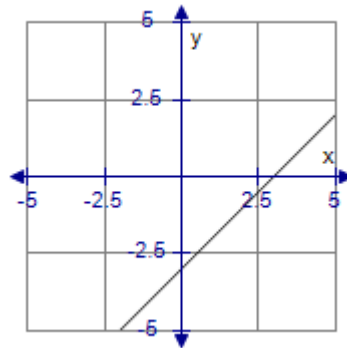
b.



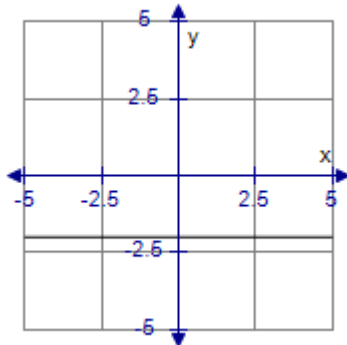
c.



d.



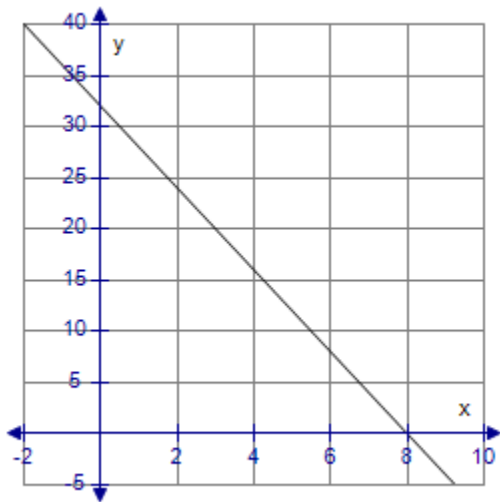
e.



ANSWER: b

5. Determine the correct equation for the line whose graph is sketched below.

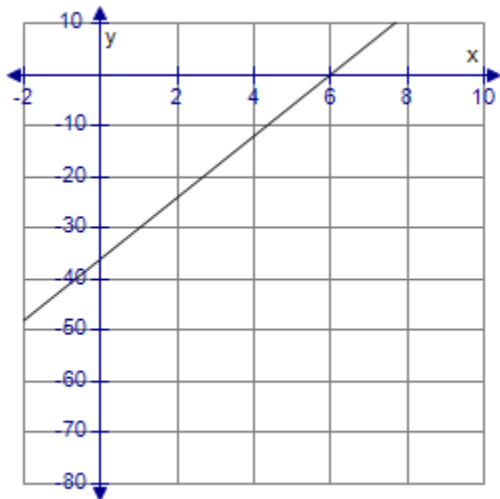
1.4 Lines



- a. $y = -4x - 32$
- b. $y = 4x - 32$
- c. $y = \frac{1}{4}x + 32$
- d. $y = 4x - 32$
- e. $y = -4x + 32$

ANSWER: e

6. Determine the correct equation for the line whose graph is sketched below.



- a. $y = -6x + 36$
- b. $y = 6x - 36$
- c. $y = 6x + 36$

1.4 Lines

d. $y = -\frac{1}{6}x - 36$

e. $y = -6x - 36$

ANSWER: b7. Determine the correct equation for the line passing through the point $(-5, -14)$ with a slope of 3.

a. $y = -3x - 1$

b. $y = -3x + 1$

c. $y = 3x + 1$

d. $y = 3x - 1$

e. $y = \frac{1}{3}x + 1$

ANSWER: c8. Determine the correct equation for the line passing through the point $(1, 8)$ with a slope of 5.

a. $y = -3x - 5$

b. $y = 5x + 3$

c. $y = \frac{1}{3}x + 5$

d. $y = 3x + 5$

e. $y = -5x + 3$

ANSWER: b9. Determine the correct equation for the line passing through the point $(3, 16)$ and the point $(17, 3)$.

a. $14y + 13x - 263 = 0$

b. $14y - 13x - 263 = 0$

c. $14y + 13x + 263 = 0$

d. $14y - 13x + 263 = 0$

e. none of these

ANSWER: a10. Determine the correct equation for the line with a slope of 6 and a y -intercept of -4 .

a. $y = \frac{1}{6} - 4$

b. $y = -6x + 4$

c. $y = -\frac{1}{6} - 4$

d. $y = 6x - 4$

e. $y = 6x + 4$

ANSWER: d

1.4 Lines

11. Determine the correct equation for the line with an x -intercept of -2 and a y -intercept of 8 .

a. $y = -4x + 8$

b. $y = 4x - 8$

c. $y = 4x + 8$

d. $y = \frac{1}{4}x + 8$

e. $y = -\frac{1}{4}x - 8$

ANSWER: c

12. Determine the correct equation for the line passing through the point $(4, -4)$ and parallel to the line $x + 2y = 10$.

a. $y = -\frac{1}{2}x - 2$

b. $y = 2x - 2$

c. $y = -\frac{1}{2}x - 2$

d. $y = \frac{1}{2}x + 2$

e. $y = 2x + 2$

ANSWER: a

13. Find an equation for the line that passes through the point $(6, 3)$ and is perpendicular to the line $x - 3y + 26 = 0$.

a. $y = \frac{1}{3}x - \frac{2}{3}$

b. $y = 3x + 18$

c. $y = 21 - 3x$

d. $y = x + 6$

e. $y = \frac{1}{6}x - 21$

ANSWER: c

14. Write the equation for the line passing through the point $(10, 6)$ which is perpendicular to the line $y = -11$.

a. $y = -10$

b. $y = 11$

c. $x = 9$

d. $y = 12$

e. $x = 10$

1.4 Lines

ANSWER: e

15. Determine the correct equation for the line passing through the point (2, 3) which is parallel to the line passing through both of the points (6, 7) and (-2, 71).

a. $y = -8x - 19$

b. $y = -8x - \frac{1}{19}$

c. $y = -8x + \frac{1}{19}$

d. $y = -8x + 19$

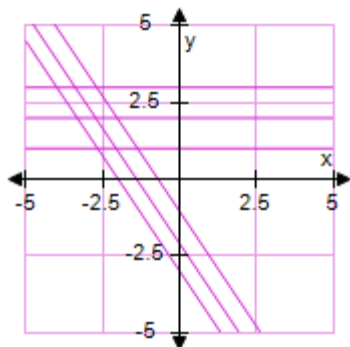
e. $y = 8x + \frac{1}{19}$

ANSWER: d

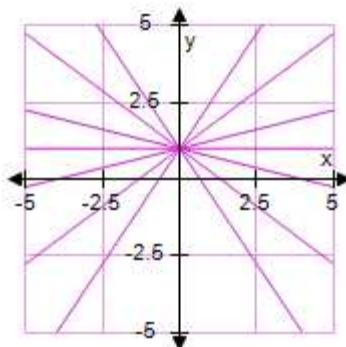
16. Use a graphing device to graph the given family of lines in the same viewing rectangle.

$y = mx + 1$, for $m = 0, \pm 0.25, \pm 0.75, \pm 1.5$

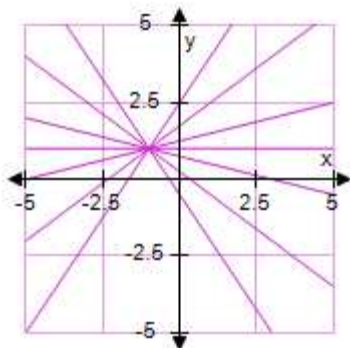
a.



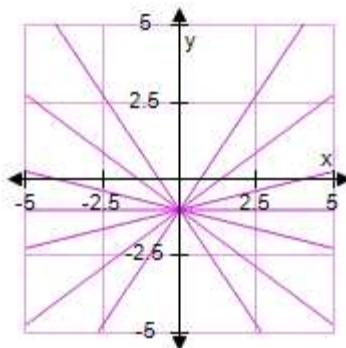
b.



c.

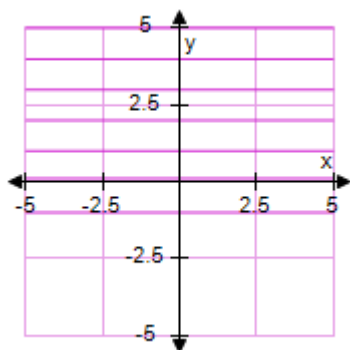


d.



1.4 Lines

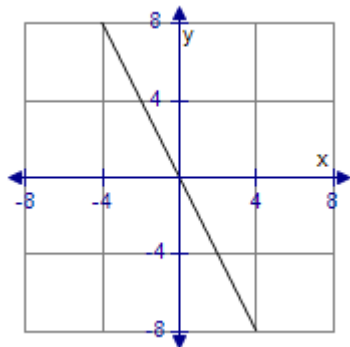
e.



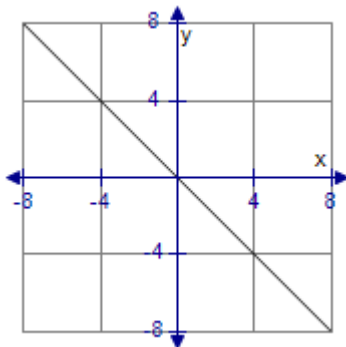
ANSWER: b

17. Find the slope and y-intercept for the line $x + y = 6$ and draw its graph.

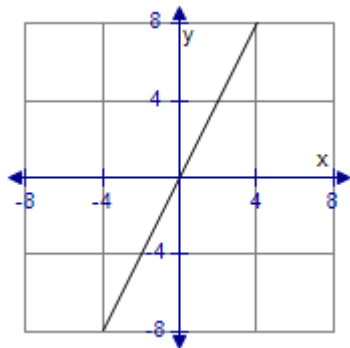
a. $m = -2, y = 0$



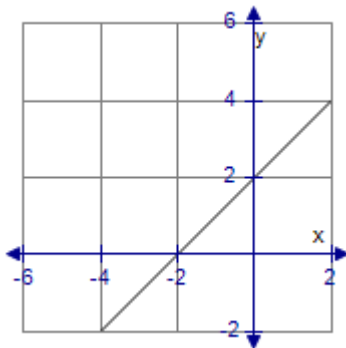
b. $m = -1, y = 0$



c. $m = 2, y = 0$

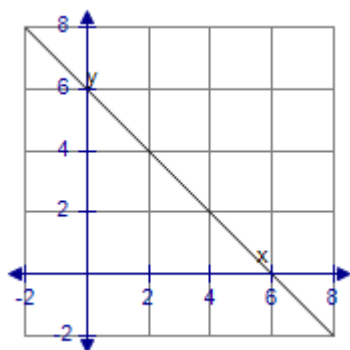


d. $m = 1, y = 6$



e. $m = -1, y = 6$

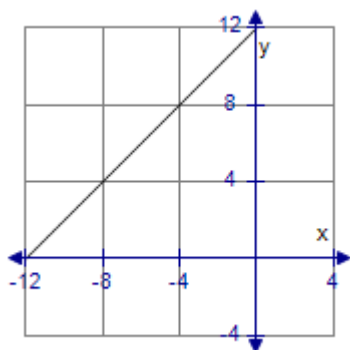
1.4 Lines



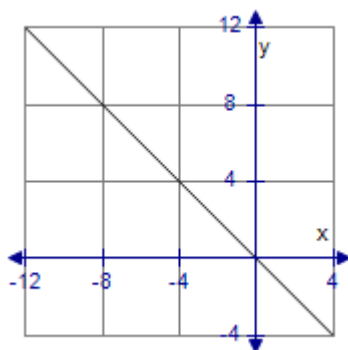
ANSWER: e

18. Find the slope and the y-intercept of the line $\frac{1}{13}x - \frac{1}{12}y + 1 = 0$ and draw its graph.

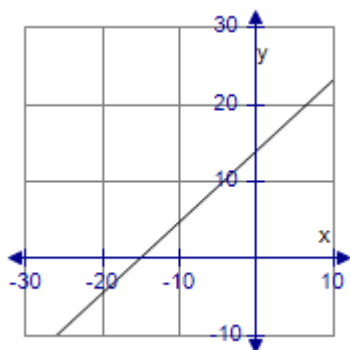
a. $m = 1$, y-intercept = 12



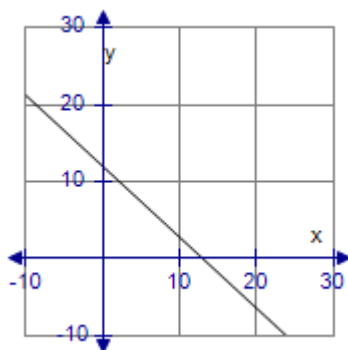
b. $m = -1$, y-intercept = 0



c. $m = \frac{12}{13}$, y-intercept = 14

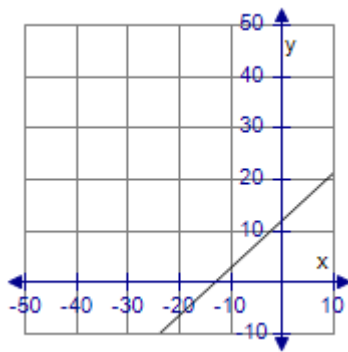


d. $m = -\frac{12}{13}$, y-intercept = 12



e. $m = \frac{12}{13}$, y-intercept = 12

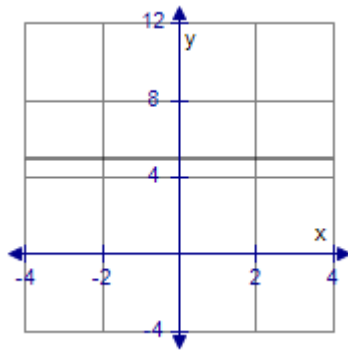
1.4 Lines



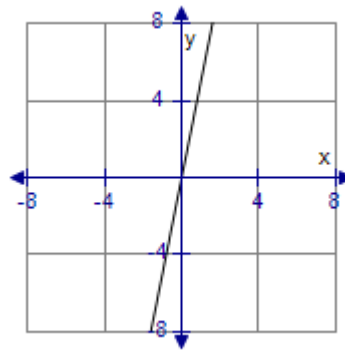
ANSWER: e

19. Find the slope and the y -intercept of the line $7y + 35 = 0$ and sketch its graph.

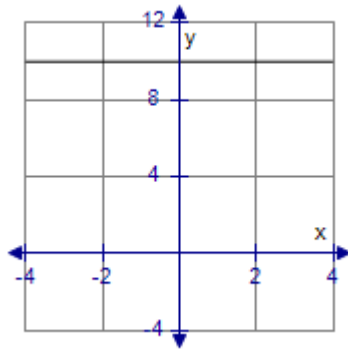
a. $m = 0$, y -intercept is 5



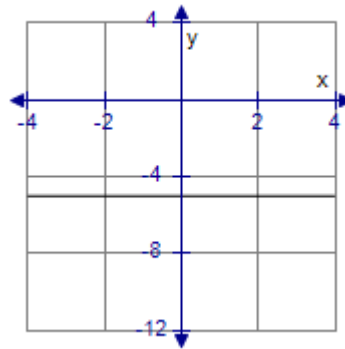
b. $m = 5$, y -intercept is 0



c. $m = 0$, y -intercept is 10

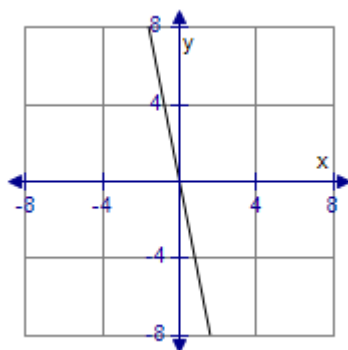


d. $m = 0$, y -intercept is -5



e. $m = -5$, y -intercept is 0

1.4 Lines



ANSWER: d

20. Determine the correct area from the triangle formed by the coordinate axes and the line $10x + 12y - 120 = 0$

- a. $a = 60$
- b. $a = 59$
- c. $a = 61$
- d. $a = 62$
- e. $a = 58$

ANSWER: a

21. The relationship between the Fahrenheit (F) and Celsius (C) temperature scales is given by the equation:

$$F = \frac{9}{5}C + 32.$$

Find the Celsius temperature corresponding to $F = 95^\circ$.

- a. $C = 34^\circ$
- b. $C = 35^\circ$
- c. $C = 37^\circ$
- d. $C = 33^\circ$
- e. $C = 36^\circ$

ANSWER: b

22. At the surface of the ocean, the water pressure is the same as the air pressure above the water, 4.48 lb/in.^2 . Below the surface, the water pressure increases by 21 lb/in.^2 for every 10 feet of descent.

Determine the correct equation for the relationship between pressure (P) and depth (d) below the ocean surface where pressure is in lb/in.^2 and depth is in feet.

- a. $P = 0.448d + 21$
- b. $P = 0.348d - 21$
- c. $P = 0.348d + 21$
- d. $P = -0.448d - 21$

1.4 Lines

e. $P = -0.448d + 21$

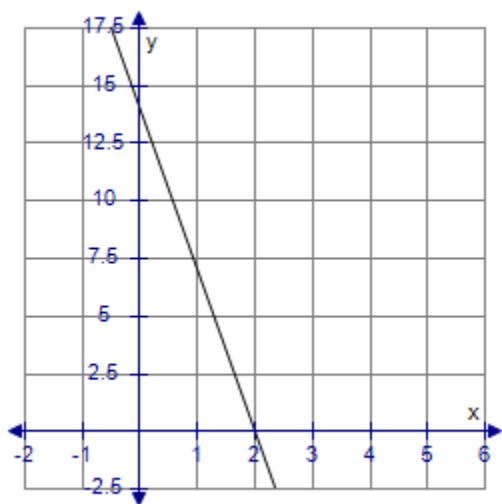
ANSWER: a

23. Find the slope of the line through $P(6, -1)$ and $Q(7, 1)$.

$m =$ _____

ANSWER: 2

24. Find the slope of the line sketched in the graph.



$m =$ _____

ANSWER: -7

25. Find the area of the triangle formed by the coordinate axes and the line $4x + 6y - 24 = 0$.

ANSWER: 12

26. Find the slope and the y-intercept of the line $\frac{1}{4}x - \frac{1}{3}y + 4 = 0$

slope = _____

y-intercept = _____

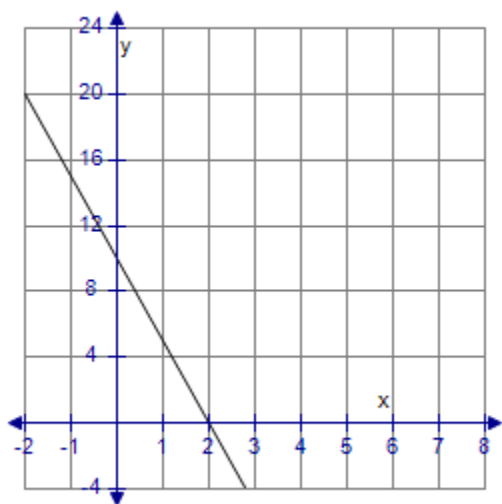
ANSWER: $\frac{3}{4}$; 12

27. Find the slope and the y-intercept of the line $3y + 3 = 0$.

ANSWER: 0; -1

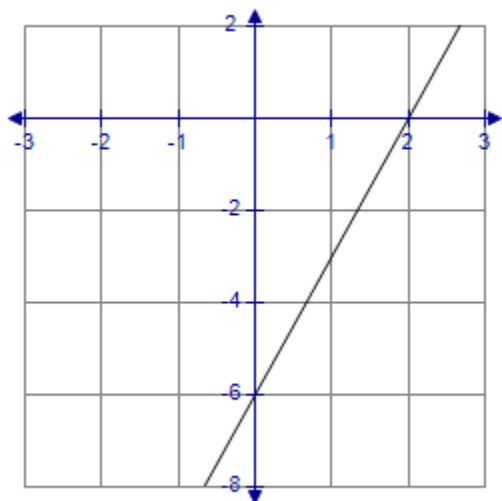
28. Find an equation for the line whose graph is sketched below.

1.4 Lines



ANSWER: $y = -5x + 10$

29. Find an equation for the line whose graph is sketched below.



ANSWER: $y = 3x - 6$

30. Write an equation for the line through the point $(-6, -33)$ which has a slope of 7.

ANSWER: $y = 7x + 9$

31. Write an equation for the line passing through the point $(-1, 2)$ and the point $(3, -4)$.

ANSWER: $3x + 2y - 1 = 0$

32. Write an equation for the line with a slope of 3 and a y -intercept of -4 .

ANSWER: $y = 3x - 4$

33. Write an equation for the line with an x -intercept of -2 and a y -intercept of 16.

1.4 Lines

ANSWER: $y = 8x + 16$

34. Write the equation for the line passing through the point $(20, -12)$ and parallel to the line $x + 4y = 12$.

ANSWER: $y = -\frac{1}{4}x - 7$

35. Write the equation for the line passing through the point $(7, 7)$ which is perpendicular to the line $y = 9$.

ANSWER: $x = 7$

36. Write the equation for the line passing through the point $(4, 10)$ which is parallel to the line passing through both of the points $(5, 2)$ and $(-4, 65)$.

ANSWER: $y = -7x + 38$

37. At the surface of the ocean, the water pressure is the same as the air pressure above the water, 11 lb/in.^2 . Below the surface, the water pressure increases by 4.12 lb/in.^2 for every 10 feet of descent.

Find an equation for the relationship between pressure (P) and depth (d) below the ocean surface where pressure is in lb/in.^2 and depth is in feet.

ANSWER: $P = 0.412d + 11$

Find the slope of the line through P and Q by matching each value of P and Q below with the corresponding slope.

Match each slope below with the letter of the corresponding coordinates.

a. $P(-6, -7)$ and $Q(-1, -12)$

b. $P(-4, -6)$ and $Q(-2, -2)$

c. $P(-7, -8)$ and $Q(0, -36)$

d. $P(-5, -5)$ and $Q(-1, 11)$

38. $m = -1$

ANSWER: a

39. $m = 4$

ANSWER: d

40. $m = -4$

ANSWER: c

41. $m = 2$

ANSWER: b

Match each equation below with the letter of the corresponding description.

a. The line is through point $(0, 2)$ with a slope of 7.

b. The line is through point $(-1, 11)$ with a slope of -7.

c. The line is through point $(4, 32)$ with a slope of 9.

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1.4 Lines

d. The line is through point (1, -9) with a slope of -6.

42. $y = -7x + 4$

ANSWER: b

43. $y = -6x - 3$

ANSWER: d

44. $y = 7x + 2$

ANSWER: a

45. $y = 9x - 4$

ANSWER: c

1.5 Solving Quadratic Equations

1. Solve the equation.

$$(t - 5)^2 = (t + 5)^2 + 40$$

- a. - 5
- b. 5
- c. - 8
- d. 2
- e. - 2

ANSWER: e

2. Find all real solutions of the equation $x^2 - 81 = 0$.

- a. $x = 9, x = - 9$
- b. $x = 40.5, x = - 40.5$
- c. $x = 9, x = - 81$
- d. $x = 81, x = - 9$
- e. $x = 81, x = - 81$

ANSWER: a

3. Find all real solutions of the equation $10x^2 - 160 = 0$.

- a. $x = 8, x = - 8$
- b. $x = \sqrt{160}, x = -\sqrt{160}$
- c. $x = 16, x = - 16$
- d. $x = 10, x = - 10$
- e. $x = 4, x = - 4$

ANSWER: e

4. Find all real solutions of the equation $(x + 9)^2 = 4$.

- a. $x = - 7, x = - 11$
- b. $x = 2, x = - 2$
- c. $x = 7, x = 11$
- d. $x = - 2, x = - 2$
- e. $x = - 11, x = 11$

ANSWER: a

5. Solve the equation.

$$(t - 4)^2 = (t + 4)^2 + 80$$

ANSWER: -5

6. Find all real solutions of the equation.

1.5 Solving Quadratic Equations

$$x^2 - 64 = 0$$

ANSWER: 8; -8

7. Find all real solutions of the equation.

$$7x^2 - 7 = 0$$

ANSWER: 1; -1

8. Find all real solutions of the equation.

$$(x + 4)^2 = 4$$

ANSWER: -2; -6

9. Solve the equation by factoring.

$$6w^2 = 11w - 3$$

a. $w = \frac{3}{2}$, $w = \frac{1}{3}$

b. $w = \frac{3}{2}$, $w = \frac{3}{5}$

c. $w = \frac{1}{5}$, $w = \frac{1}{3}$

d. $w = \frac{3}{11}$, $w = \frac{3}{2}$

e. none of these

ANSWER: a

10. Solve the equation by factoring.

$$x^2 = 5(x + 210)$$

a. $x = -35$, $x = -30$

b. $x = 35$, $x = -30$

c. $x = 35$, $x = 30$

d. $x = -35$, $x = -60$

e. none of these

ANSWER: b

11. Solve the equation by completing the square.

$$x^2 - 6x - 7 = 0$$

a. $x = 7$, $x = 1$

b. $x = -7$, $x = -2$

1.5 Solving Quadratic Equations

c. $x = -7, x = -1$

d. $x = 7, x = -1$

e. none of these

ANSWER: d

12. Solve the equation by completing the square.

$$x^2 + 13x + 40 = 0$$

a. $x = -8, x = 5$

b. $x = 8, x = -5$

c. $x = 8, x = 5$

d. $x = -8, x = -5$

e. none of these

ANSWER: d

13. Solve the equation by completing the square.

$$x^2 = \frac{7}{8}x - \frac{3}{16}$$

a. $x = \frac{8}{3}, \frac{1}{2}$

b. $x = 24, 2$

c. $x = \frac{3}{8}, \frac{1}{2}$

d. $x = \frac{3}{8}, -\frac{1}{2}$

e. none of these

ANSWER: c

14. Find all real solutions of the equation.

$$4x^2 + 7x - 36 = 0$$

a. $x = \frac{9}{4}, x = -4$

b. $x = -\frac{9}{4}, x = 4$

c. $x = \frac{11}{4}, x = -9$

d. $x = -\frac{9}{4}, x = -4$

1.5 Solving Quadratic Equations

e. none of these

ANSWER: a

15. Find all real solutions of the equation.

$$\theta^2 - \frac{9}{8}\theta + \frac{81}{256} = 0$$

a. $\theta = -\frac{9}{8}$

b. $\theta = \frac{9}{16}$

c. $\theta = \frac{9}{16}, \theta = -\frac{9}{8}$

d. $\theta = \frac{9}{16}, \theta = -\frac{9}{16}$

e. none of these

ANSWER: b

16. Find all real solutions of the equation.

$$x^2 - \sqrt{85}x + 9 = 0$$

a. $x = \frac{\sqrt{85}-7}{2}, x = \frac{\sqrt{85}+7}{2}$

b. $x = -\frac{\sqrt{85}-7}{2}, x = \frac{\sqrt{85}+7}{2}$

c. $x = \frac{\sqrt{85}-7}{2}, x = -\frac{\sqrt{85}+7}{2}$

d. $x = -\frac{\sqrt{85}-7}{2}, x = -\frac{\sqrt{85}+7}{2}$

e. None of these

ANSWER: a

17. Find all real solutions of the equation

$$ax^2 - (2a+1)x + (a+1) = 0, \text{ for } a = 5.$$

a. $x = \frac{6}{5}, x = 1$

1.5 Solving Quadratic Equations

b. $x = \frac{6}{5}, x = -1$

c. $x = -\frac{6}{5}, x = -1$

d. $x = -\frac{6}{5}, x = 1$

e. none of these

ANSWER: a

18. Use the quadratic formula and a calculator to find all real solutions of the equation, correct to three decimal places.

$$x^2 - 2.467x - 2.723 = 0$$

a. $x = 0.827, x = 3.294$

b. $x = -0.827, x = -3.294$

c. $x = -0.827, x = 3.294$

d. $x = 0.827, x = -3.294$

e. none of these

ANSWER: c

19. Use the discriminant to determine the number of real solutions of the equation.

$$x^2 - 5.17x + 3.29 = 0$$

Do not solve the equation.

a. no real solutions

b. exactly one real solution

c. two real solutions

d. more than two real solutions

e. none of these

ANSWER: c

20. Find all values of k that ensure that the equation has exactly one solution.

$$4x^2 + kx + 4 = 0$$

a. $k = 16, k = -16$

b. $k = 8, k = -8$

c. $k = 8, k < -8$

d. $k = -8, k > 8$

e. none of these

ANSWER: b

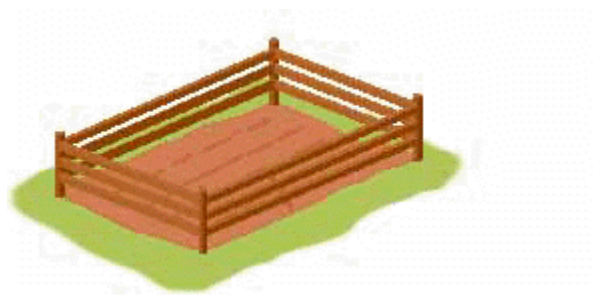
21. Find two numbers whose sum is 37 and whose product is 322.

1.5 Solving Quadratic Equations

- a. 14, 23
- b. 13, 24
- c. 14, 18
- d. 15, 22
- e. none of these

ANSWER: a

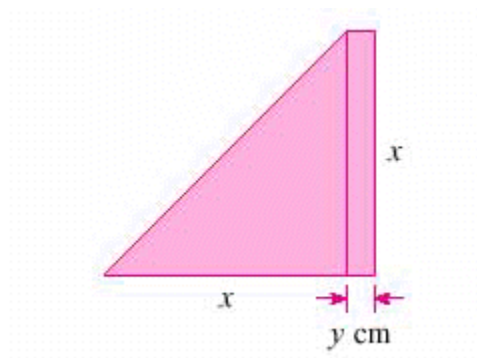
22. A farmer has a rectangular garden plot surrounded by 220 feet of fence. Find the length and width of the garden if its area is 2,800 feet².



- a. width = 60, length = 50
- b. width = 70, length = 40
- c. width = 60, length = 30
- d. width = 65, length = 45
- e. none of these

ANSWER: b

23. Find the length x if the shaded area is 3,000 cm² and $y = 20$ cm.

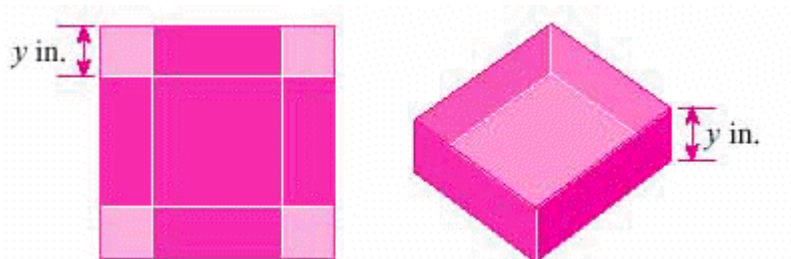


- a. 70 cm
- b. 80 cm
- c. 60 cm
- d. 50 cm
- e. none of these

ANSWER: c

1.5 Solving Quadratic Equations

24. A box with a square base and no top is to be made from a square piece of cardboard by cutting y in. squares from each corner and folding up the sides, as shown in the figure. The box is to hold 484 in^3 . What is the length of the starting piece of cardboard, if $y = 4$ in?



- a. 24 in
- b. 21 in
- c. 19 in
- d. 18 in
- e. none of these

ANSWER: c

25. A wire 210 in. long is cut into two pieces. One piece is formed into a square and the other into a circle. If the two figures have the same area, what are the lengths of the two pieces of wire to the nearest tenth of an inch?

- a. 66.8 in. and 143.2 in.
- b. 170.5 in. and 39.5 in.
- c. 111.3 in. and 98.7 in.
- d. 115.5 in. and 94.5 in.
- e. none of these

ANSWER: c

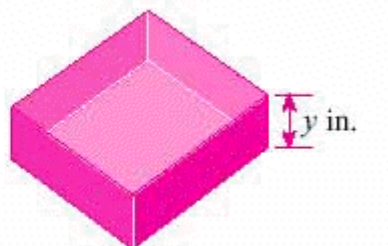
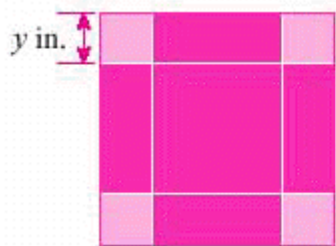
26. It took a crew 4 h 48 min to row 4.4 km upstream and back again. If the rate of flow of the stream was 5 km/h, what was the rowing rate of the crew in still water?

- a. 9 km/h
- b. 6 km/h
- c. 10 km/h
- d. 8 km/h
- e. none of these

ANSWER: b

27. A box with a square base and no top is to be made from a square piece of cardboard by cutting y inch squares from each corner and folding up the sides, as shown in the figure. The box is to hold 245 in^3 . How big a piece of cardboard is needed if $y = 5$ inches?

1.5 Solving Quadratic Equations



Give the length (in inches) of the starting piece of cardboard.

_____ inches

ANSWER: 17

28. Use the discriminant to determine the number of real solutions of the equation. Do not solve the equation.

$$x^2 - 5.15x + 3.39 = 0$$

ANSWER: 2

29. It took a crew 4 h 48 min to row 10.8 km upstream and back again. If the rate of flow of the stream was 3 km/h, what was the rowing rate of the crew in still water?

_____ km/h

ANSWER: 6

30. Solve the equation by factoring.

$$6w^2 = 7w - 2$$

ANSWER: $w = \frac{1}{2}, w = \frac{2}{3}$

31. Solve the equation by factoring.

$$x^2 = 3(x + 126)$$

ANSWER: $x = 21, x = -18$

32. Solve the equation by completing the square.

$$x^2 - 6x - 27 = 0$$

ANSWER: $x = 9, x = -3$

33. Solve the equation by completing the square.

$$x^2 + 12x + 32 = 0$$

ANSWER: $x = -8, x = -4$

34. Solve the equation by completing the square.

1.5 Solving Quadratic Equations

$$x^2 = \frac{7}{8}x - \frac{5}{32}$$

ANSWER: $x = \frac{5}{8}, x = \frac{1}{4}$

35. Find all real solutions of the equation.

$$4x^2 + 19x - 30 = 0$$

ANSWER: $x = \frac{5}{4}, x = -6$

36. Find all real solutions of the equation.

$$\theta^2 - \frac{6}{5}\theta + \frac{9}{25} = 0$$

ANSWER: $\theta = \frac{3}{5}$

37. Find all real solutions of the equation.

$$x^2 - \sqrt{61}x + 9 = 0$$

ANSWER: $x = \frac{(\sqrt{61} - 5)}{2}, x = \frac{(\sqrt{61} + 5)}{2}$

38. Use the quadratic formula and a calculator to find all real solutions of the equation, correct to three decimal places.

$$x^2 - 4.207x - 2.498 = 0$$

ANSWER: $x = -0.528, x = 4.735$

39. Find all values of k that ensure that the equation has exactly one solution.

$$16x^2 + kx + 4 = 0$$

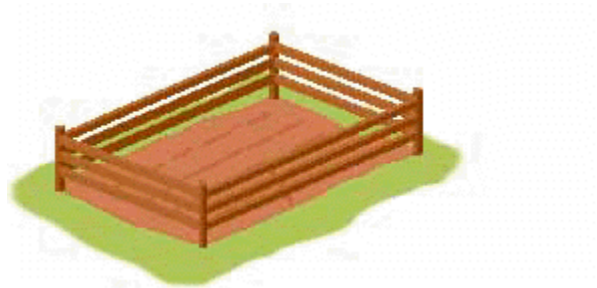
ANSWER: $k = 16, k = -16$

40. Find two numbers whose sum is 31 and whose product is 238.

ANSWER: 14, 17

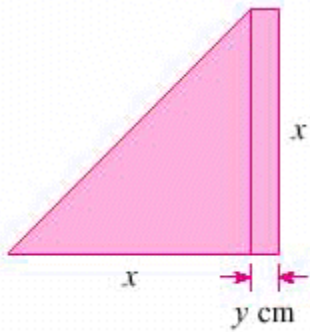
41. A farmer has a rectangular garden plot surrounded by 260 feet of fence. Find the length and width of the garden if its area is 3,000 feet².

1.5 Solving Quadratic Equations



ANSWER: 100, 30

42. Find the length x if the shaded area is $6,300 \text{ cm}^2$ and $y = 13 \text{ cm}$.



ANSWER: $x=100$

43. A wire 400 in. long is cut into two pieces. One piece is formed into a square and the other into a circle. If the two figures have the same area, what are the lengths of the two pieces of wire to the nearest tenth of an inch?

ANSWER: 212.1, 187.9

1.6 Complex Numbers

1. Find the real and imaginary part of the complex number $3 - 5i$.

- a. Real part = 3, Imaginary part = -5 .
- b. Real part = 3, Imaginary part = $-5i$.
- c. Real part = -5 , Imaginary part = 3.
- d. Real part = $5i$, Imaginary part = 3.
- e. none of these

ANSWER: a

2. Find the real and imaginary parts of the complex number.

8

- a. Real part 8, imaginary part 8
- b. Real part 0, imaginary part 8
- c. Real part 8, imaginary part 0

ANSWER: c

3. Find the real and imaginary part of the complex number $\sqrt{12} + \sqrt{-7}$.

- a. Real part = $\sqrt{-12}$, Imaginary part = $\sqrt{-7}$
- b. Real part = $\sqrt{12}$, Imaginary part = $\sqrt{7}$
- c. Real part = $\sqrt{7}$, Imaginary part = $\sqrt{12}$
- d. Real part = 12, Imaginary part = -7
- e. none of these

ANSWER: b

4. Evaluate the expression

$$(11 + 14i) + (16 - 2i)$$

and write the result in the form $a + bi$.

- a. $27 - 12i$
- b. $27 + 12i$
- c. $12 + 27i$
- d. $11 + 14i$
- e. none of these

ANSWER: b

5. Evaluate the expression $2(-3 + 8i)$ and write the result in the form $a + bi$.

- a. $-6 + 16i$
- b. $6 - 16i$
- c. $-16 - 6i$
- d. $-16 + 6i$

1.6 Complex Numbers

e. none of these

ANSWER: a

6. Evaluate the expression $(4 + 4i)(11 - 10i)$ and write the result in the form $a + bi$.

a. $-4 - 84i$

b. $84 + 4i$

c. $4 + 84i$

d. $44 + 44i$

e. none of these

ANSWER: b

7. Evaluate the expression $\frac{25 - 10i}{1 - 2i}$ and write the result in the form $a + bi$.

a. $9 + 8i$

b. $-8 - 9i$

c. $9 - 2i$

d. $8 + 9i$

e. none of these

ANSWER: a

8. Evaluate the expression $\frac{40}{6 - 2i}$ and write the result in the form $a + bi$.

a. $6 + 2i$

b. $-2 - 6i$

c. $6 - 2i$

d. $2 + 6i$

e. none of these

ANSWER: a

9. Evaluate the expression $\frac{12 + 54i}{6i}$ and write the result in the form $a + bi$.

a. $54 - 12i$

b. $9 - 2i$

c. $-9 + 2i$

d. $2 - 9i$

e. none of these

ANSWER: b

10. Evaluate the expression $\frac{130}{5 + i} - \frac{26}{5 - i}$ and write the result in the form $a + bi$.

1.6 Complex Numbers

- a. $-6 - 20i$
- b. $20 - 6i$
- c. $20 + 6i$
- d. $6 - 20i$
- e. none of these

ANSWER: b

11. Evaluate the expression i^7 and write the result in the form $a + bi$.

- a. $-i$
- b. $-(-i)$
- c. 1
- d. -1
- e. none of these

ANSWER: a

12. Evaluate the expression i^{52} and write the result in the form $a + bi$.

- a. $-(1)$
- b. $-i$
- c. 1
- d. i
- e. none of these

ANSWER: c

13. Evaluate the expression $\sqrt{-36}$ and write the result in the form $a + bi$.

- a. $6i$
- b. -6
- c. $-6i$
- d. 6
- e. none of these

ANSWER: a

14. Evaluate the expression $\sqrt{-64}\sqrt{-16}$ and write the result in the form $a + bi$.

- a. -32
- b. $32i$
- c. $-32i$
- d. 32
- e. none of these

ANSWER: a

1.6 Complex Numbers

15. Evaluate the expression $(3 + \sqrt{-64})(12 - \sqrt{-4})$ and write the result in the form $a + bi$.

- a. $52 + 90i$
- b. $-16 + 90i$
- c. $90 - 52i$
- d. $36 + 96i$
- e. none of these

ANSWER: a

16. Evaluate the expression $\frac{\sqrt{-441}}{\sqrt{-7}\sqrt{-9}}$ and write the result in the form $a + bi$.

- a. $-\sqrt{7}$
- b. $-7i$
- c. $-i\sqrt{7}$
- d. $i\sqrt{7}$
- e. none of these

ANSWER: c

17. Find all solutions of the equation $x^2 + 25 = 0$ and express them in the form $a + bi$.

- a. $x = 5i, x = -5$
- b. $x = 5, x = -5$
- c. $x = 5i, x = -5i$
- d. $x = 5i$
- e. none of these

ANSWER: c

18. Find all solutions of the equation $x^2 - 8x + 20 = 0$ and express them in the form $a + bi$.

- a. $x = 4 + 2i, x = 4 - 2i$
- b. $x = 2 + 5i, x = 2 - 5i$
- c. $x = 4, x = -4$
- d. $x = 16 + 8i, x = 16 - 8i$
- e. No solutions

ANSWER: a

19. Find all solutions of the equation $3x^2 - 18x + 39 = 0$ and express them in the form $a + bi$.

- a. $x = 12 + 8i, x = 12 - 8i$
- b. $x = 3 + 2i, x = 3 - 2i$

1.6 Complex Numbers

c. $x = 3, x = -3$

d. $x = 2 + 4i, x = 2 - 4i$

e. No solutions

ANSWER: b

20. Find all solutions of the equation $z + 4 + \frac{13}{z} = 0$ and express them in the form $a + bi$.

a. $z = -8 + 12i, z = -8 - 12i$

b. $z = 3 + 3i, z = 3 - 3i$

c. $z = -2 + 3i, z = -2 - 3i$

d. $z = 2, z = -2$

e. No solutions

ANSWER: c

21. Evaluate the expression i^{78} and write the result in the form $a + bi$.

ANSWER: -1

22. Evaluate the expression $\sqrt{-81}\sqrt{-49}$ and write the result in the form $a + bi$.

ANSWER: -63

23. Evaluate the expression and write the result in the form $a + bi$.

$$\frac{5 + \sqrt{-75}}{1 + \sqrt{-3}}$$

ANSWER: 5

24. Perform the subtraction and write the result in the form $a + bi$.

$$\left(4 + \frac{3}{2}i\right) - \left(3 + \frac{9}{2}i\right)$$

ANSWER: $1 - 3i$

25. Perform the subtraction and write the result in the form $a + bi$.

$$(0.3 - 1.5i) - (1.2 - 3.6i)$$

ANSWER: $-0.9 + 2.1i$

26. Evaluate the expression $(6 + 19i) + (13 - 12i)$ and write the result in the form $a + bi$.

ANSWER: $19 + 7 \cdot i$

27. Evaluate the expression $15(-5 + 11i)$ and write the result in the form $a + bi$.

ANSWER: $-75 + 165 \cdot i$

28. Evaluate the expression $(7 + 5i)(4 - 2i)$ and write the result in the form $a + bi$.

1.6 Complex Numbers**ANSWER:** $38 + 6 \cdot i$

29. Evaluate the expression $\frac{125 - 50i}{3 - 4i}$ and write the result in the form $a + bi$. Round a and b to the nearest whole number, if necessary.

ANSWER: $23 + 14 \cdot i$

30. Evaluate the expression $\frac{106}{9 - 5i}$ and write the result in the form $a + bi$.

ANSWER: $9 + 5 \cdot i$

31. Evaluate the expression and write the result in the form $a + bi$.

$$\left(\frac{2}{3} + 24i \right) \left(\frac{1}{6} + 12i \right)$$

ANSWER: $-\frac{2,591}{9} + 12i$

32. Evaluate the expression and write the result in the form $a + bi$.

$$(5 - 4i)^{-1}$$

ANSWER: $\frac{5}{41} + \frac{4}{41} \cdot i$

33. Evaluate the expression $\frac{36 + 32i}{4i}$ and write the result in the form $a + bi$.

ANSWER: $8 - 9i$

34. Evaluate the expression and write the result in the form $a + bi$.

$$\frac{(1 + 4i)(3 - i)}{2 + i}$$

ANSWER: $5 + 3i$

35. Evaluate the expression $\frac{70}{3 + i} - \frac{60}{3 - i}$ and write the result in the form $a + bi$.

ANSWER: $3 - 13 \cdot i$

36. Evaluate the expression i^{27} and write the result in the form $a + bi$.

ANSWER: $-i$

37. Evaluate the expression $\sqrt{-9}$ and write the result in the form $a + bi$.

ANSWER: $3 \cdot i$

1.6 Complex Numbers

38. Evaluate the expression $(10 + \sqrt{-25})(7 - \sqrt{-4})$ and write the result in the form $a + bi$.

ANSWER: $80 + 15 \cdot i$

39. Evaluate the expression $\frac{\sqrt{-1,764}}{\sqrt{-7}\sqrt{-36}}$ and write the result in the form $a + bi$.

ANSWER: $-i \cdot \sqrt{7}$

40. Find all solutions of the equation $x^2 + 1 = 0$ and express them in the form $a + bi$.

ANSWER: $i, -i$

41. Find all solutions of the equation $x^2 - 8x + 17 = 0$ and express them in the form $a + bi$.

ANSWER: $4 + i, 4 - i$

42. Find all solutions of the equation $2x^2 - 8x + 40 = 0$ and express them in the form $a + bi$.

ANSWER: $2 + 4i, 2 - 4i$

43. Find all solutions of the equation $z + 6 + \frac{10}{z} = 0$ and express them in the form $a + bi$.

ANSWER: $-3 + i, -3 - i$

44. Find all solutions of the equation and express them in the form $a + bi$.

$$25x^2 + 16 = 0$$

ANSWER: $x = -\frac{4}{5} \cdot i, \frac{4}{5} \cdot i$

45. Find all solutions of the equation and express them in the form $a + bi$.

$$2x^2 + 4 = 2x$$

ANSWER: $x = \frac{1}{2} \pm \frac{\sqrt{7}}{2} \cdot i$

46. Find all solutions of the equation and express them in the form $a + bi$.

$$z + 8 + \frac{96}{z} = 0$$

ANSWER: $z = -4 \pm 4\sqrt{5} \cdot i$

47. Find all solutions of the equation and express them in the form $a + bi$.

$$\frac{1}{2}x^2 - 5x + 25 = 0$$

1.6 Complex Numbers

ANSWER: $x = 5 \pm 5i$

Find the real and imaginary part of the complex number $4 - 2i$. Match each lettered word with the corresponding number below.

Choose the correct letter for the numbered questions below.

- a. Real part
- b. Imaginary part

48. 4

ANSWER: a

49. -2

ANSWER: b

Find the real and imaginary part of the complex number $\sqrt{11} + \sqrt{-10}$. Match each lettered word with the corresponding number below.

Choose the correct letter for the numbered questions below.

- a. Real part
- b. Imaginary part

50. $\sqrt{10}$

ANSWER: b

51. $\sqrt{11}$

ANSWER: a

1.7 Solving Other Types of Equations

1. Determine whether the given value is a solution of the equation.

$$\frac{1}{x} - \frac{1}{x-6} = 2, x = 6$$

- a. no
- b. yes

ANSWER: a

2. Determine whether the given value is a solution of the equation.

$$\frac{x-a}{x-d} = \frac{a}{d} \quad (d \neq 0), x = 0$$

- a. no
- b. yes

ANSWER: b

3. Solve the equation.

$$2x - 1 = 3x + 6$$

- a. 5
- b. 6
- c. - 7
- d. - 5
- e. 7

ANSWER: c

4. Solve the equation.

$$-7w + 16 = -15w$$

- a. 2
- b. 3
- c. - 2
- d. 16
- e. - 3

ANSWER: c

5. Solve the equation.

$$\frac{z}{7} = \frac{4}{35}z + 10$$

- a. 4
- b. 350
- c. - 50

1.7 Solving Other Types of Equations

d. 70

e. 10

ANSWER: b

6. Solve the equation.

$$4(x + 6) + 1 = -5(x + 6) + 10$$

a. 9

b. - 5

c. - 11

d. 4

e. 5

ANSWER: b

7. Solve the equation.

$$\frac{1}{x} = \frac{14}{9x} + 5$$

a. $\frac{1}{5}$

b. - 14

c. $-\frac{1}{9}$

d. $\frac{1}{9}$

e. 9

ANSWER: c

8. Solve the equation.

$$\sqrt{6x} + \sqrt{24} = \frac{5x + 4}{\sqrt{6}}$$

a. 8

b. - 24

c. - 12

d. - 8

e. 24

ANSWER: d

9. Solve the equation.

1.7 Solving Other Types of Equations

$$\frac{9}{x-10} + \frac{2}{x+10} = \frac{81}{x^2-100}$$

- a. - 10
- b. 9
- c. 1
- d. 100
- e. 10

ANSWER: c

10. Solve the equation.

$$x - \frac{1}{9}x - \frac{1}{12}x - \frac{522}{108} = 0$$

- a. - 6
- b. - 9
- c. 9
- d. 6
- e. 7

ANSWER: d

11. Solve the equation.

$$\frac{u}{u - \frac{7u-9}{8}} = 9$$

- a. 80
- b. - 81
- c. 81
- d. 72
- e. - 72

ANSWER: b

12. Solve the equation.

$$\frac{1}{x} - \frac{9}{6x+43} = \frac{1}{6x^2+43x}$$

- a. 13
- b. 14
- c. 18
- d. 15
- e. 3

1.7 Solving Other Types of Equations

ANSWER: b

13. Find all real solutions of the equation $(x - 5)^3 + 64 = 0$.

- a. $x = -5$
- b. $x = -4$
- c. $x = 9$
- d. $x = -1$
- e. $x = 1$

ANSWER: e

14. Find all real solutions of the equation $\sqrt[3]{x} = 4$.

- a. $x = -64, x = 64$
- b. $x = \sqrt[3]{4}$
- c. $x = 64$
- d. $x = 12$
- e. $x = -4$

ANSWER: c

15. Find all real solutions of the equation $4x^{2/3} - 16 = 0$.

- a. $x = 8, x = -8$
- b. $x = 6, x = 4$
- c. $x = 4$
- d. $x = 6$
- e. $x = 8$

ANSWER: a

16. Find the solution of the equation $8.75 - x = 8.41x + 6.39$. Round your answer to two decimal places.

- a. 2.91
- b. 1.27
- c. 0.73
- d. 0.25
- e. 1.91

ANSWER: d

17. Solve the equation $P = 8l + 5w$ for l .

- a. $l = \frac{P + 8w}{5}$
- b. $l = -\frac{P + 5w}{8}$

1.7 Solving Other Types of Equations

c. $l = \frac{P + 5w}{8}$

d. $l = \frac{P - 5w}{8}$

e. $l = \frac{P - 8w}{5}$

ANSWER: d

18. Solve the equation.

$$8x - 8 = 9x + 1$$

ANSWER: -9

19. Solve the equation.

$$-6w + 36 = -12w$$

ANSWER: -6

20. Solve the equation.

$$\frac{z}{3} = \frac{6}{21}z + 3$$

ANSWER: 63

21. Solve the equation.

$$2(x + 7) + 2 = -5(x + 3) + 3$$

ANSWER: -4

22. Solve the equation.

$$(t - 4)^2 = (t + 4)^2 + 80$$

ANSWER: -5

23. Solve the equation.

$$\sqrt{3}x + \sqrt{3} = \frac{2x + 9}{\sqrt{3}}$$

ANSWER: 6

24. Solve the equation.

$$\frac{2}{x - 4} + \frac{1}{x + 4} = \frac{22}{x^2 - 16}$$

ANSWER: 6

25. Solve the equation.

1.7 Solving Other Types of Equations

$$x - \frac{1}{12}x - \frac{1}{11}x - \frac{545}{132} = 0$$

ANSWER: 5

26. Solve the equation.

$$\frac{u}{u - \frac{2u-3}{3}} = 4$$

ANSWER: -12

27. Solve the equation.

$$\frac{1}{x} - \frac{9}{8x+16} = \frac{1}{8x^2+16x}$$

ANSWER: 15

28. Find all real solutions of the equation.

$$(x-2)^3 + 125 = 0$$

ANSWER: -3

29. Find all real solutions of the equation.

$$\sqrt[3]{x} = 4$$

ANSWER: 64

30. Find the solution of the equation. Round your answer to two decimal places.

$$3.61 - x = 5.48x + 6.19$$

ANSWER: -0.40

31. Determine whether the given value is a solution of the equation. Answer *yes* or *no*.

$$\frac{1}{x} - \frac{1}{x-4} = \frac{1}{4}, x = 4$$

ANSWER: no

32. Determine whether the given value is a solution of the equation. Answer *yes* or *no*.

$$\frac{x-c}{x-m} = \frac{c}{m} \quad (m \neq 0), \quad x = m$$

ANSWER: no

33. Solve the equation.

$$\frac{1}{x} = \frac{12}{3x} + 9$$

1.7 Solving Other Types of Equations

ANSWER: $-\frac{1}{3}$

34. Find all real solutions of the equation.

$$2x^{2/3} - 50 = 0$$

ANSWER: 125, -125,

For the equation $P = 7l + 2w$, match each indicated variable below with the corresponding solution when you solve the equation for that variable.

Choose the correct letter for the numbered questions below.

a. l

b. w

35. $\frac{P - 7l}{2}$

ANSWER: b

36. $\frac{P - 2w}{7}$

ANSWER: a

37. Find all real solutions of the equation.

$$x^3 - 5x^2 + 4x = 0$$

a. 0, 6, 7

b. 1, 4

c. 6, 7

d. 0, 6, 4

e. 0, 1, 4

ANSWER: e

38. Find all real solutions of the equation.

$$x^3 - 6x^2 + x - 6 = x^2 + 1$$

a. 7

b. 7, 3

c. 8

d. 8, 3

e. - 4

ANSWER: a

39. Find all solutions, real and complex, of the equation.

1.7 Solving Other Types of Equations

$$x^6 - 28x^3 + 27 = 0$$

a. $1, \pm 3, \frac{-1 + i\sqrt{3}}{2}, \frac{-3 \pm 3i\sqrt{3}}{2}$

b. $\pm 1, \pm 3, \frac{-1 + i\sqrt{3}}{2}$

c. $1, 3, \frac{-1 \pm i\sqrt{3}}{2}, \frac{-3 \pm 3i\sqrt{3}}{2}$

d. $1, 3, \frac{-1 \pm i\sqrt{3}}{4}, \frac{-3 \pm 3i\sqrt{3}}{2}$

e. $\pm 1, 3, \frac{-1 + i\sqrt{3}}{2}, \frac{-3 \pm 3i\sqrt{3}}{2}$

ANSWER: c

40. Solve the equation for the variable x . The constant c represents a positive real number.

$$\sqrt{x+c} + \sqrt{x-c} = \sqrt{2}\sqrt{x+5}$$

a. $\sqrt{c^2 - 25}$

b. $\sqrt{c^2 + 25}$

c. $\sqrt{c^2 + 5}$

d. $\sqrt{c^2 - 5}$

e. $\sqrt{c^2 + 20}$

ANSWER: b

41. Find all real solutions of the equation.

$$x^4 = 49x^2$$

a. $x = 0, x = 49$

b. $x = 0, x = 7, x = -7$

c. $x = 0, x = 49, x = -49$

d. $x = 0$

e. none of these

1.7 Solving Other Types of Equations**ANSWER:** b

42. Find all real solutions of the equation.

$$x^5 = 27x^2$$

- a. $x = 0$
- b. $x = 0, x = 27$
- c. $x = 0, x = 3, x = -3$
- d. $x = 0, x = 3$
- e. none of these

ANSWER: d

43. Find all real solutions of the equation.

$$\frac{5}{x} - \frac{45}{x+4} + 4 = 0$$

- a. $x = 0, x = 5$
- b. $x = 0, x = -45$
- c. $x = 1, x = 5$
- d. $x = 2, x = 10$
- e. none of these

ANSWER: c

44. Find all real solutions of the equation.

$$\frac{x^2}{x+12} = 1$$

- a. $x = 0, x = -3$
- b. $x = 16, x = -12$
- c. $x = 4, x = -3$
- d. $x = 0, x = -1$
- e. none of these

ANSWER: c

45. Find all real solutions of the equation.

$$\frac{1}{x-5} - \frac{36}{x^2} = 0$$

- a. $x = 6, x = 30$
- b. $x = 0, x = -36$
- c. $x = 0, x = 30$
- d. $x = 24, x = 120$

1.7 Solving Other Types of Equations

e. none of these

ANSWER: a

46. Find all real solutions of the equation.

$$(x + 3)^2 - 9(x + 3) + 18 = 0$$

a. $x = 0, x = 6$

b. $x = 0, x = -3$

c. $x = 0, x = 3$

d. $x = 0, x = -4$

e. none of these

ANSWER: c

47. Find all real solutions of the equation.

$$\left(\frac{x}{x+4}\right)^2 = \frac{6x}{x+4} - 9$$

a. - 6

b. 0, 6

c. 6, - 6

d. 2

e. none of these

ANSWER: a

48. Find all real solutions of the equation.

$$x^{\frac{4}{3}} - 41x^{\frac{2}{3}} + 400 = 0$$

a. 0, 64

b. $\pm 64, \pm 125$

c. 64, 125

d. $\pm 4, \pm 5$

e. none of these

ANSWER: b

49. Find all real solutions of the equation.

$$\sqrt{x} - 3\sqrt[4]{x} + 2 = 0$$

a. $x = -1, x = 16$

b. $x = -1, x = -16$

c. $x = 1, x = -16$

1.7 Solving Other Types of Equations

d. $x = 1, x = 16$

e. none of these

ANSWER: d

50. Find all real solutions of the equation.

$$x - 6\sqrt{x} + 8 = 0$$

a. $x = -16, x = -4$

b. $x = -16, x = 4$

c. $x = 16, x = -4$

d. $x = 16, x = 4$

e. none of these

ANSWER: d

51. Find all real solutions of the equation.

$$\sqrt{5x+4} + 2 = x$$

a. 0, 9

b. -1, 0

c. -9

d. 9

e. 0

ANSWER: d

52. Find all real solutions of the equation.

$$\sqrt{\sqrt{x+4} + x} = 4$$

a. $x = -42, x = -25$

b. $x = 12$

c. $x = 16$

d. $x = 21, x = 12$

e. $x = -21, x = 12$

ANSWER: b

53. Find all solutions, real and complex, of the equation.

$$x^3 = 125$$

a. $x = 5, x = \frac{5}{2}(1 - \sqrt{3}i), x = \frac{5}{2}(1 + \sqrt{3}i)$

b. $x = 5, x = -5$

c. $x = 5$

1.7 Solving Other Types of Equations

d. $x = 5, x = -\frac{5}{3}(1 - \sqrt{3}i), x = -\frac{5}{3}(1 + \sqrt{3}i)$

e. none of these

ANSWER: a

54. A social club charts a bus at a cost of \$630 to take a group of members on an excursion. At the last minute, 5 people in the group decide not to go. This raises the transportation cost per person by \$3. How many people originally intended to take the trip?

- a. 40 people
- b. 31 people
- c. 41 people
- d. 35 people
- e. 30 people

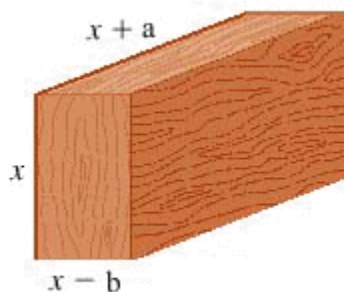
ANSWER: d

55. A large pond is stocked with fish. The fish population P is modeled by the formula $P = 4t + 7\sqrt{t} + 255$, where t is the number of days since the fish were first introduced into the pond. How many days will it take for the fish population to reach 312?

- a. 10 days
- b. 6 days
- c. 9 days
- d. 3 days
- e. 18 days

ANSWER: c

56. A large plywood box has a volume of 864 ft^3 . Its length is a ft greater than its height, and its width is b ft less than its height. What is the height of the box if $a = 7$ and $b = 3$?



- a. 8 feet
- b. 9 feet
- c. 10 feet
- d. 4 feet
- e. 18 feet

1.7 Solving Other Types of Equations

ANSWER: b

57. A jeweler has three small solid spheres made of gold, of radius 1 mm, 3 mm, and 4 mm. He decides to melt these down and make just one sphere out of them. What will the radius of this larger sphere be?

- a. 5.10 mm
- b. 18.91 mm
- c. 4.51 mm
- d. 56.73 mm
- e. 8.00 mm

ANSWER: c

58. Grain is falling from a chute onto the ground, forming a conical pile whose diameter is always three times its height. How high is the pile to the nearest hundredth of a foot when it contains $2,400 \text{ ft}^3$ of grain?



- a. 31.92 feet
- b. 6.34 feet
- c. 10.06 feet
- d. 14.51 feet
- e. 9.28 feet

ANSWER: c

59. A spherical tank has a capacity of 550 gallons. Using the fact that one gallon is about 0.1337 ft^3 , find the radius of the tank. Round your answer to the nearest hundredth of a foot.

- a. 5.59 feet
- b. 6.16 feet
- c. 2.60 feet
- d. 5.08 feet
- e. 4.19 feet

ANSWER: c

60. A city lot has the shape of a right triangle whose hypotenuse is 25 ft longer than one of the other sides. The perimeter of the lot is 300 ft. How long is the hypotenuse of the lot?

- a. 125 feet

1.7 Solving Other Types of Equations

- b. 75 feet
- c. 100 feet
- d. 62.5 feet
- e. 250 feet

ANSWER: a

61. Find all real solutions of the equation.

$$x^3 - x^2 + x - 1 = x^2 + 1$$

ANSWER: 2

62. Find all real solutions of the equation.

$$\sqrt{5x + 4} + 2 = x$$

ANSWER: 9

63. Find all real solutions of the equation.

$$\sqrt{\sqrt{x + 19} + x} = 1$$

ANSWER: -3

64. A social club charts a bus at a cost of \$1,400 to take a group of members on an excursion. At the last minute, 5 people in the group decide not to go. This raises the transportation cost per person by \$5. How many people originally intended to take the trip?

_____ people

ANSWER: 40

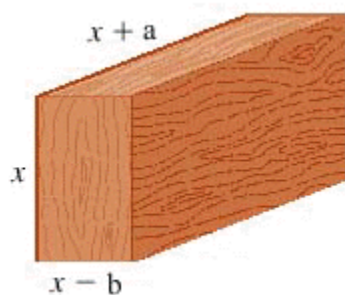
65. A large pond is stocked with fish. The fish population P is modeled by the formula $P = 4t + 10\sqrt{t} + 100$, where t is the number of days since the fish were first introduced into the pond. How many days will it take for the fish population to reach 204?

_____ days

ANSWER: 16

66. A large plywood box has a volume of 540 ft^3 . Its length is a ft greater than its height, and its width is b ft less than its height. What is the height of the box if $a = 3$ and $b = 4$?

1.7 Solving Other Types of Equations



_____ feet
ANSWER: 9

67. A jeweler has three small solid spheres made of gold, of radius 3 mm, 6 mm, and 8 mm. He decides to melt these down and make just one sphere out of them. What will the radius of this larger sphere be?

_____ mm
ANSWER: 9.11

68. Grain is falling from a chute onto the ground, forming a conical pile whose diameter is always three times its height. How high is the pile to the nearest hundredth of a foot when it contains $1,000 \text{ ft}^3$ of grain?



_____ feet
ANSWER: 7.52

69. A spherical tank has a capacity of 650 gallons. Using the fact that one gallon is about 0.1337 ft^3 , find the radius of the tank to the nearest hundredth of a foot.

_____ feet
ANSWER: 2.75

70. A city lot has the shape of a right triangle whose hypotenuse is 36 ft longer than one of the other sides. The perimeter of the lot is 216 ft. How long is the hypotenuse of the lot?

_____ feet
ANSWER: 90

1.7 Solving Other Types of Equations

71. Find all real solutions of the equation.

$$x^3 - 13x^2 + 42x = 0$$

ANSWER: 0,6,7

72. Find all solutions, real and complex, of the equation.

$$x^6 - 65x^3 + 64 = 0$$

ANSWER:

$$1, 4, \frac{-1 \pm i \cdot \sqrt{3}}{2}, -2 \pm 2i \cdot \sqrt{3}$$

73. Solve the equation for the variable x . The constant b represents a positive real number.

$$\sqrt{x+b} + \sqrt{x-b} = \sqrt{2} \sqrt{x+6}$$

ANSWER: $\sqrt{b^2 + 36}$

74. Find all real solutions of the equation.

$$x^4 = 25x^2$$

ANSWER: 5,-5,0

75. Find all real solutions of the equation.

$$x^5 = 64x^2$$

ANSWER: 4,0

76. Find all real solutions of the equation.

$$\frac{4}{x} - \frac{24}{x+4} + 2 = 0$$

ANSWER: 2,4

77. Find all real solutions of the equation.

$$\frac{x^2}{x+6} = 1$$

ANSWER: 3,-2

78. Find all real solutions of the equation.

$$\frac{1}{x-7} - \frac{64}{x^2} = 0$$

ANSWER: 8,56

79. Find all real solutions of the equation.

1.7 Solving Other Types of Equations

$$(x + 5)^2 - 8(x + 5) + 15 = 0$$

ANSWER: -2,0

80. Find all real solutions of the equation.

$$\left(\frac{x}{x+6}\right)^2 = \frac{12x}{x+6} - 36$$

ANSWER: $-\frac{36}{5}$

81. Find all real solutions of the equation.

$$x^{\frac{4}{3}} - 34x^{\frac{2}{3}} + 225 = 0$$

ANSWER: 27,125,-27,-125

82. Find all real solutions of the equation.

$$\sqrt{x} - 5\sqrt[4]{x} + 6 = 0$$

ANSWER: 81,16

83. Find all real solutions of the equation.

$$x - 6\sqrt{x} + 8 = 0$$

ANSWER: 4,16

84. Find all solutions, real and complex, of the equation.

$$x^3 = 27$$

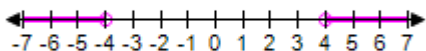
ANSWER: $x = 3, x = \frac{-3 \pm 3 \cdot \sqrt{3} \cdot i}{2}$

1.8 Solving Inequalities

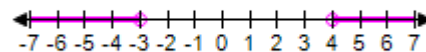
1. Solve the nonlinear inequality. Express the solution using interval notation and graph the solution set.

$$x^2 + x > 12$$

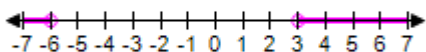
a. $(-\infty, -4) \cup (4, \infty)$;



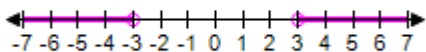
b. $(-\infty, -3) \cup (4, \infty)$;



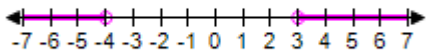
c. $(-\infty, -6) \cup (3, \infty)$;



d. $(-\infty, -3) \cup (3, \infty)$;



e. $(-\infty, -4) \cup (3, \infty)$;



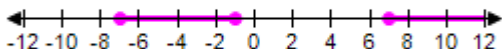
ANSWER: e

2. Solve the nonlinear inequality. Express the solution using interval notation and graph the solution set.

$$49x \leq x^3$$

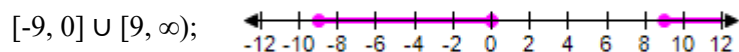
a.

$[-7, -1] \cup [7, \infty)$;

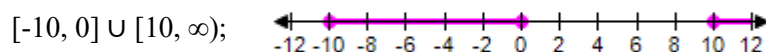


1.8 Solving Inequalities

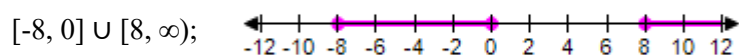
b.



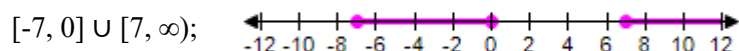
c.



d.



e.



ANSWER: e

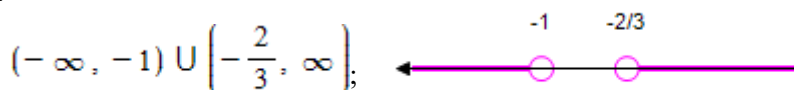
3. Solve the nonlinear inequality. Express the solution using interval notation and graph the solution set.

$$\frac{x}{x+1} > 3x$$

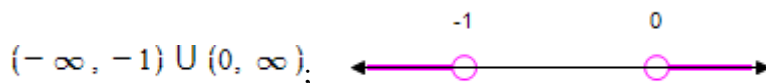
a.



b.

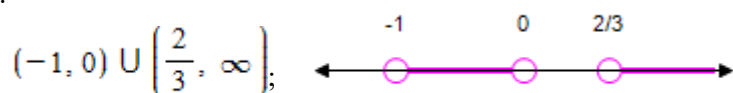


c.

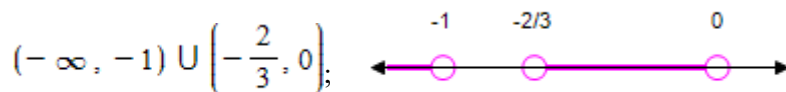


1.8 Solving Inequalities

d.



e.

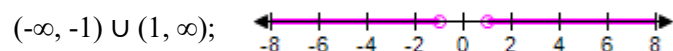


ANSWER: e

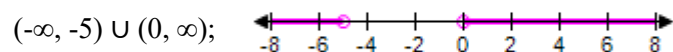
4. Solve the nonlinear inequality. Express the solution using interval notation and graph the solution set.

$$x^4 > 25x^2$$

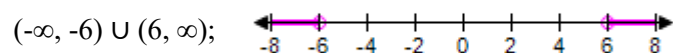
a.



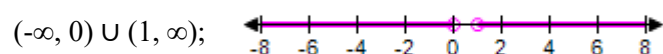
b.



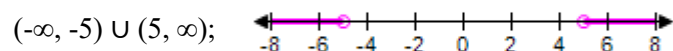
c.



d.



e.



ANSWER: e

5. Determine the values of the variable for which the expression is defined as a real number.

1.8 Solving Inequalities

$$\left(\frac{1}{x^2 - x - 42} \right)^{\frac{1}{2}}$$

- a. $(-\infty, -4) \cup (5, \infty)$
- b. $(-\infty, -5) \cup (8, \infty)$
- c. $(-\infty, -6) \cup (7, \infty)$
- d. $(-\infty, -5) \cup (7, \infty)$
- e. $(-\infty, -6) \cup (8, \infty)$

ANSWER: c

6. In the vicinity of a bonfire, the temperature T in $^{\circ}\text{C}$ at a distance of x meters from the center of the fire was given by

$$T = \frac{950,000}{x^2 + 300}.$$



At what range of distances from the fire's center was the temperature less than 500°C ?

- a. More than 20 meters
- b. More than 35 meters
- c. More than 45 meters
- d. More than 10 meters
- e. More than 40 meters

ANSWER: e

7. A riverboat theater offers bus tours to groups on the following basis. Hiring the bus costs the group \$360, to be shared equally by the group members. Theater tickets, normally \$30 each, are discounted by 25 cents times the number of people in the group. How many members must be in the group so that the cost of the theater tour (bus fare plus theater ticket) is less than \$39 per person?

- a. at least 25 members
- b. at least 12 members
- c. at least 16 members
- d. at least 24 members
- e. at least 20 members

ANSWER: a

8. Solve the inequality. Express the solution using interval notation.

$$4x \leq 16$$

1.8 Solving Inequalities

a. $x \in (-\infty, 9)$

b. $x \in (-4, \infty)$

c. $x \in (-\infty, 4]$

d. $x \in (-\infty, 4)$

e. $x \in (-\infty, 9]$

ANSWER: c

9. Solve the inequality. Express the solution using interval notation.

$$3x + 13 < 7$$

a. $x \in (-\infty, 3)$

b. $x \in (-\infty, 2)$

c. $x \in (-2, \infty)$

d. $x \in (-\infty, -2)$

e. $x \in (-\infty, 13]$

ANSWER: d

10. Solve the inequality. Express the solution using interval notation.

$$11 - 3x \leq -13$$

a. $x \in (-\infty, 8)$

b. $x \in (-\infty, 4]$

c. $x \in (-8, \infty)$

d. $x \in [8, \infty)$

e. $x \in (-\infty, -4)$

ANSWER: d

11. Solve the inequality. Express the solution using interval notation.

$$0 < 5 - 2x$$

a. $x \in [\frac{3}{2}, \infty)$

b. $x \in (-\infty, \frac{5}{2})$

c. $x \in (-\infty, \frac{3}{2})$

d. $x \in (-\infty, \frac{5}{2}]$

e. $x \in (\frac{3}{2}, \infty)$

ANSWER: b

1.8 Solving Inequalities

12. Solve the inequality. Express the solution using interval notation.

$$3 - x \geq 3x + 7$$

- a. $x \in (-\infty, 2)$
- b. $x \in (-\infty, -1]$
- c. $x \in (-\infty, -2)$
- d. $x \in (-\infty, -1)$
- e. $x \in (-\infty, 1)$

ANSWER: b

13. Solve the inequality. Express the solution using interval notation.

$$\frac{9}{10}x + 1 < \frac{1}{10} - 9x$$

- a. $x \in (-\infty, -15)$
- b. $x \in \left[-\frac{1}{11}, \infty\right)$
- c. $x \in (-\infty, -11)$
- d. $x \in \left[-\frac{1}{15}, \infty\right)$
- e. $x \in \left[-\infty, -\frac{1}{11}\right)$

ANSWER: e

14. Solve the inequality. Express the solution using interval notation.

$$6 \leq x + 9 < 8$$

- a. $[6, 7)$
- b. $[-3, -1)$
- c. $[-7, -6)$
- d. $[1, 3)$
- e. $[-8, -1)$

ANSWER: b

15. Solve the inequality. Express the solution using interval notation.

$$7 < 5x + 12 \leq 32$$

- a. $(-1, 4]$
- b. $(-1, 10]$
- c. $(9, 9]$
- d. $[-9, -9]$

1.8 Solving Inequalities

e. $[9, 10)$

ANSWER: a

16. Solve the inequality. Express the solution using interval notation.

$$-25 \leq 10 - 5x \leq 20$$

a. $[-2, 7)$

b. $[-7, 2]$

c. $(-2, 7)$

d. $[-2, 7]$

e. $[-7, 2)$

ANSWER: d

17. Solve the inequality. Express the solution using interval notation.

$$\frac{1}{2} \geq \frac{2x - 5}{8} > \frac{1}{4}$$

a. $(\frac{11}{2}, \frac{21}{2}]$

b. $[-\frac{7}{2}, \frac{9}{2})$

c. $(\frac{7}{2}, \frac{13}{2}]$

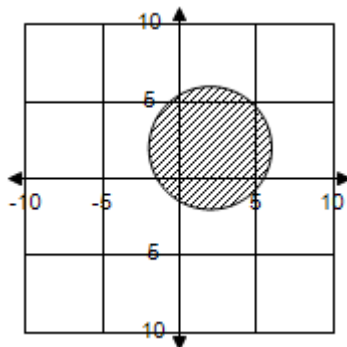
d. $(\frac{7}{2}, \frac{9}{2}]$

e. $[-\frac{11}{2}, \frac{21}{2})$

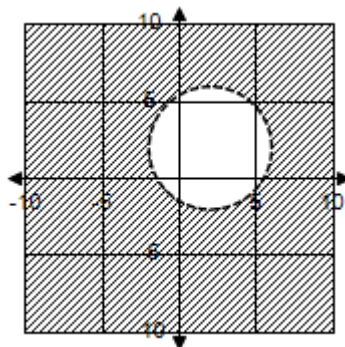
ANSWER: d

18. Determine the correct sketch of the area given by the inequality $x^2 + y^2 - 4x - 4y < 8$

a.

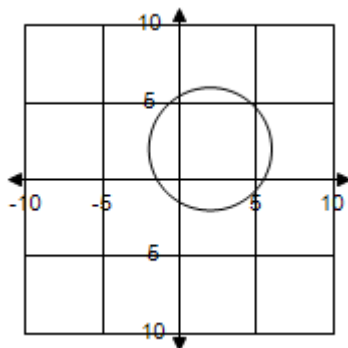


b.

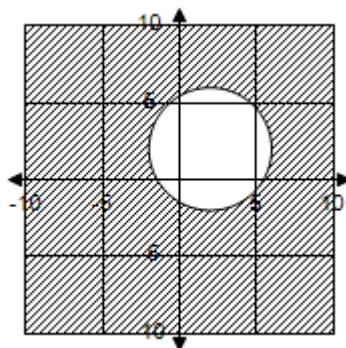


1.8 Solving Inequalities

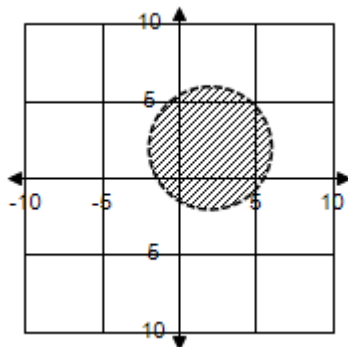
c.



d.



e.



ANSWER: e

19. A car rental company offers two plans for renting a car.

Plan A: \$30 per day and \$0.20 per mile.

Plan B: \$45 per day with free unlimited mileage.

For what range of miles will plan B save you money?

- a. Less than 160 mi
- b. Less than 325 mi
- c. More than 75 mi
- d. More than 160 mi
- e. Less than 75 mi

ANSWER: c

20. It is estimated that the annual cost of driving a certain new car is given by the formula

$$C = 0.5m + 2,100,$$

where m represents the number of miles driven per year and C is the cost in dollars. Jane has purchased such a car, and decides to budget between \$9,600 and \$11,100 for next year's driving costs. What is the corresponding range of miles that she can drive her new car?

- a. Between 14,000 mi and 16,000 mi
- b. Between 14,000 mi and 18,000 mi
- c. Between 15,000 mi and 18,000 mi
- d. Between 15,000 mi and 16,000 mi

1.8 Solving Inequalities

e. More than 18,000 mi

ANSWER: c

21. Solve the inequality for x , assuming that p , b , and d are positive constants.

$$p(bx - d) \geq bd$$

a. $x \geq \frac{p(d + b)}{db}$

b. $x \leq \frac{b(p + d)}{pd}$

c. $x \geq \frac{d(b - p)}{pb}$

d. $x \geq \frac{d(p + b)}{pb}$

e. $x \leq \frac{p(p - b)}{db}$

ANSWER: d

22. Let $S = \left\{-5, 0, \frac{1}{7}, \sqrt{7}, 7\right\}$.

Use substitution to determine which elements of S satisfy the inequality $x + 5 \geq 0$.

a. $\frac{1}{7}$

b. 0

c. 7

d. $\sqrt{7}$

e. -5

ANSWER: a, b, c, d, e

23. Let $S = \left\{-2, 0, \frac{1}{7}, \sqrt{7}, 7\right\}$.

Use substitution to determine which elements of S satisfy the inequality $x - 7 < 0$.

a. $\sqrt{7}$

b. $\frac{1}{7}$

c. 0

d. 7

1.8 Solving Inequalities

e. -2

ANSWER: a, b, c, e

24. A riverboat theater offers bus tours to groups on the following basis. Hiring the bus costs the group \$180, to be shared equally by the group members. Theater tickets, normally \$30 each, are discounted by 25 cents times the number of people in the group. How many members must be in the group so that the cost of the theater tour (bus fare plus theater ticket) is less than \$42 per person?

At least _____ members

ANSWER: 13

25. Determine the values of the variable for which the expression is defined as a real number.

$$\left(\frac{1}{x^2 - 3x - 28} \right)^{\frac{1}{2}}$$

ANSWER: $(-\infty, -4) \cup (7, \infty)$

26. In the vicinity of a bonfire, the temperature T in $^{\circ}\text{C}$ at a distance of x meters from the center of the fire was given by

$$T = \frac{350,000}{x^2 + 300}.$$



At what range of distances from the fire's center was the temperature less than 500°C ?

ANSWER: $(20, \infty)$

27. Let $S = \left\{ -1, 0, \frac{1}{3}, \sqrt{3}, 3 \right\}.$

Use substitution to determine which elements of S satisfy the inequality $x + 1 \geq 0$.

ANSWER: $S = \left\{ -1, 0, \frac{1}{3}, \sqrt{3}, 3 \right\}$

28. Let $S = \left\{ -3, 0, \frac{1}{5}, \sqrt{5}, 5 \right\}.$

Use substitution to determine which elements of S satisfy the inequality $x - 5 < 0$.

ANSWER: $S = \left\{ -3, 0, \frac{1}{5}, \sqrt{5} \right\}$

29. Solve the inequality. Express the solution using interval notation.

$$2x \leq 12$$

1.8 Solving Inequalities**ANSWER:** $(-\infty, 6]$

30. Solve the inequality. Express the solution using interval notation.

$$4x + 15 < 3$$

ANSWER: $(-\infty, -3)$

31. Solve the inequality. Express the solution using interval notation.

$$3 - 4x \leq -9$$

ANSWER: $[3, \infty)$

32. Solve the inequality. Express the solution using interval notation.

$$0 < 7 - 3x$$

ANSWER: $\left(-\infty, \frac{7}{3}\right)$

33. Solve the inequality. Express the solution using interval notation.

$$7 - x \geq 5x + 19$$

ANSWER: $(-\infty, -2]$

34. Solve the inequality. Express the solution using interval notation.

$$\frac{2}{5}x + 1 < \frac{1}{5} - 2x$$

ANSWER: $\left(-\infty, -\frac{1}{3}\right)$

35. Solve the inequality. Express the solution using interval notation.

$$6 \leq x + 9 < 8$$

ANSWER: $[-3, -1)$

36. Solve the inequality. Express the solution using interval notation.

$$2 < 3x + 5 \leq 26$$

ANSWER: $(-1, 7]$

37. Solve the inequality. Express the solution using interval notation.

$$-2 \leq 12 - 2x \leq 16$$

ANSWER: $[-2, 7]$

38. Solve the inequality. Express the solution using interval notation.

$$\frac{2}{3} \geq \frac{2x - 9}{12} > \frac{1}{6}$$

1.8 Solving Inequalities

ANSWER: $(\frac{11}{2}, \frac{17}{2}]$

39. A car rental company offers two plans for renting a car.

Plan A: \$25 per day and \$0.25 per mile.

Plan B: \$50 per day with free unlimited mileage.

For what range of miles will plan B save you money?

ANSWER: $m > 100$

40. It is estimated that the annual cost of driving a certain new car is given by the formula

$$C = 0.15m + 1,700,$$

where m represents the number of miles driven per year and C is the cost in dollars. Jane has purchased such a car, and decides to budget between \$3,350 and \$3,950 for next year's driving costs. What is the corresponding range of miles that she can drive her new car?

ANSWER: $15,000 \geq m \geq 11,000$

41. Solve the inequality for x , assuming that m , n , and d are positive constants.

$$m(nx - d) \geq nd$$

ANSWER: $x \geq \frac{d \cdot (m + n)}{(m \cdot n)}$

1.9 Solving Absolute-Value Eqns and Ineqs

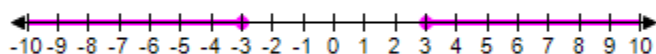
1. A phrase describing set of real numbers is given. Express the phrase as an inequality involving an absolute value.

All real numbers x at least 3 units from 4

- a. $|x - 4| \leq 3$
- b. $|x - 3| < 4$
- c. $|x - 4| > 3$
- d. $|x - 4| < 3$
- e. $|x - 4| \geq 3$

ANSWER: d

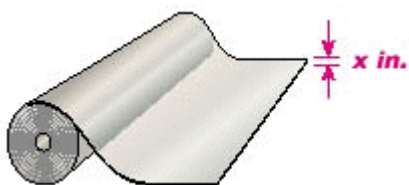
2. A set of real numbers is graphed. Find an inequality involving an absolute value that describes the set.



- a. $|x| < 3$
- b. $|x| \geq 3$
- c. $|x - 4| \geq 3$
- d. $|x| \leq 3$
- e. $|x| > 3$

ANSWER: b

3. A company manufactures industrial laminates (thin nylon-based sheets) of thickness 0.024 in, with a tolerance of 0.004 in.



Solve the inequality involving absolute values that describes the range of possible thickness for the laminate.

- a. $0.021 \leq x \leq 0.028$
- b. $0.021 \leq x \leq 0.029$
- c. $0.020 \leq x \leq 0.029$
- d. $0.020 \leq x \leq 0.028$
- e. $0.022 \leq x \leq 0.026$

ANSWER: d

4. Solve the equation.

1.9 Solving Absolute-Value Eqns and Ineqs

$$|2x| = 10$$

- a. $x = \pm 3$
- b. $x = \pm 20$
- c. $x = \pm 2$
- d. $x = \pm 5$
- e. $x = 5$

ANSWER: d

5. Solve the equation.

$$|x - 2| = 4$$

- a. $x = 6$
- b. $x = 8$ and $x = 0$
- c. $x = 3$ and $x = -5$
- d. $x = \pm 6$
- e. $x = 6$ and $x = -2$

ANSWER: e

6. Solve the equation.

$$|x + 1| = 0.5$$

- a. $x = 1.5$ and $x = 0.5$
- b. $x = 2.5$ and $x = 1.5$
- c. $x = \pm 0.5$
- d. $x = -0.5$
- e. $x = -0.5$ and $x = -1.5$

ANSWER: e

7. Solve the problem.

$$|8x + 6| = 10$$

- a. $x = 0.5$ and $x = -2$
- b. $x = 2.5$ and $x = 0$
- c. $x = 0.5$
- d. $x = \pm 0.5$
- e. $x = -2.5$ and $x = -5$

ANSWER: a

8. Solve the equation.

$$|3 - 4x| + 8 = 12$$

1.9 Solving Absolute-Value Eqns and Ineqs

- a. $x = 2.75$ and $x = 4.75$
- b. $x = 1.75$ and $x = 3.75$
- c. $x = -0.25$ and $x = 1.75$
- d. $x = -0.25$
- e. $x = \pm 0.25$

ANSWER: c

9. Solve the equation.

$$\left| \frac{2}{5}x + 4 \right| - \frac{1}{4} = 6$$

- a. $x = \pm \frac{45}{8}$
- b. $x = \frac{45}{8}$ and $x = -\frac{205}{8}$
- c. $x = \frac{43}{6}$ and $x = -\frac{208}{11}$
- d. $x = \frac{45}{8}$
- e. $x = \frac{48}{11}$ and $x = -\frac{203}{6}$

ANSWER: b

10. Solve the equation.

$$|x + 25| = |4x + 7|$$

- a. $x = \pm 6$
- b. $x = 6$
- c. $x = 3$ and $x = -\frac{29}{4}$
- d. $x = 6$ and $x = -\frac{32}{5}$
- e. $x = 4$ and $x = -\frac{30}{3}$

ANSWER: d

11. Solve the inequality. Express the answer using interval notation.

$$|x| < 4$$

1.9 Solving Absolute-Value Eqns and Ineqs

- a. Interval: $(-4, 4)$
- b. Interval: $(-\infty, -4) \cup (4, \infty)$
- c. Interval: $[-4, 4]$
- d. Interval: $[-3, 3]$
- e. $\emptyset$

ANSWER: a

12. Solve the inequality. Express the answer using interval notation.

$$|x - 4| > 2$$

- a. Interval: $(-\infty, 2] \cup [6, \infty)$
- b. Interval: $(2, 6)$
- c. Interval: $(-\infty, 2) \cup (6, \infty)$
- d. Interval: $(-\infty, 6) \cup (6, \infty)$
- e. $\emptyset$

ANSWER: c

13. Solve the inequality. Express the answer using interval notation.

$$|x + 4| \geq 8$$

- a. Interval: $(-\infty, -12) \cup (4, \infty)$
- b. Interval: $[4, \infty)$
- c. Interval: $(-\infty, -12] \cup [4, \infty)$
- d. Interval: $[-12, 4]$
- e. $\emptyset$

ANSWER: c

14. Solve the inequality.

$$|7x - 2| < 8$$

- a. Interval: $(-\infty, -\frac{6}{7}) \cup (\frac{10}{7}, \infty)$
- b. Interval: $(-\frac{6}{7}, \frac{10}{7})$
- c. Interval: $(-\infty, -\frac{6}{7})$
- d. Interval: $[-\frac{6}{7}, \frac{10}{7}]$

1.9 Solving Absolute-Value Eqns and Ineqse. $\emptyset$

ANSWER: b

15. Solve the inequality.

$$\left| \frac{x+5}{2} \right| \geq 9$$

a. Interval: $[-23, 13]$ b. Interval: $(-\infty, -23) \cup (13, \infty)$ c. Interval: $(-\infty, -23] \cup [13, \infty)$ d. Interval: $[23, \infty)$ e. $\emptyset$

ANSWER: c

16. Solve the inequality.

$$11 - |2x + 2| \leq 3$$

a. Interval: $(-\infty, -5) \cup (3, \infty)$ b. Interval: $[5, \infty)$ c. Interval: $[-5, 3]$ d. Interval: $(-\infty, -5] \cup [3, \infty)$ e. $\emptyset$

ANSWER: d

17. Solve the inequality. Express the answer using interval notation.

$$4|x + 6| + 4 > 3$$

a. Interval: $(-\infty, \infty)$ b. Interval: $[5.8, \infty)$ c. Interval: $(-\infty, -7) \cup (7, \infty)$ d. Interval: $(-\infty, -1) \cup (1, \infty)$ e. $\emptyset$

ANSWER: a

18. Solve the inequality.

$$3\left|\frac{1}{2}x + 5\right| + 4 \leq 73$$

a. $(-\infty, -56] \cup [36, \infty)$

1.9 Solving Absolute-Value Eqns and Ineqs

- b. $[-56, 36]$
- c. $(-56, 36)$
- d. $\emptyset$

ANSWER: b

19. Solve the inequality. Express the answer using interval notation.

$$5 \leq |x| \leq 9$$

- a. $[-9, -5] \cup [5, 9]$
- b. $(-9, -5) \cup (5, 9)$
- c. $[-9, 9]$
- d. $(-\infty, -9] \cup [-5, 5] \cup [9, \infty)$
- e. $\emptyset$

ANSWER: a

20.

Solve the inequality.

$$0 < |x - 3| \leq \frac{1}{4}$$

- a. $[\frac{11}{4}, 3) \cup (3, \frac{13}{4}]$
- b. $[\frac{-13}{4}, -3) \cup (3, \frac{13}{4}]$
- c. $(\frac{11}{4}, 3) \cup (3, \frac{13}{4})$
- d. $[\frac{11}{4}, \frac{13}{4}]$
- e. $\emptyset$

ANSWER: a

21. Solve the inequality.

$$\frac{1}{|3x - 7|} \leq 3$$

- a. $[-\frac{20}{9}, \frac{20}{9}]$
- b. $[\frac{20}{9}, \frac{22}{9}]$

1.9 Solving Absolute-Value Eqns and Ineqs

c. $(-\infty, \frac{20}{9}] \cup [\frac{22}{9}, \infty)$

d. $(-\infty, \infty)$

e. $\emptyset$

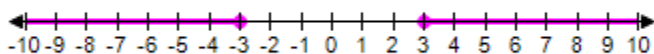
ANSWER: c

22. A phrase describing set of real numbers is given. Express the phrase as an inequality involving an absolute value.

All real numbers x less than 2 units from 6

ANSWER: $|x - 6| < 2$

23. A set of real numbers is graphed. Find an inequality involving an absolute value that describes the set.



ANSWER: $|x| \geq 3$

24. Solve the equation.

$|3x| = 24$

ANSWER: $8, -8$

25. Solve the equation.

$|x - 7| = 4$

ANSWER: $11, 3$

26. Solve the equation.

$|x + 6| = 3.5$

ANSWER: $x = -2.5, x = -9.5$

27. Solve the problem.

$|4x + 7| = 9$

ANSWER: $x = 0.5, x = -4$

28. Solve the equation.

$|3 - 4x| + 4 = 16$

ANSWER: $\frac{-9}{4}, \frac{15}{4}$

29. Solve the equation.

1.9 Solving Absolute-Value Eqns and Ineqs

$$\left| \frac{2}{5}x + 6 \right| - \frac{1}{2} = 6$$

$$\text{ANSWER: } \frac{5}{4}, -\frac{125}{4}$$

30. Solve the equation.

$$|x + 11| = |6x + 1|$$

$$\text{ANSWER: } 2, -\frac{12}{7}$$

31. Solve the inequality. Express the answer using interval notation.

$$|x| < 9$$

$$\text{ANSWER: } (-9, 9)$$

32. Solve the inequality. Express the answer using interval notation.

$$|x - 3| > 6$$

$$\text{ANSWER: } (-\infty, -3) \cup (9, \infty)$$

33. Solve the inequality. Express the answer using interval notation.

$$|x + 4| \geq 6$$

$$\text{ANSWER: } (-\infty, -10] \cup [2, \infty)$$

34. Solve the inequality. Express the answer using interval notation.

$$|7x - 2| < 8$$

$$\text{ANSWER: } \left(\frac{-6}{7}, \frac{10}{7} \right)$$

35. Solve the inequality. Express the answer using interval notation.

$$\left| \frac{x+2}{4} \right| \geq 8$$

$$\text{ANSWER: } (-\infty, -34] \cup [30, \infty)$$

36. Solve the inequality. Express the answer using interval notation.

$$9 - |2x + 11| \leq 2$$

$$\text{ANSWER: } (-\infty, -9] \cup [-2, \infty)$$

37. Solve the inequality. Express the answer using interval notation.

$$5|x + 4| + 5 > 4$$

1.9 Solving Absolute-Value Eqns and Ineqs

ANSWER: $(-\infty, \infty)$

38. Solve the inequality. Express the answer using interval notation.

$$2\left|\frac{1}{3}x + 2\right| + 4 \leq 60$$

ANSWER: $[-90, 78]$

39. Solve the inequality. Express the answer using interval notation.

$$1 \leq |x| \leq 5$$

ANSWER: $[-5, -1] \cup [1, 5]$

40. Solve the inequality. Express the answer using interval notation.

$$0 < |x - 7| \leq \frac{1}{2}$$

ANSWER: $[\frac{13}{2}, 7) \cup (7, \frac{15}{2}]$

41. Solve the inequality. Express the answer in interval notation.

$$\frac{1}{|5x - 1|} \leq 7$$

ANSWER: $(-\infty, \frac{6}{35}] \cup [\frac{8}{35}, \infty)$

1.10 Solving Eqns and Ineqs Graphically

1. Use a graphing calculator to decide which viewing rectangle produces the most appropriate graph of the equation.

$$y = x^4 + 3$$

- a. $[-60, 6]$ by $[-6, 6]$
- b. $[-6, 6]$ by $[-60, 6]$
- c. $[-3, 3]$ by $[-3, 3]$
- d. $[-6, 6]$ by $[-6, 60]$
- e. $[-6, 60]$ by $[-6, 6]$

ANSWER: d

2. Use a graphing calculator to decide which viewing rectangle produces the most appropriate graph of the equation.

$$y = 12 + 36x - x^3$$

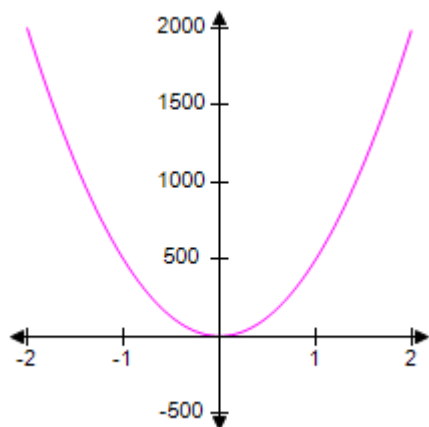
- a. $[-1, 12]$ by $[-150, 150]$
- b. $[-6, 6]$ by $[-20, 60]$
- c. $[-10, 10]$ by $[-150, 150]$
- d. $[-12, 6]$ by $[-20, 80]$
- e. $[-12, 0]$ by $[-36, 150]$

ANSWER: c

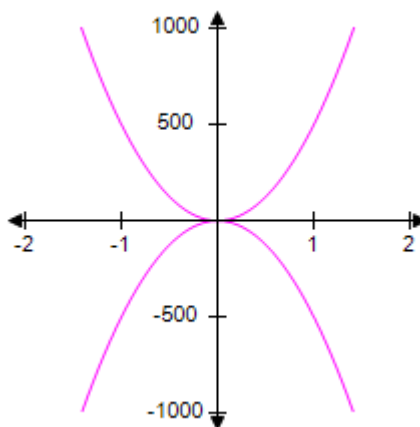
3. Draw the graph.

$$y = -500x^2$$

a.

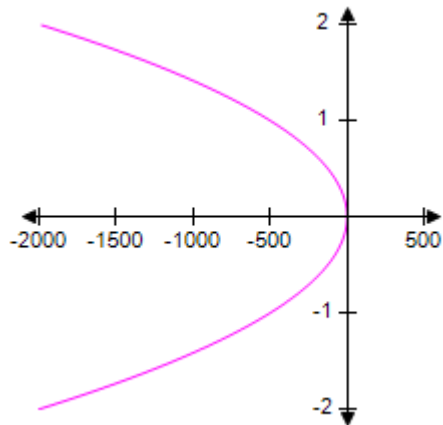


b.

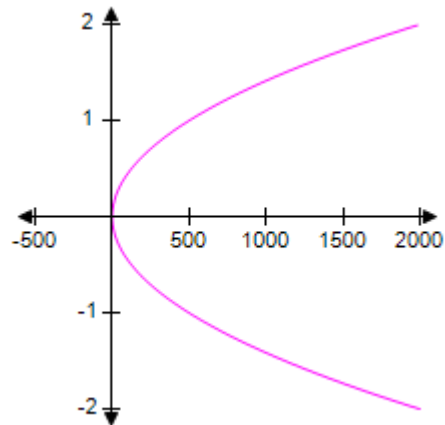


1.10 Solving Eqns and Ineqs Graphically

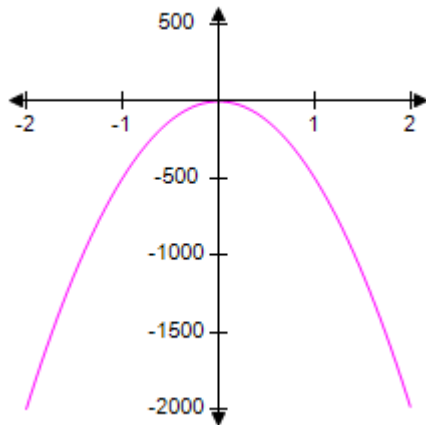
c.



d.



e.

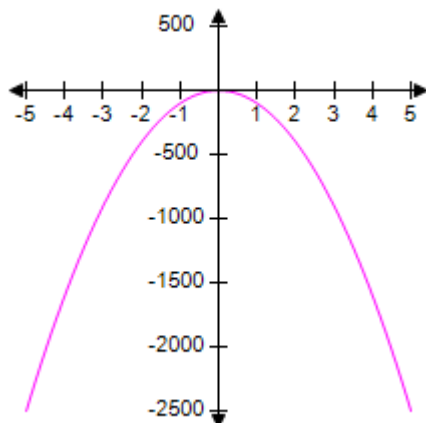


ANSWER: e

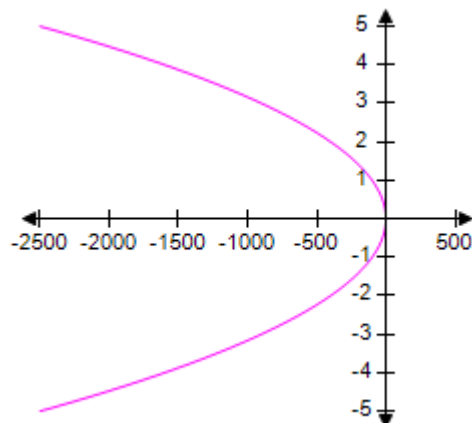
4. Draw the graph.

$$y = 100x^2$$

a.

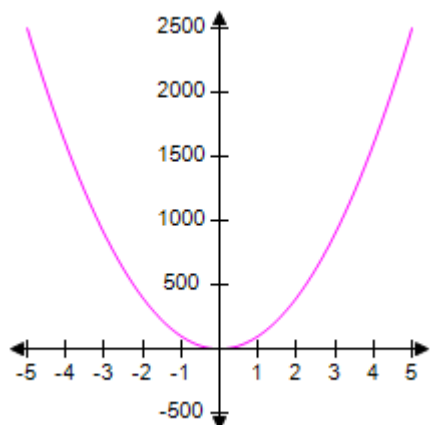


b.

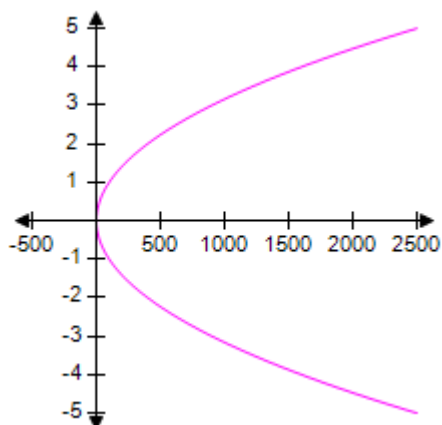


1.10 Solving Eqns and Ineqs Graphically

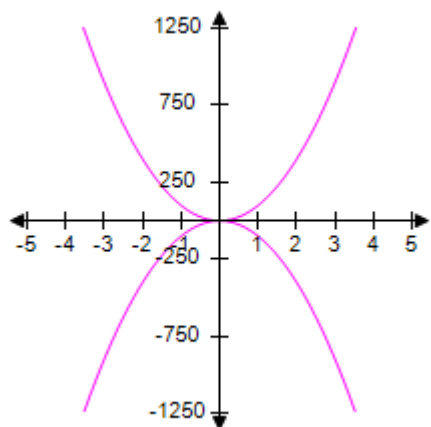
c.



d.



e.

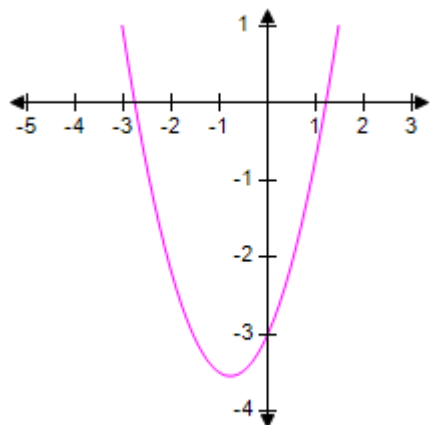


ANSWER: c

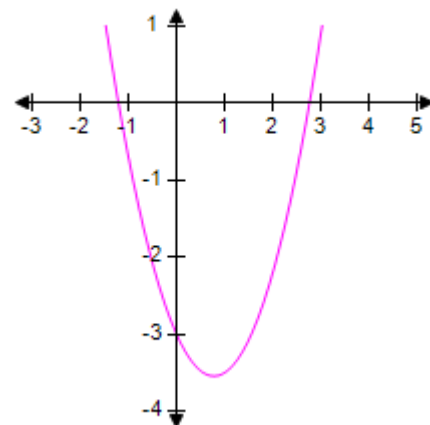
5. Draw the graph.

$$y = 0.9x^2 + 1.4x - 3$$

a.

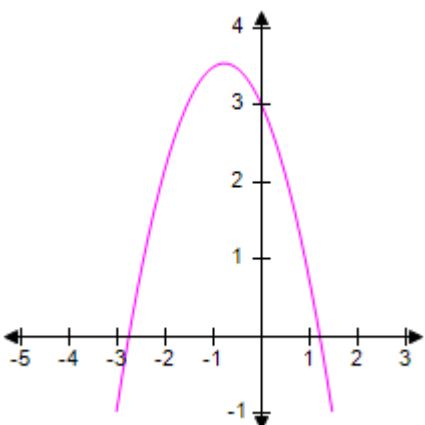


b.

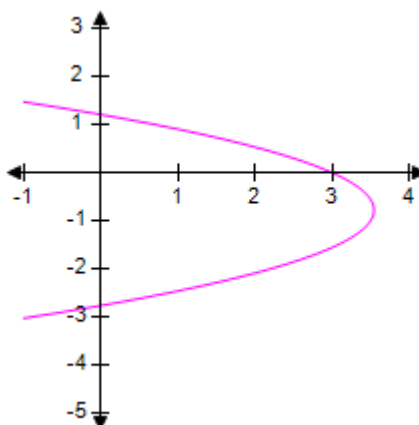


1.10 Solving Eqns and Ineqs Graphically

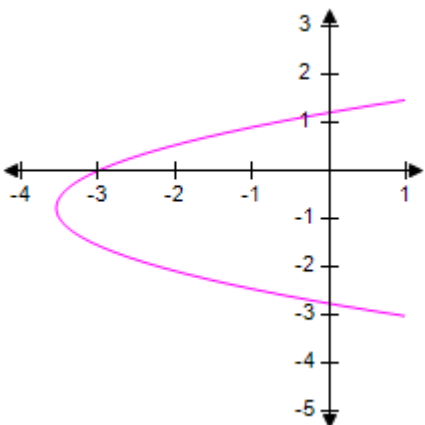
c.



d.



e.

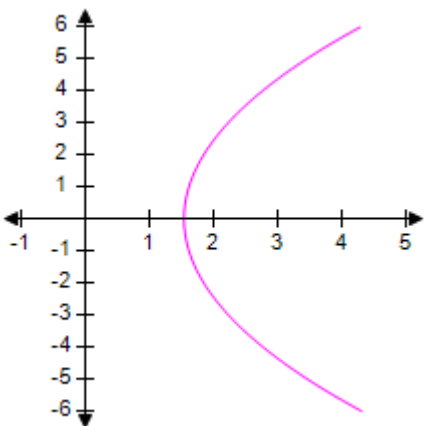


ANSWER: a

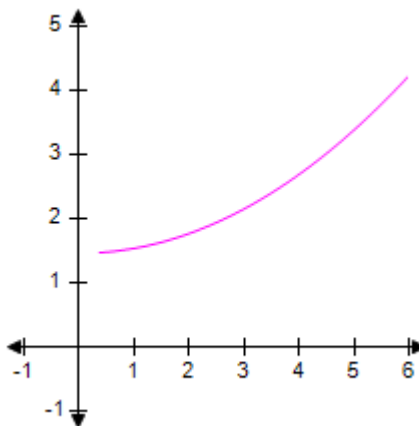
6. Draw the graph.

$$y = \sqrt{13x - 19}$$

a.

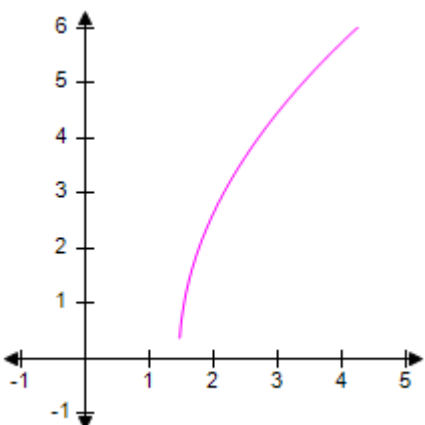


b.

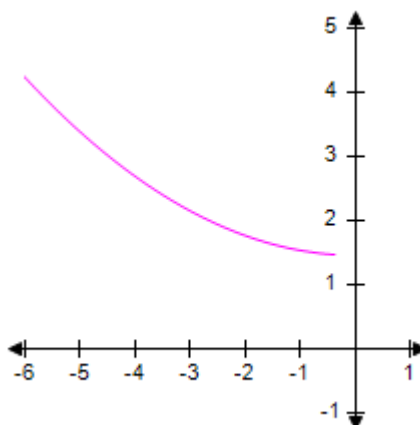


1.10 Solving Eqns and Ineqs Graphically

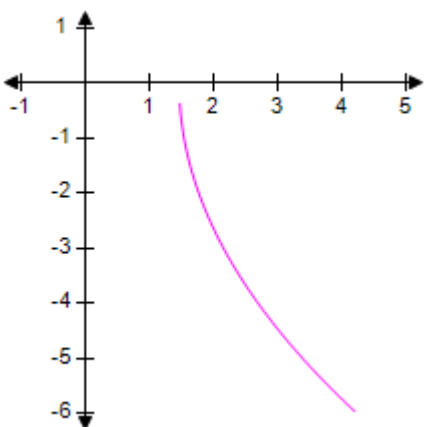
c.



d.



e.

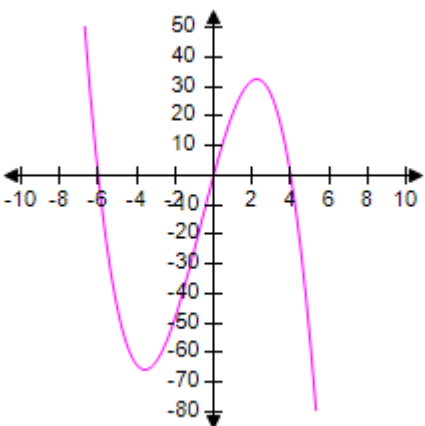


ANSWER: c

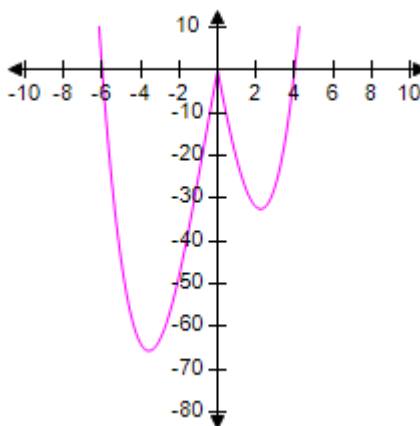
7. Draw the graph.

$$y = x(x + 6)(x - 4)$$

a.

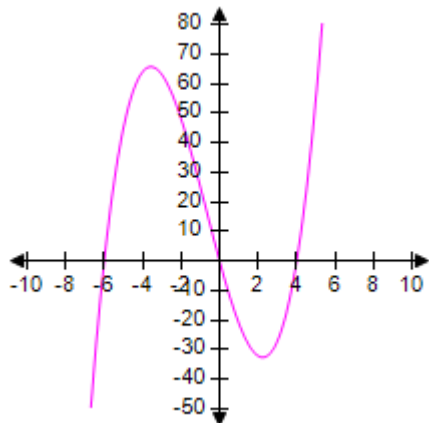


b.

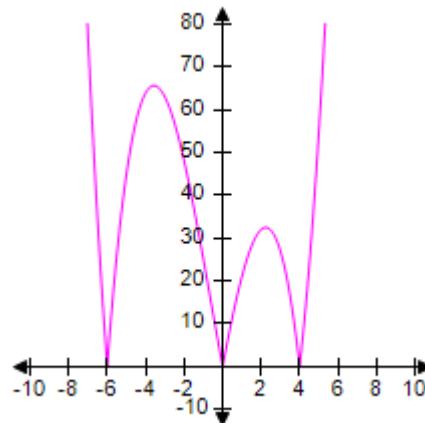


1.10 Solving Eqns and Ineqs Graphically

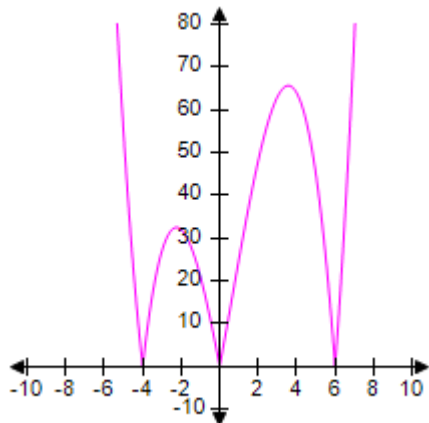
c.



d.



e.

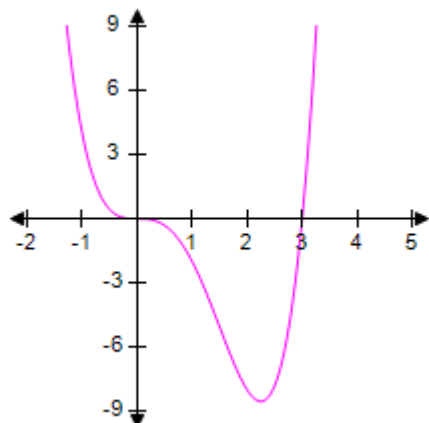


ANSWER: c

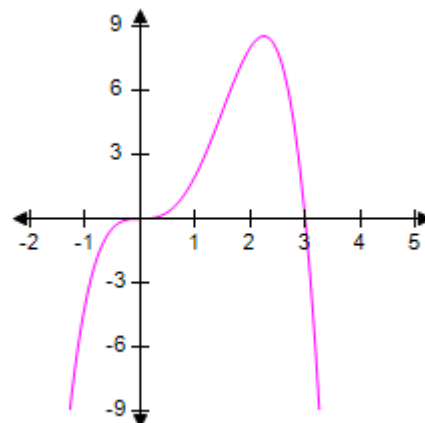
8. Draw the graph.

$$y = x^4 - 3x^3$$

a.

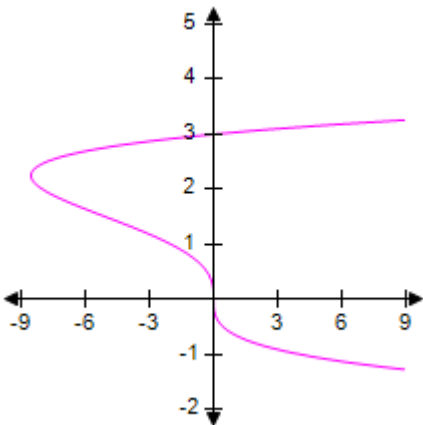


b.

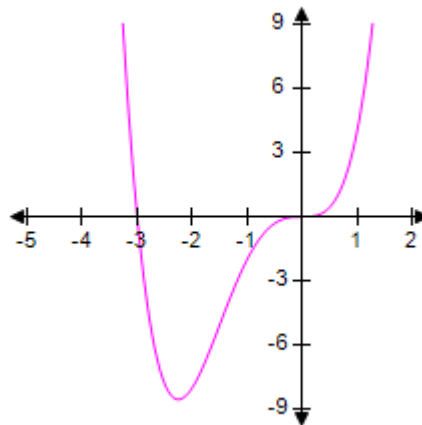


1.10 Solving Eqns and Ineqs Graphically

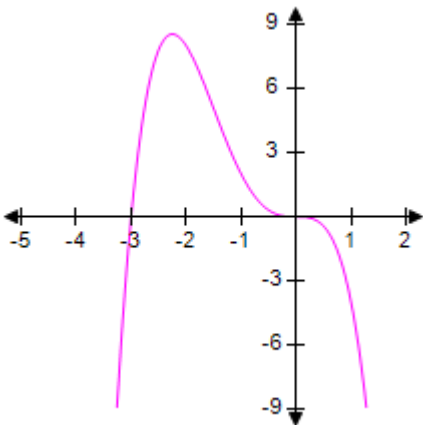
c.



d.



e.

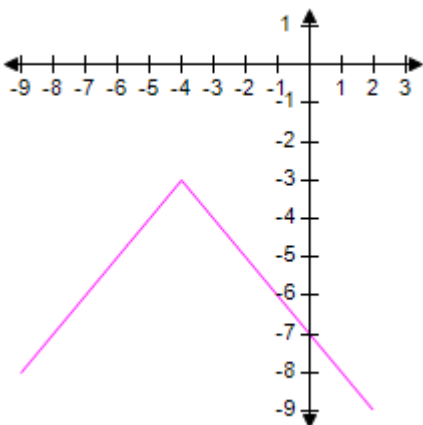


ANSWER: a

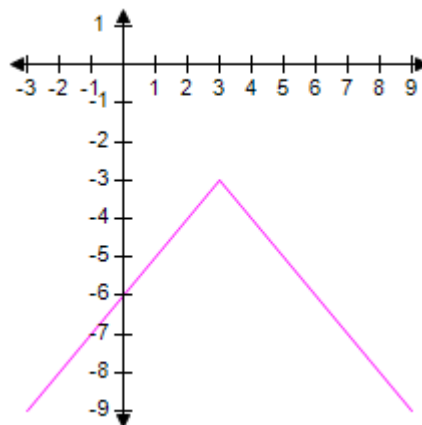
9. Draw the graph.

$$y = 3 + |x - 3|$$

a.

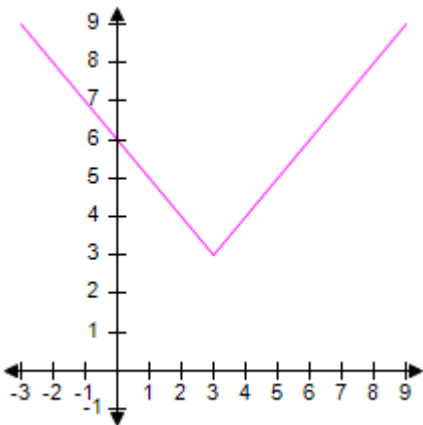


b.

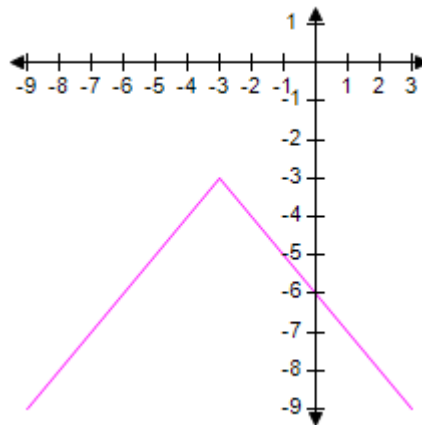


1.10 Solving Eqns and Ineqs Graphically

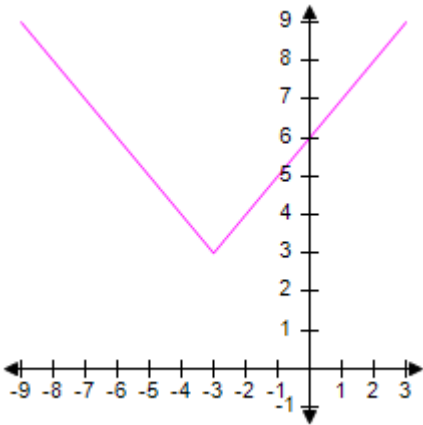
c.



d.



e.

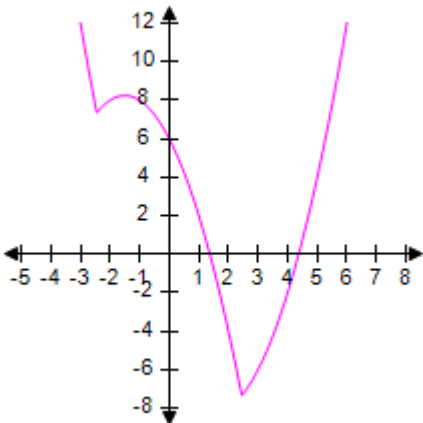


ANSWER: c

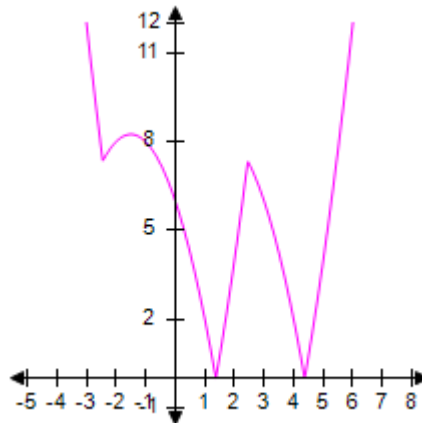
10. Draw the graph.

$$y = 3x - |x^2 - 6|$$

a.

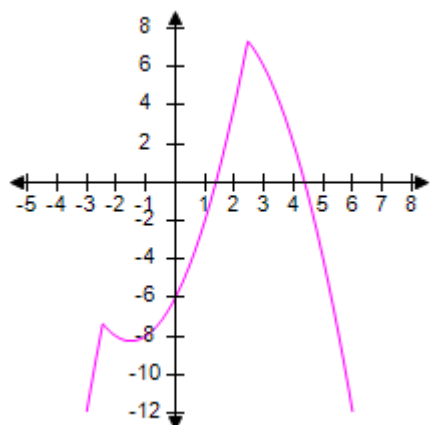


b.

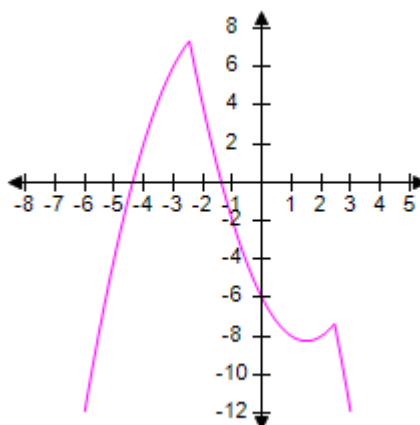


1.10 Solving Eqns and Ineqs Graphically

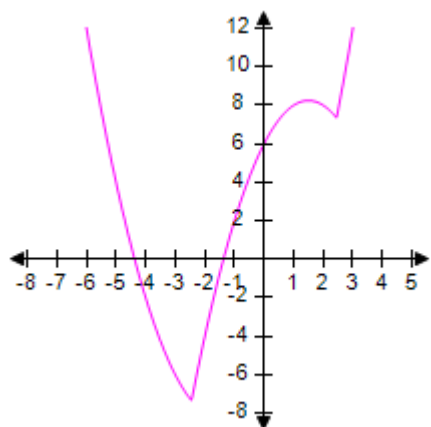
c.



d.



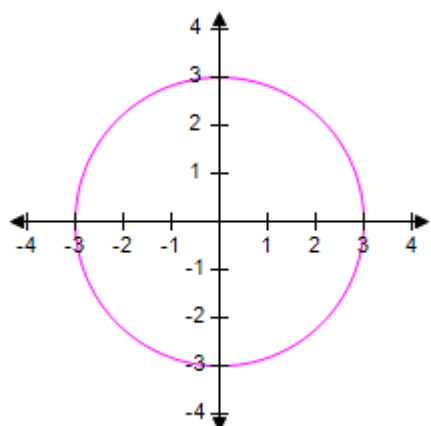
e.



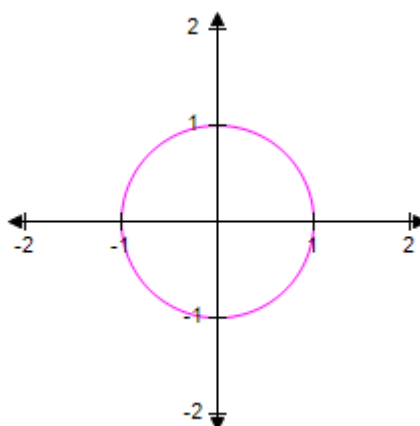
ANSWER: c

11. Graph the circle $x^2 + y^2 = 1$ by solving for y and graphing the two equations corresponding to the negative and positive square roots. (This graph is called a circle.).

a.

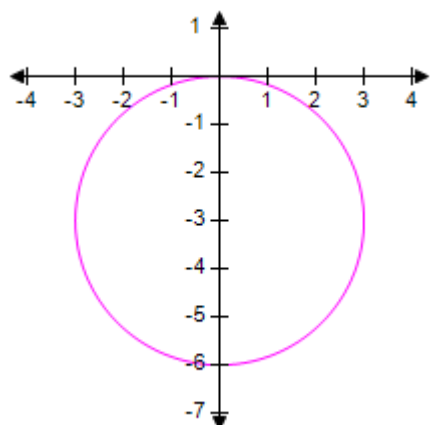


b.

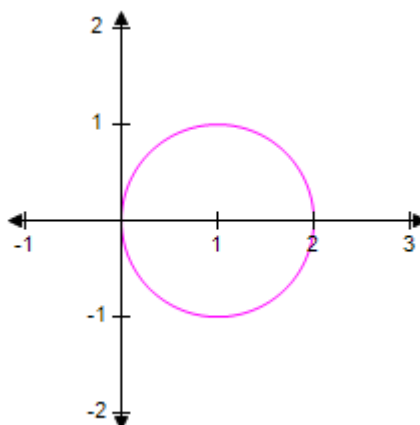


1.10 Solving Eqns and Ineqs Graphically

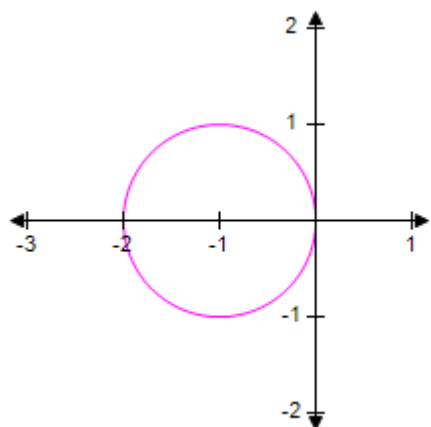
c.



d.



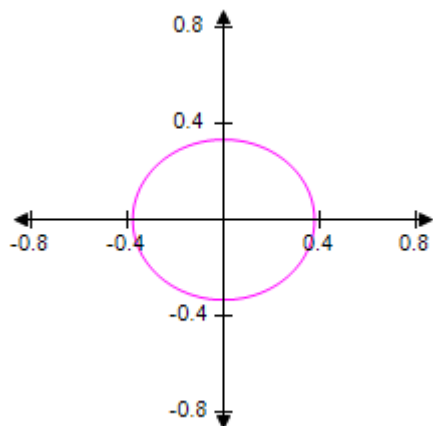
e.



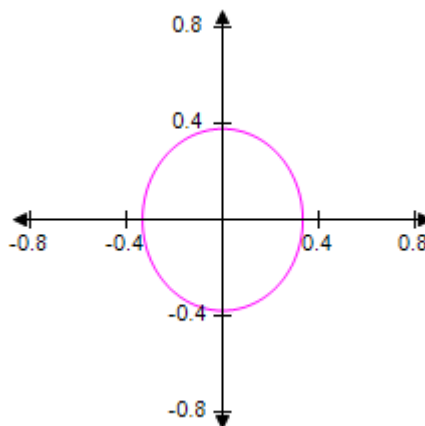
ANSWER: b

12. Graph the equation $9x^2 + 7y^2 = 1$ by solving for y and graphing the two equations corresponding to the negative and positive square roots. (This graph is called an ellipse.)

a.

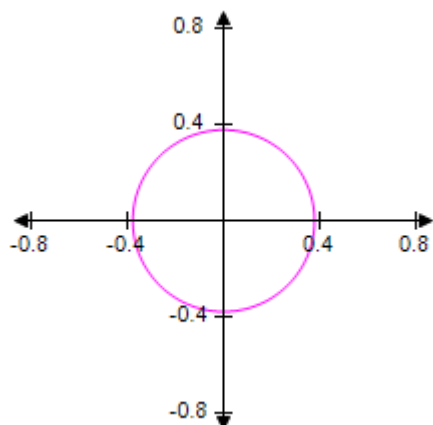


b.

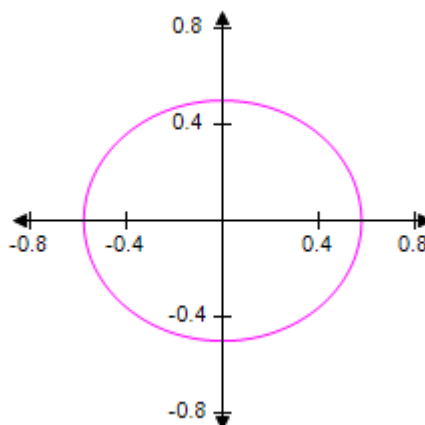


1.10 Solving Eqns and Ineqs Graphically

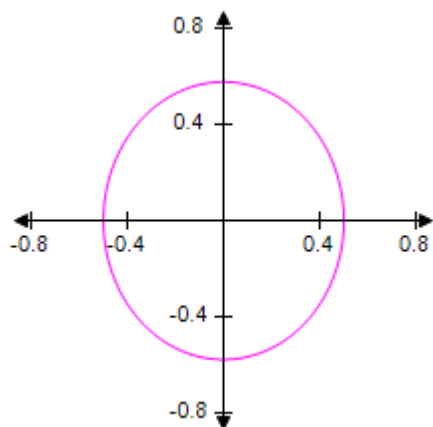
c.



d.



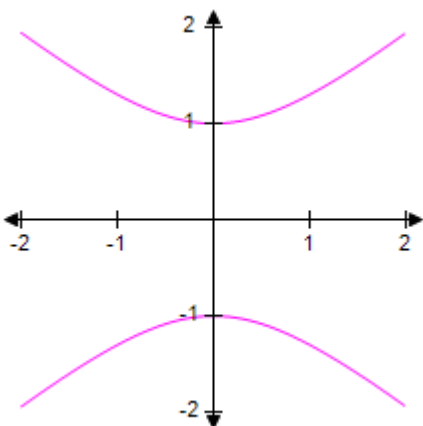
e.



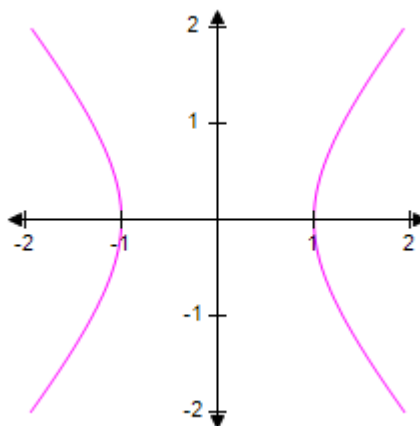
ANSWER: b

13. Graph the equation $y^2 - 25x^2 = 1$ by solving for y and graphing the two equations corresponding to the positive and negative square roots. (This graph is called a hyperbola.)

a.

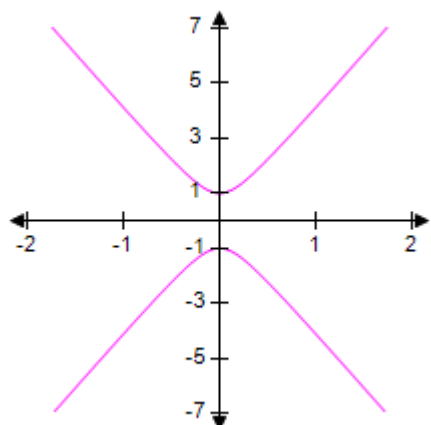


b.

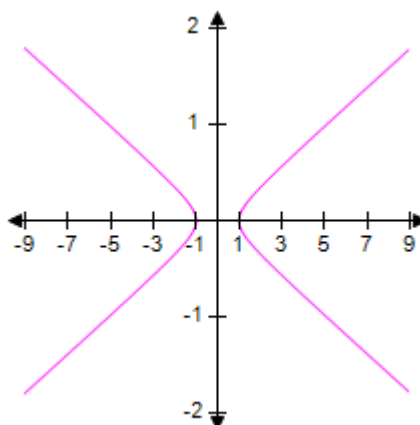


1.10 Solving Eqns and Ineqs Graphically

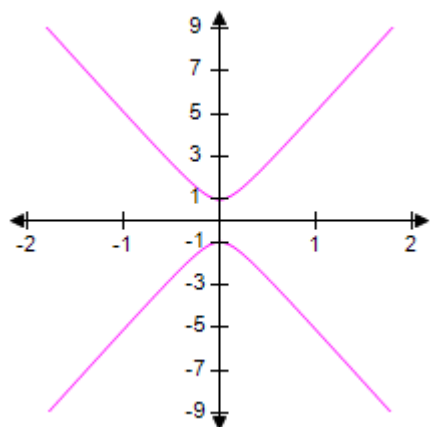
c.



d.



e.



ANSWER: e

14. Do the graphs of $y = -3x^2 + 6x - \frac{1}{2}$ and $y = \sqrt{7 - \frac{7}{10}x^2}$ intersect in the viewing rectangle $[-4, 4]$ by $[-1, 3]$?

If they intersect, determine the number of points of intersection.

- a. 4
- b. 0
- c. 5
- d. 2
- e. 1

ANSWER: b

15. Do the graphs of $y = 12 - 3x - x^2$ and $y = 3x + 21$ intersect in the viewing rectangle $[-7, 3]$ by $[-5, 23]$?

If they intersect, determine the number of points of intersection.

- a. 2
- b. 0

1.10 Solving Eqns and Ineqs Graphically

- c. 3
- d. 1
- e. 6

ANSWER: d

16. Solve the equation both algebraically and graphically.

$$x - 2 = 5x + 2$$

- a. $x = -1$
- b. $x = -3$
- c. $x = -2$
- d. $x = -5$
- e. $x = -7$

ANSWER: a

17. Solve the equation both algebraically and graphically.

$$\frac{1}{2}x - 4 = 8 + 2x$$

- a. $x = -2$
- b. $x = -1$
- c. $x = -8$
- d. $x = -10$
- e. $x = -7$

ANSWER: c

18. Solve the equation both algebraically and graphically.

$$\frac{2}{x} + \frac{1}{2x} = 5$$

- a. $x = \frac{1}{7}$
- b. $x = \frac{1}{5}$
- c. $x = \frac{1}{2}$
- d. $x = \frac{15}{19}$
- e. $x = \frac{1}{3}$

ANSWER: c

1.10 Solving Eqns and Ineqs Graphically

19. Solve the equation both algebraically and graphically.

$$\frac{3}{x+4} - \frac{6}{3x} = \frac{7}{3x+12}$$

- a. $x = 6$
- b. $x = -6$
- c. $x = -2$
- d. $x = 1$
- e. $x = -1$

ANSWER: b

20. Solve the equation both algebraically and graphically.

$$x^2 - 45 = 0$$

- a. $x = \pm 5\sqrt{2}$
- b. $x = \pm 5\sqrt{5}$
- c. $x = \pm 3\sqrt{5}$
- d. $x = \pm 2$
- e. $x = \pm 3\sqrt{2}$

ANSWER: c

21. Solve the equation both algebraically and graphically.

$$x^3 + 32 = 0$$

- a. $x = -2\sqrt[3]{4}$
- b. $x = -4\sqrt[3]{2}$
- c. $x = 4\sqrt[3]{4}$
- d. $x = -2\sqrt[3]{2}$
- e. $x = -4\sqrt[3]{4}$

ANSWER: a

22. Solve the equation both algebraically and graphically.

$$81x^4 = 625$$

- a. $x = \pm \frac{3}{5}$

1.10 Solving Eqns and Ineqs Graphically

b. $x = \pm \frac{5}{3}$

c. $x = \pm \frac{5}{6}$

d. $x = \pm \frac{6}{5}$

e. $x = \pm 3$

ANSWER: b

23. Solve the equation both algebraically and graphically.

$$5x^5 + 7,776 = 0$$

a. $x = -\frac{6}{\sqrt[5]{5}}$

b. $x = -\frac{4}{\sqrt[5]{5}}$

c. $x = \frac{6}{\sqrt[5]{5}}$

d. $x = \frac{4}{\sqrt[5]{5}}$

e. $x = \pm \frac{1}{\sqrt[5]{5}}$

ANSWER: a

24. Solve the equation both algebraically and graphically.

$$(x - 7)^4 - 405 = 0$$

a. $x = \pm 3\sqrt[4]{3}$

b. $x = 7 \pm 2\sqrt[4]{3}$

c. $x = 7 \pm 3\sqrt[4]{5}$

d. $x = 7 \pm 3\sqrt[4]{3}$

e. $x = 7 \pm 2\sqrt[4]{5}$

ANSWER: c

25. Solve the equation both algebraically and graphically.

$$21(x + 2)^5 = 729$$

1.10 Solving Eqns and Ineqs Graphically

a. $x = -2 + \frac{3}{\sqrt[5]{6}}$

b. $x = -2 + \frac{2}{\sqrt[5]{7}}$

c. $x = -2 + \frac{3}{\sqrt[5]{7}}$

d. $x = \frac{3}{\sqrt[5]{6}}$

e. $x = -2 + \frac{2}{\sqrt[5]{6}}$

ANSWER: c26. Solve the equation $x^2 - 10x + 24 = 0$ graphically in the interval $[0, 8]$.

a. $x = 4, x = 6$

b. $x = 4, x = 7$

c. $x = 4$

d. $x = 5, x = 7$

e. $x = 5, x = 6$

ANSWER: a27. Solve the equation $x^3 - 10x^2 + 29x - 20 = 0$ graphically in the interval $[-1, 8]$.

a. $x = 1.00, x = 4.50, x = 5.00$

b. $x = 1.00, x = 4.00, x = 5.00$

c. $x = 3.50, x = 4.50, x = 5.50$

d. $x = 3.50, x = 4.00, x = 5.00$

e. $x = 1.00, x = 4.00, x = 5.50$

ANSWER: b28. Solve the equation $25x^3 + 50x^2 = x + 2$ graphically in the interval $[-4, 4]$.

a. $x = -3.00, x = -0.20, x = 0.20$

b. $x = -3.00, x = -0.33, x = 0.33$

c. $x = -3.00, x = -0.25, x = 0.25$

d. $x = -2.00, x = -0.33, x = 0.33$

e. $x = -2.00, x = -0.20, x = 0.20$

ANSWER: e29. Solve the equation $x - \sqrt{x + 8} = 0$ graphically in the interval $[-8, 7]$.

If necessary, round your answer(s) to the nearest hundredth.

1.10 Solving Eqns and Ineqs Graphically

- a. $x = -2.35$
- b. $x = -2.35, x = 3.35$
- c. $x = 3.37$
- d. $x = 3.35$
- e. $x = -2.37, x = 3.37$

ANSWER: c30. Find all real solutions of the equation $x^4 - 8x^2 + 3 = 0$.

If necessary, round your answer(s) to the nearest hundredth.

- a. $-2.74, -0.61, 0.61, 2.74$
- b. $-2.74, -0.63, 0.63, 2.74$
- c. $-2.76, -0.63, 0.63, 2.76$
- d. $-2.80, -0.67, 0.67, 2.80$
- e. $-2.76, -0.61, 0.61, 2.76$

ANSWER: c31. Find all real solutions of the equation $x(x-5)(x+6) = \frac{1}{7}x$

If necessary, round your answer(s) to the nearest hundredth.

- a. $-6.01, 0, 5.01$
- b. $-5.99, 0, 5.01$
- c. $-5.99, 0, 4.99$
- d. $-6.05, 0, 5.05$
- e. $-6.01, 0, 4.99$

ANSWER: a32. Do the graphs of $y = -3x^2 + 6x - \frac{1}{2}$ and $y = \sqrt{7 - \frac{7}{10}x^2}$ intersect in the viewing rectangle $[-4, 4]$ by $[-1, 3]$?

Determine the number of points of intersection. If there are no points of intersection, answer 0.

ANSWER: 033. Do the graphs of $y = 12 - 2x - x^2$ and $y = 3x + 18$ intersect in the viewing rectangle $[-6, 3]$ by $[-5, 20]$?

Determine the number of points of intersection. If there are no points of intersection, answer 0.

ANSWER: 234. Solve the equation $x - \sqrt{x+9} = 0$ graphically in the interval $[-9, 6]$.

Round your answer to two decimal places.

1.10 Solving Eqns and Ineqs Graphically

$x =$ _____
ANSWER: 3.54

35. Solve the equation $x^2 - 5x + 6 = 0$ graphically in the interval $[0, 5]$.

$x =$ _____
ANSWER: 2, 3

36. Solve the equation $x^3 - 14x^2 + 55x - 42 = 0$ graphically in the interval $[-1, 8]$.

$x =$ _____
ANSWER: 1, 6, 7

37. Solve the equation $25x^3 + 50x^2 = x + 2$ graphically in the interval $[-4, 4]$.

$x =$ _____
ANSWER: -2, -0.2, 0.2

38. Find all real solutions of the equation $x^4 - 4x^2 + 2 = 0$

$x =$ _____
ANSWER: -1.85, -0.77, 0.77, 1.85

Use a graphing calculator to decide which viewing rectangle produces the most appropriate graph of the equation.

Match each viewing rectangle below with the letter of the corresponding equation.

- a. $y = x^4 + 2$
- b. $y = -x^4 - 2$
- c. $x = y^4 + 2$
- d. $x = -y^4 - 2$

39. $[-4, 4]$ by $[-4, 40]$
ANSWER: a

40. $[-4, 4]$ by $[-40, 4]$
ANSWER: b

41. $[-4, 40]$ by $[-4, 4]$
ANSWER: c

42. $[-40, 4]$ by $[-4, 4]$
ANSWER: d

1.10 Solving Eqns and Ineqs Graphically

43. Find all real solutions of the equation $x(x-5)(x+6) = \frac{1}{4}x$.

$x =$ _____

ANSWER: -6.02, 0, 5.02

Use a graphing calculator to decide which viewing rectangle produces the most appropriate graph of the equation.

Match each viewing rectangle below with the letter of the corresponding equation.

a. $y = 10 + 25x - x^3$

b. $y = (x-5)^3$

c. $y = x^2 + 5x$

d. $y = -x^3 + 10$

44. $[-10, 10]$ by $[-150, 150]$

ANSWER: a

45. $[-10, 5]$ by $[-20, 80]$

ANSWER: c

46. $[-1, 10]$ by $[-150, 150]$

ANSWER: b

1.11 Modeling Variation

1. Express the statement as a formula.

t is jointly proportional to the quantities x and y and inversely proportional to r .

Determine if the table is either true or false where c is given as the constant of proportionality.

x	y	r	t	c
9	-45	9	45	-1
27	90	-18	270	2
45	-135	27	1,125	5

a. True

b. False

ANSWER: False

2. The cost C of printing a magazine is jointly proportional to the number of pages p in the magazine and the number of magazines printed m . And, for this problem, k is the constant of proportionality.

$C(\$)$	p	m	k
9,800	50	2,800	0.07
4,800	120	2,000	0.02
1,180	20	5,900	0.01

Determine if the values in this table are true or false.

a. True

b. False

ANSWER: True

3. Determine the equation that expresses the statement.

G varies directly as x .

The symbols a , b , c , and d are constants.

a. $G = t \times x$

b. $G = ax^2 + b$

c. $G = cx$

d. $G = d$

e. $G = c/x$

ANSWER: c

4. Determine the equation that expresses the statement.

F is directly proportional to z .

Symbols a , b , c , and d are constants.

a. $F = b$

b. $F = cz^3 + d$

1.11 Modeling Variation

c. $F = a$

d. $F = cz^5 + d$

e. $F = a \cdot z$

ANSWER: e

5. Determine the equation that expresses “ D is jointly proportional to G and x .” Symbols a , b , c , d , and f are constants.

a. $D = dGx^2 + f$

b. $D = aG + bx$

c. $D = cGx$

d. $D = cxGx$

e. $D = cG$

ANSWER: c

6. Determine the equation that expresses “ d is proportional to G and inversely proportional to z .” Symbols a , b , and c are constants.

a. $d = c \frac{G}{z}$

b. $d = \frac{G}{z}$

c. $d = zc \frac{G}{z}$

d. $d = aGz$

e. $d = b \frac{z}{G}$

ANSWER: a

7. Write an equation that expresses “ y as it varies inversely as R .” The symbols a , b , c , and d are constants.

a. $y = \frac{a}{R}$

b. $y = cR + d$

c. $y = \frac{R}{b}$

d. $y = R \frac{a}{y}$

e. $y = R - aR$

ANSWER: a

8. Write an equation that expresses “ G is proportional to the square root of z ” The symbols a , b , c , and d are constants.

a. $G = b\sqrt{z}$

1.11 Modeling Variation

b. $G = c + \sqrt{z}$

c. $G = \sqrt{2a} \cdot \sqrt{2d}$

d. $G = \sqrt{b + \sqrt{a - z}}$

e. $G = \frac{a}{\sqrt{z}}$

ANSWER: a

9. Determine the equation that expresses “ G is proportional to the square of z and inversely proportional to the cube of d .” Symbols a , b , c , and d are constants.

a. $G = d \frac{d^3}{z^2}$

b. $G = c \frac{d^2}{z^3}$

c. $G = az^2 + bd^3$

d. $G = c \frac{z^2}{d^3}$

e. $G = c \frac{z^3}{d^2}$

ANSWER: d

10. Determine the equation expressing the formula “ F is jointly proportional to the squares of y and A .” Symbols a , b , c , and d are constants.

a. $F = by^2 + A^2$

b. $F = ay^2 A^2$

c. $F = cy^2 A + d$

d. $F = ay^3 A^3$

e. $F = ay^2 b^2$

ANSWER: b

11. Determine the equation that expresses that “ R is proportional to k and inversely proportional to B and x .” Symbols a , b , and c are constants.

a. $R = \frac{ck}{xB}$

b. $R = \frac{ck}{RR}$

1.11 Modeling Variation

c. $R = \frac{a}{bc}$

d. $R = \frac{bB}{xk}$

e. $R = \frac{ax}{kB}$

ANSWER: a

12. Express the statement as a formula.

y is directly proportional to x .

If $x = 6$ and $y = 36$, what is the constant of proportionality?

a. 11

b. $\frac{1}{6}$

c. 6

d. 10

e. 9

ANSWER: c

13. Express the statement as a formula.

M varies directly as x and inversely as y .

If $x = 48$, $y = -8$, and $M = -6$, what is the constant of proportionality?

a. 3

b. 5

c. 1

d. 11

e. 2

ANSWER: c

14. Express the statement as a formula.

s is inversely proportional to the square root of t .

If $s = 13$ and $t = 9$, what is the constant of proportionality?

a. 39

b. 13

c. 42

d. 1

e. 117

ANSWER: a

1.11 Modeling Variation

15. The pressure P of a sample of gas is directly proportional to the temperature T and inversely proportional to the volume V . 120 L of gas exerts a pressure of 33.7 kPa at a temperature of 300 K (absolute temperature measured on the Kelvin scale).

If the temperature is increased to 500 K and the volume is decreased to 50 L, what is the pressure of the gas?

- a. 134.80 kPa
- b. 80.88 kPa
- c. 124.65 kPa
- d. 0.11 kPa
- e. 144.80 kPa

ANSWER: a

16. The resistance R of a wire varies directly as its length L and inversely as the square of its diameter d . Find the constant of proportionality K if a wire 1.7 m long and 0.001 m in diameter has a resistance of 17 ohms. Find the resistance R_1 of a wire made of the same material that is 3 m long and has a diameter of 0.005 m.

- a. $K = 0.00001$; $R_1 = 14.4$
- b. $K = 0.000001$; $R_1 = 0.12$
- c. $K = 0.000001$; $R_1 = 3.98$
- d. $K = 0.00001$; $R_1 = 1.2$
- e. $K = 0.00001$; $R_1 = 0.006$

ANSWER: d

17. In the short growing season of the Canadian arctic territory of Nunavut, some gardeners find it possible to grow gigantic cabbages in the midnight sun. Assume that the final size of a cabbage is proportional to the amount of nutrients it receives, and inversely proportional to the number of other cabbages surrounding it. A cabbage that received 25 oz of nutrients and had 10 other cabbages around it grew to 25 lb. What size would it grow to if it received 5 oz of nutrients and had only 5 cabbage neighbors?

- a. 9
- b. 10
- c. 11
- d. 12
- e. 6

ANSWER: b

18. The value of a building lot on Galiano Island is jointly proportional to its area and the quantity of water produced by a well on the property. A 500 ft by 100 ft lot has a well producing 5 gallons of water per minute, and is valued at \$12,000. What is the value of a 300 ft by 300 ft lot if the well on the lot produces 6 gallons of water per minute?

- a. \$28,468
- b. \$20,736
- c. \$27,030
- d. \$38,880
- e. \$25,920

1.11 Modeling Variation

ANSWER: e

19. The heat experienced by a hiker at a campfire is proportional to the amount of wood on the fire, and inversely proportional to the cube of his distance from the fire. If he is 19 ft from the fire, and someone doubles the amount of wood burning, approximately how far from the fire would he have to be so that he feels the same heat as before?

- a. 24 ft
- b. 13 ft
- c. 38 ft
- d. 90 ft
- e. 28.5 ft

ANSWER: a

20. A car is traveling on a curve that forms a circular arc. The force F needed to keep the car from skidding is jointly proportional to the weight w of the car and the square of its speed s , and is inversely proportional to the radius r of the curve. A car weighing 900 lb travels around a curve at 80 mi/h. The next car to round this curve weighs 2,500 lb and requires the same force as the first car to keep from skidding. How fast is the second car traveling?



- a. 46 mi/h
- b. 42 mi/h
- c. 44 mi/h
- d. 48 mi/h
- e. 49 mi/h

ANSWER: d

21. The stopping distance D of a car after the brakes have been applied varies directly as the square of the speed s . A certain car traveling at 54 mi/h can stop in 230 ft. What is the maximum speed it can be traveling if it needs to stop in 170 ft? Please round the answer to the nearest tenth.

- a. $s = 73.1$ mi/h
- b. $s = 41.4$ mi/h
- c. $s = 62.8$ mi/h
- d. $s = 46.4$ mi/h
- e. $s = 6.3$ mi/h

ANSWER: d

22. The power P that can be obtained from a windmill is directly proportional to the cube of the wind speed s . Find the

1.11 Modeling Variation

constant of proportionality for a windmill that produces 97 watts of power when the wind is blowing at 23 mi/h. Please round your answer to four decimal places.

a. $k = 0.1834 \text{ watts} \cdot \text{h}^3/\text{mi}^3$

b. $k = 0.0085 \text{ watts} \cdot \text{h}^3/\text{mi}^3$

c. $k = 0.0070 \text{ watts} \cdot \text{h}^3/\text{mi}^3$

d. $k = 4.2174 \text{ watts} \cdot \text{h}^3/\text{mi}^3$

e. $k = 0.0080 \text{ watts} \cdot \text{h}^3/\text{mi}^3$

ANSWER: e

23. Express the statement as a formula.

y is directly proportional to x .

If $x = 11$ and $y = -33$, what is the constant of proportionality?

ANSWER: -3

24. Express the statement as a formula.

M varies directly as x and inversely as y .

If $x = -63$, $y = -7$, and $M = 18$, what is the constant of proportionality?

ANSWER: 2

25. Express the statement as a formula.

s is inversely proportional to the square root of t .

If $s = 5$ and $t = 4$, what is the constant of proportionality?

ANSWER: 10

26. In the short growing season of the Canadian arctic territory of Nunavut, some gardeners find it possible to grow gigantic cabbages in the midnight sun. Assume that the final size of a cabbage is proportional to the amount of nutrients it receives, and inversely proportional to the number of other cabbages surrounding it. A cabbage that received 35 oz of nutrients and had 10 other cabbages around it grew to 30 lb. What size would it grow to if it received 17.5 oz of nutrients and had only 5 cabbage neighbors?

Round to the nearest tenth, if necessary.

_____ lbs

ANSWER: 30

27. The value of a building lot on Galiano Island is jointly proportional to its area and the quantity of water produced by a well on the property. A 300 ft by 400 ft lot has a well producing 4 gallons of water per minute, and is valued at \$10,000. What is the value of a 800 ft by 800 ft lot if the well on the lot produces 10 gallons of water per minute?

Round to the nearest dollar.

\$ _____

ANSWER: 133,333

1.11 Modeling Variation

28. The stopping distance D of a car after the brakes have been applied varies directly as the square of the speed s . A certain car traveling at 47 mi/h can stop in 245 ft. What is the maximum speed it can be traveling if it needs to stop in 155 ft? Please round the answer to the nearest tenth.

$$s = \underline{\hspace{2cm}} \text{ mi/h}$$

ANSWER: 37.4

29. The pressure P of a sample of gas is directly proportional to the temperature T and inversely proportional to the volume V .

Find the constant of proportionality if 90 L of gas exerts a pressure of 35 kPa at a temperature of 200 K (absolute temperature measured on the Kelvin scale). Round your answer to three decimal places.

$$k = \underline{\hspace{2cm}}$$

If the temperature is increased to 800 K and the volume is decreased to 70 L, what is the pressure of the gas? Round your answer to three decimal places.

$$P = \underline{\hspace{2cm}} \text{ kPa}$$

ANSWER: 15.750; 180.000

30. Write an equation that expresses the statement.

R varies directly as y .

ANSWER: $R = cy$

31. Write an equation that expresses the statement.

N is directly proportional to x .

ANSWER: $N = cx$

32. Write an equation that expresses “ y as it varies inversely as F .”

ANSWER: $y = \frac{c}{F}$

33. Write an equation that expresses that “ G is proportional to the square root of t .”

ANSWER: $G = c\sqrt{t}$

34. Write an equation that expresses “ G is proportional to the square of y and inversely proportional to the cube of B .”

ANSWER: $G = \frac{cy^2}{B^3}$

35. Write an equation that expresses “ G is jointly proportional to the squares of y and B .”

ANSWER: $G = c \cdot y^2 \cdot B^2$

36. Write an equation that expresses “ F is proportional to n and inversely proportional to d and x .”

ANSWER: $F = \frac{c \cdot n}{dx}$

1.11 Modeling Variation

37. The resistance R of a wire varies directly as its length L and inversely as the square of its diameter d .

Find the constant of proportionality if a wire 1 m long and 0.001 m in diameter has a resistance of 10 ohms. _____

Next find the resistance of a wire made of the same material that is 3 m long and has a diameter of 0.002 m. _____

ANSWER: 0.00001, 7.5

38. The pressure P of a sample of gas is directly proportional to the temperature T and inversely proportional to the volume V .

Find the constant of proportionality if 110 L of gas exerts a pressure of 30.1 kPa at a temperature of 200 K (absolute temperature measured on the Kelvin scale). Round to three decimal places.

$k =$ _____

If the temperature is increased to 800 K and the volume is decreased to 70 L, what is the pressure of the gas? Round to three decimal places.

$kPa =$ _____

ANSWER: 16.555, 189.200

The heat experienced by a hiker at a campfire is proportional to the amount of wood on the fire, and inversely proportional to the cube of his distance from the fire. If he is x ft from the fire, and someone doubles the amount of wood burning, how far from the fire would he have to be so that he feels the same heat as before?

Match each new distance below with the letter of the corresponding old distance.

a. $x = 15$ ft

b. $x = 20$ ft

c. $x = 26$ ft

d. $x = 30$ ft

e. $x = 24$ ft

39. 30.24 ft

ANSWER: e

40. 18.90 ft

ANSWER: a

41. 37.80 ft

ANSWER: d

42. 25.20 ft

ANSWER: b

43. 32.76 ft

ANSWER: c